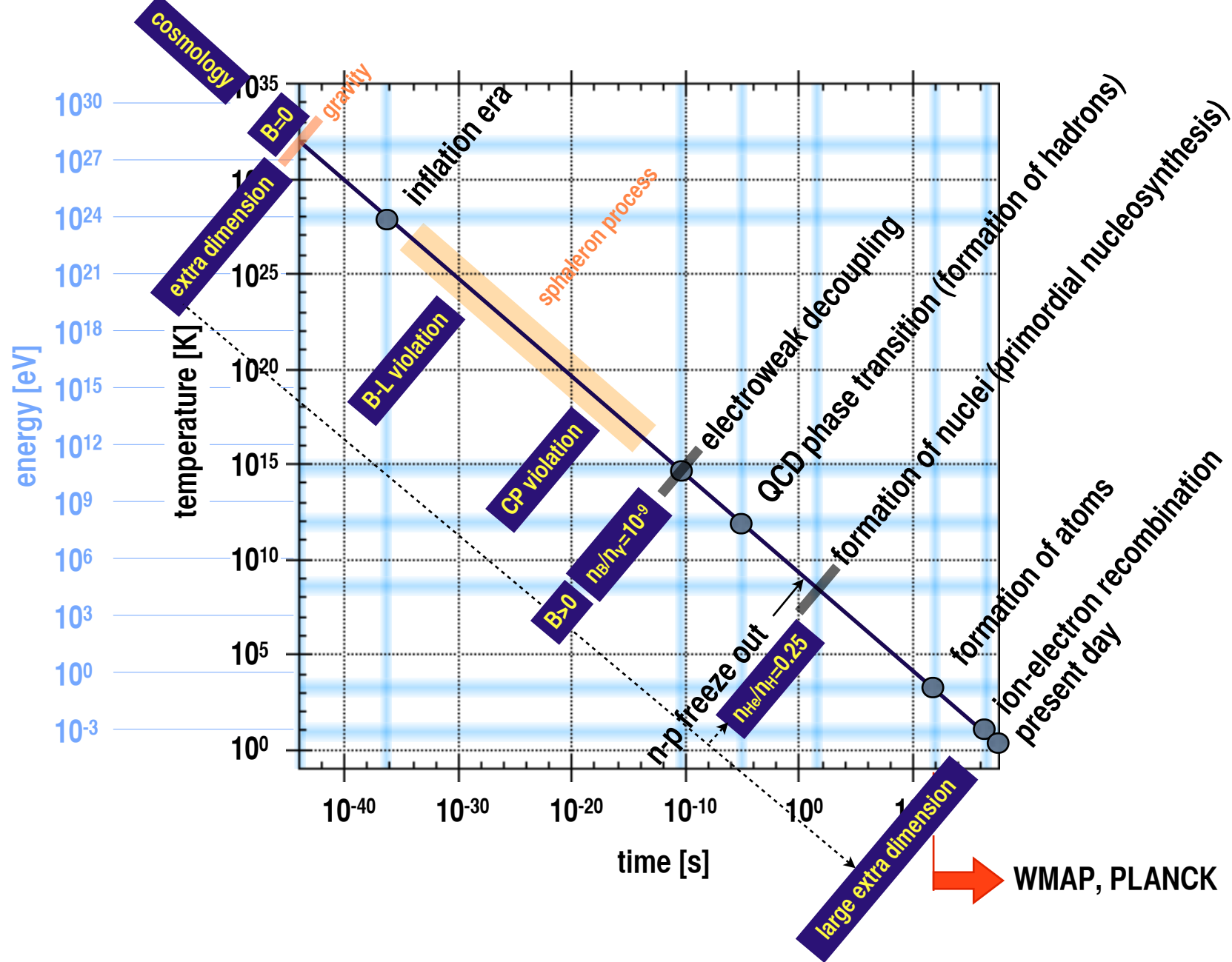


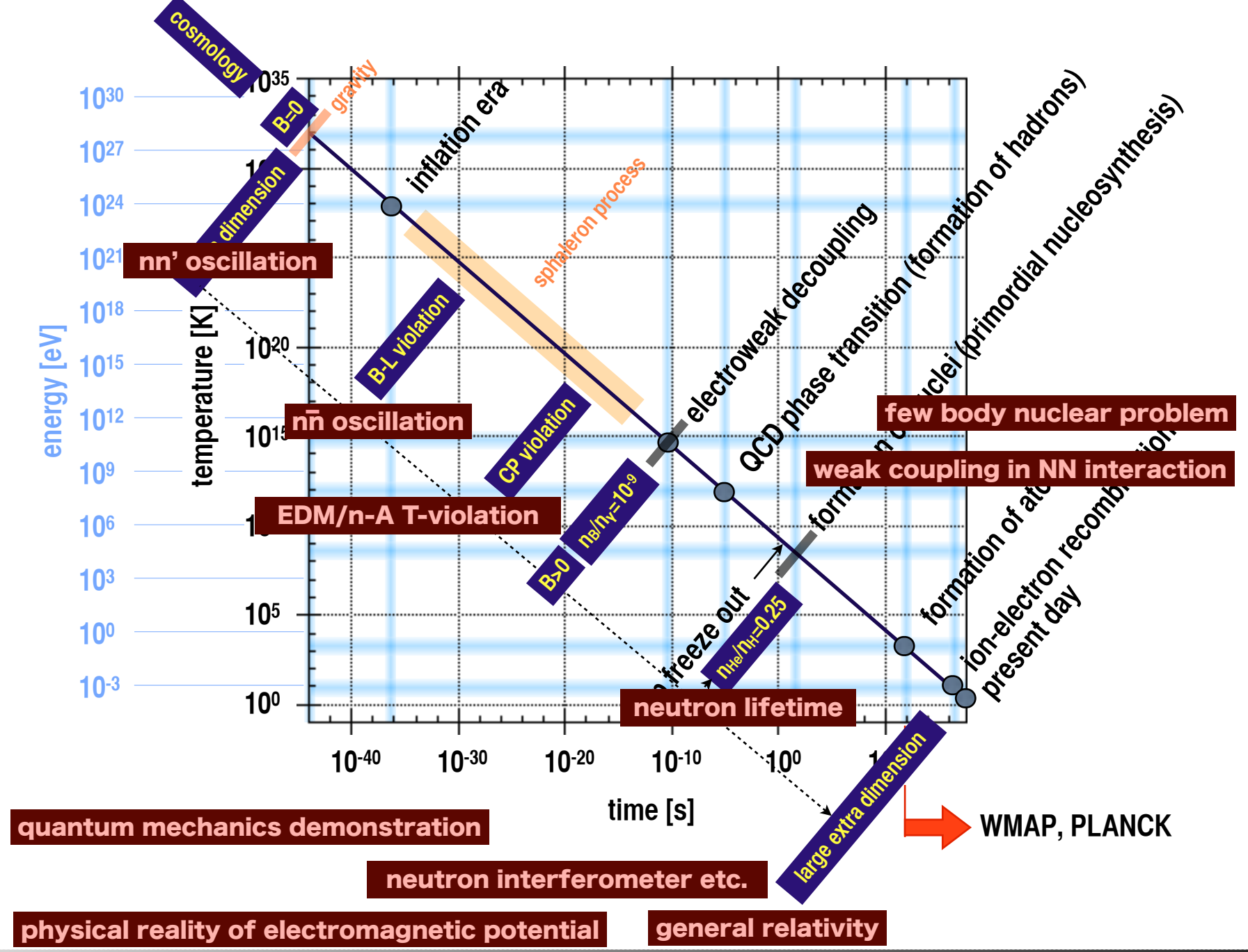
Very Cold Neutrons for Fundamental Physics

Hirohiko SHIMIZU

Department of Physics, Nagoya University

hirohiko.shimizu@nagoya-u.jp



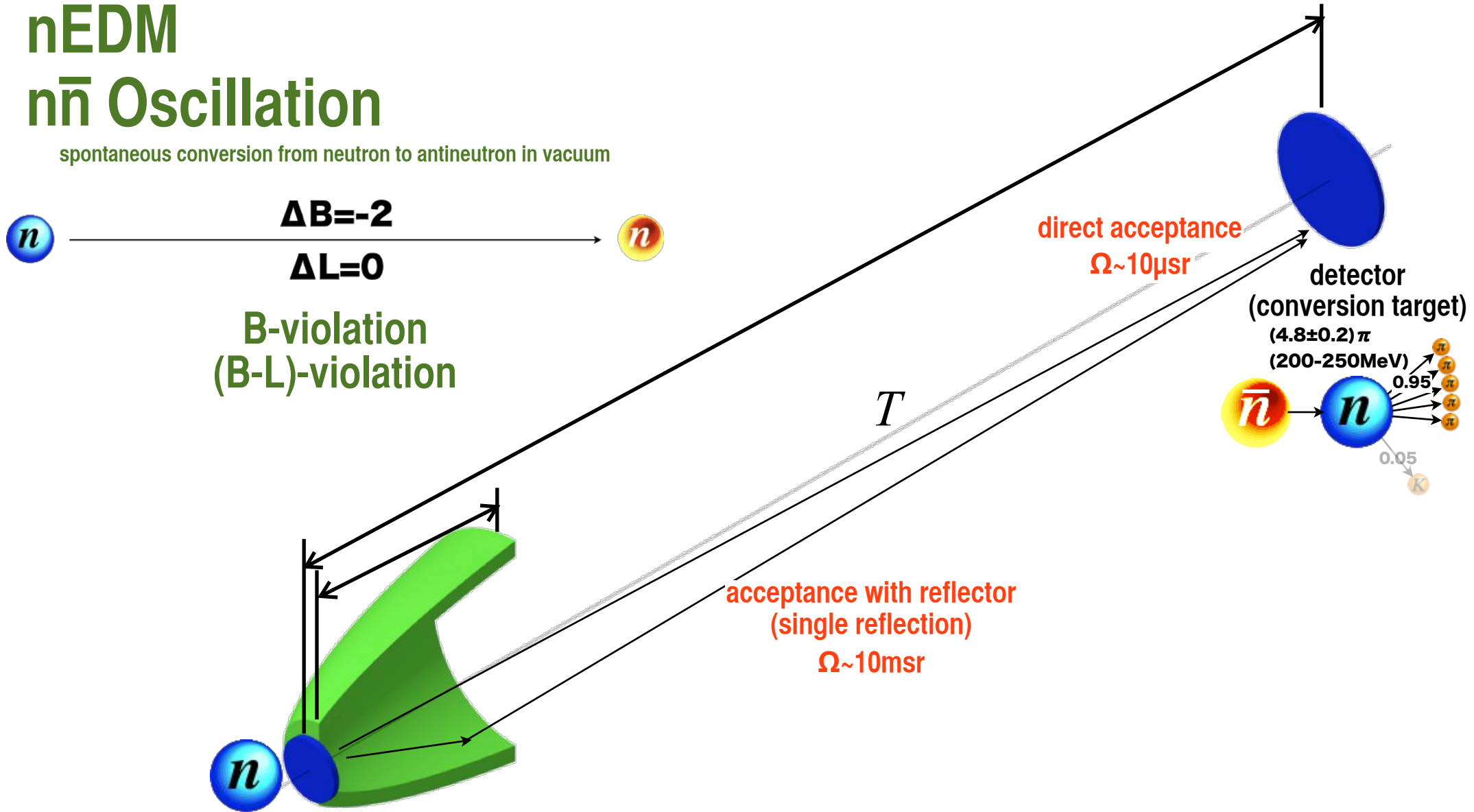


n β -decay

nEDM

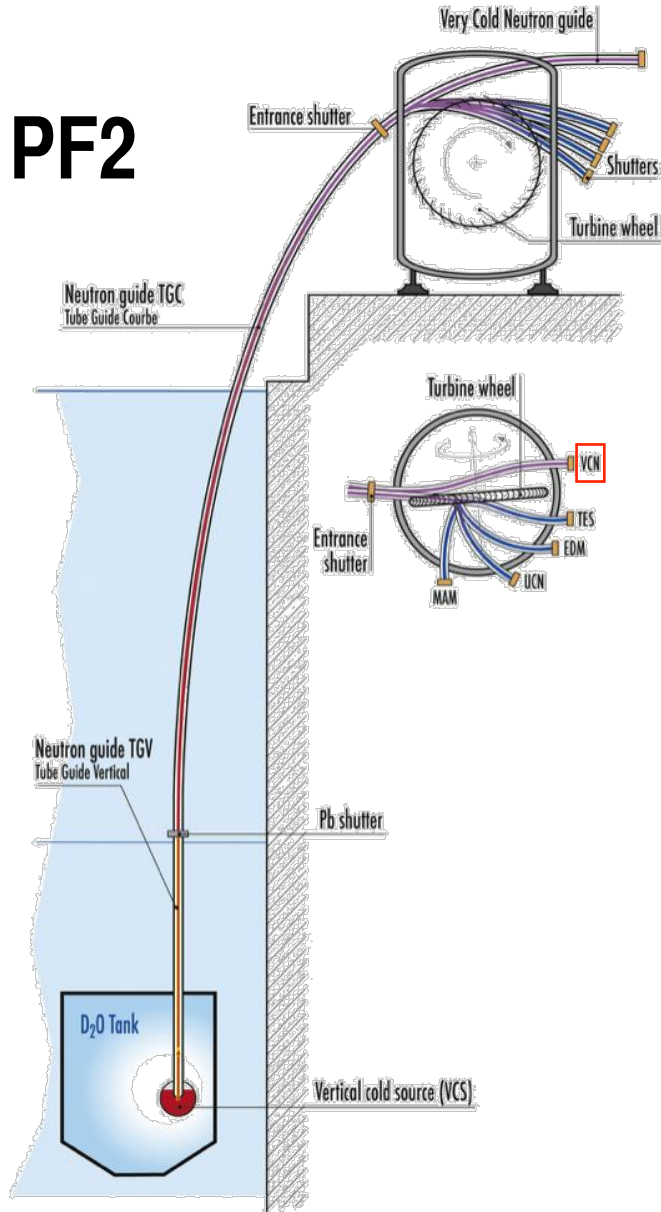
n \bar{n} Oscillation

spontaneous conversion from neutron to antineutron in vacuum



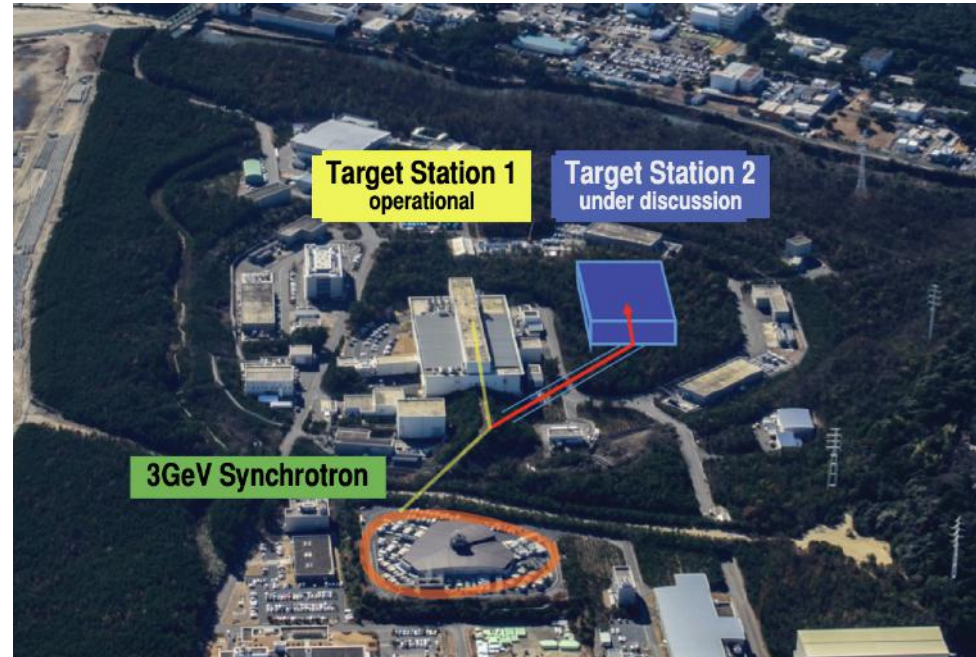
Very cold neutrons

ILL PF2



SNS-STS ESS

J-PARC MLF 2nd Target Station Conceptual Design ver.1.1 (2019/03/22)

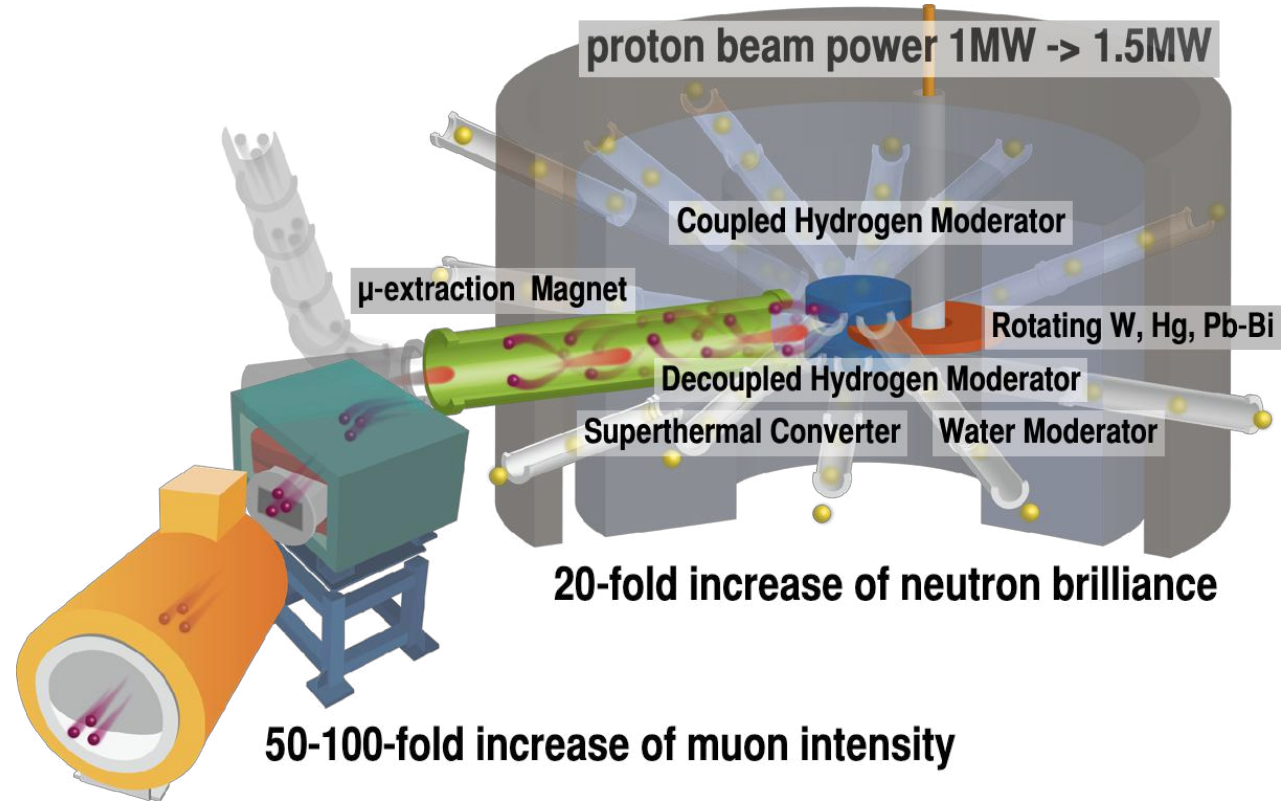
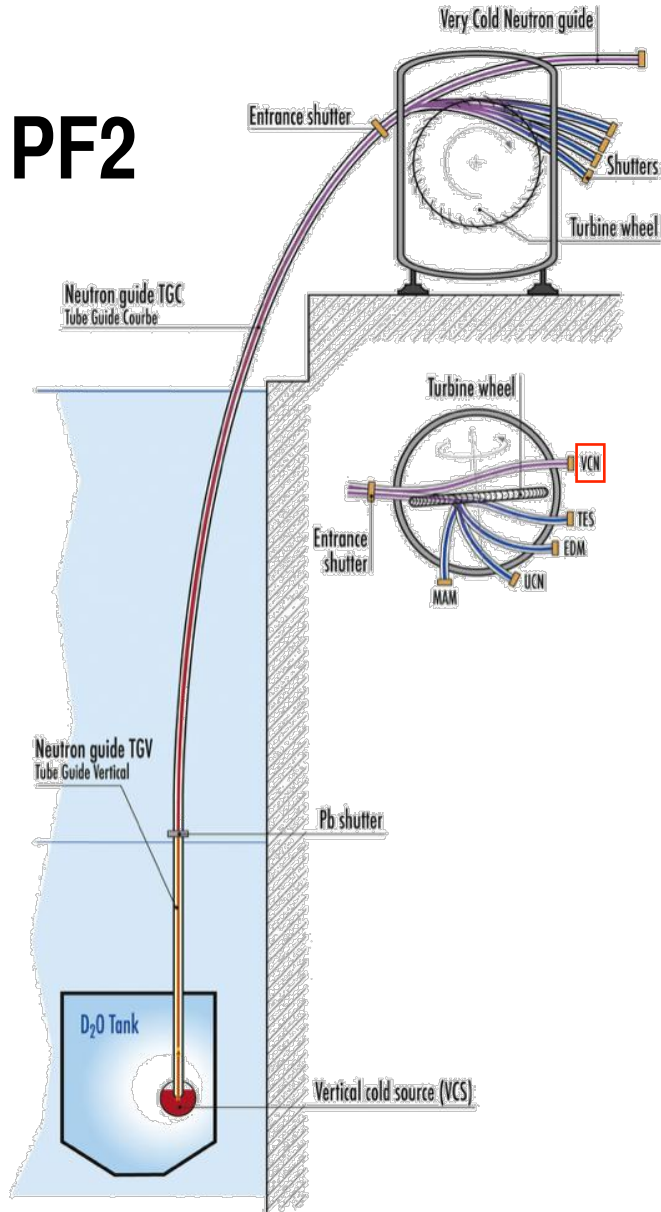


Very cold neutrons

SNS-STS ESS

J-PARC MLF 2nd Target Station Conceptual Design ver.1.1 (2019/03/22)

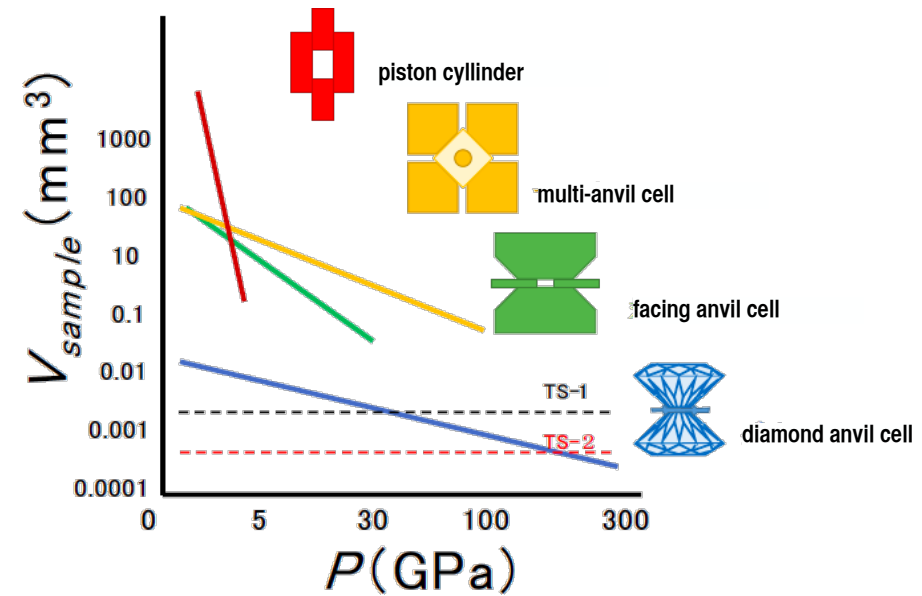
ILL PF2



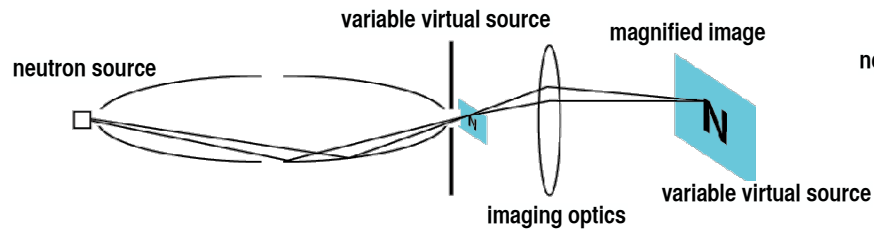
Very cold neutrons

with high phase-space-density
with flexible optical control
similar to photon optics

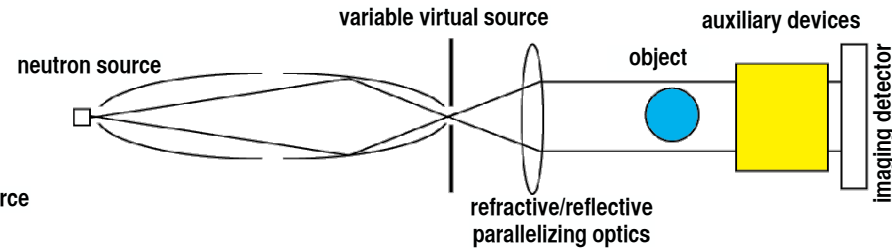
enable various applications.



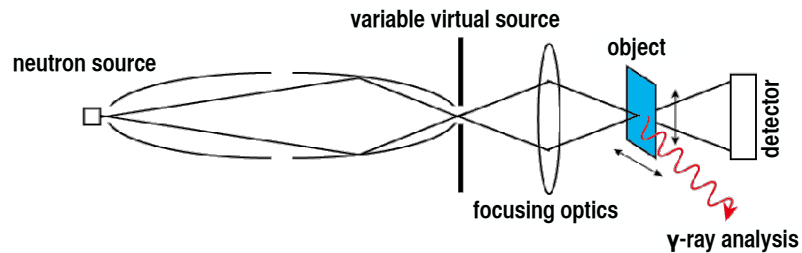
high-resolution imaging



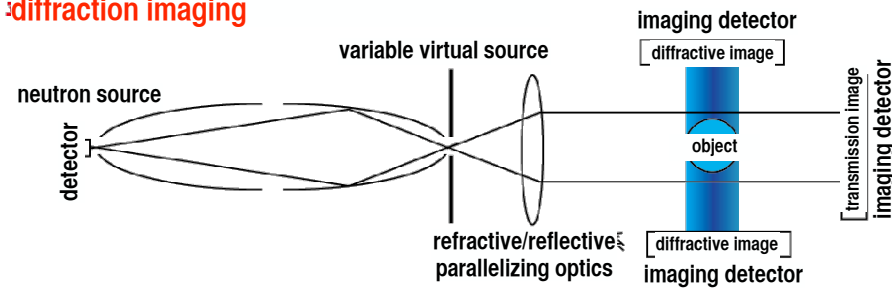
versatile imaging



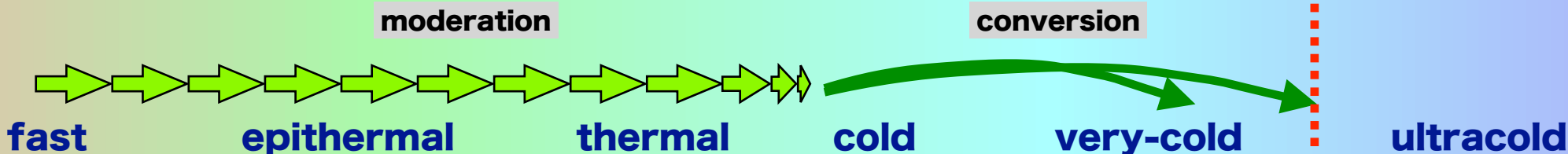
scanning imaging, scanning prompt gamma-ray analysis



diffraction imaging



neutron



kinetic energy

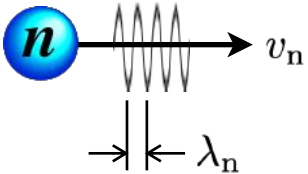
MeV eV meV μeV neV

temperature

10^{10}K 10^9K 10^5K 10^4K 10^3K 100K 10K 1K 0.1K 0.01K 1mK 100 μK 10 μK

wavelength

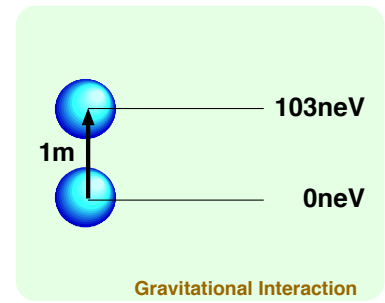
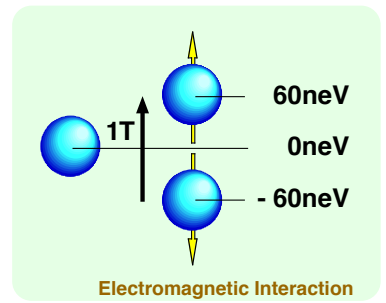
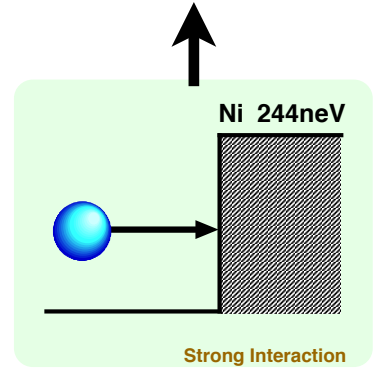
100fm 0.01nm 0.1nm 1nm 10nm 100nm 1 μm



Very cold neutrons

exhibit significant wave nature,
 can be flexibly controlled by optics,
 can go across material boundaries

neutron interferometry

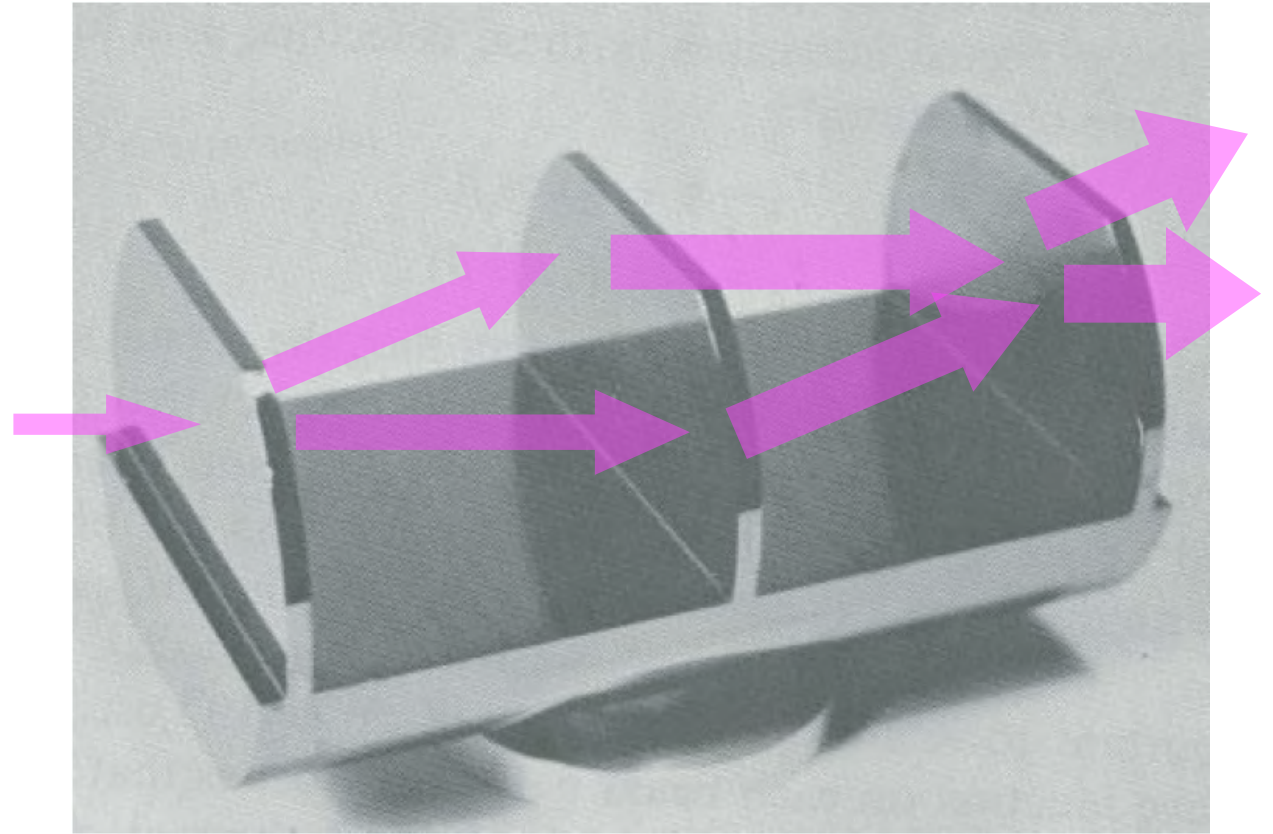
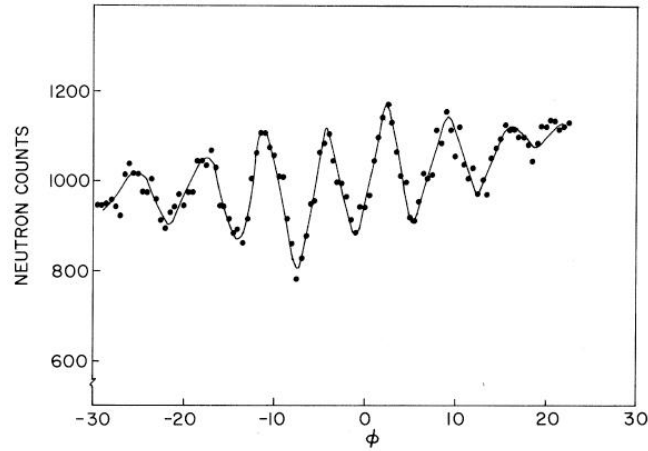
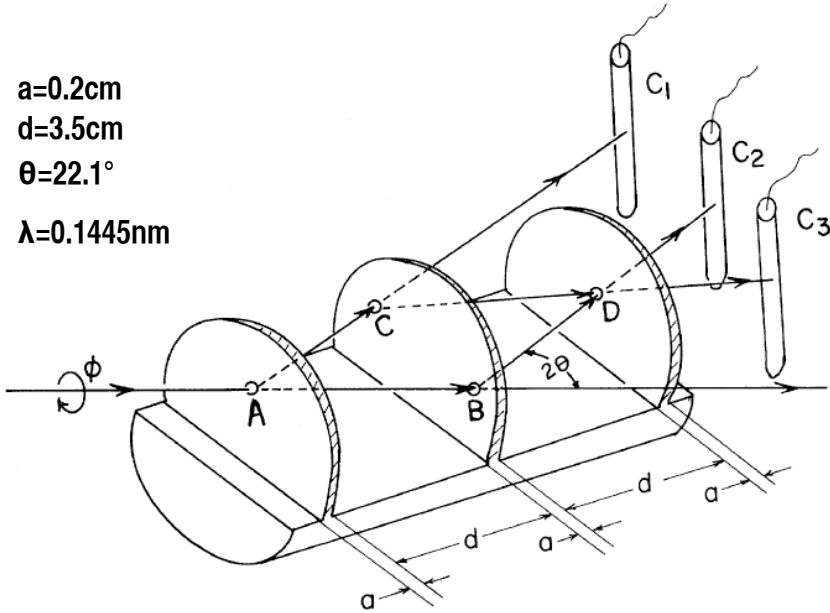


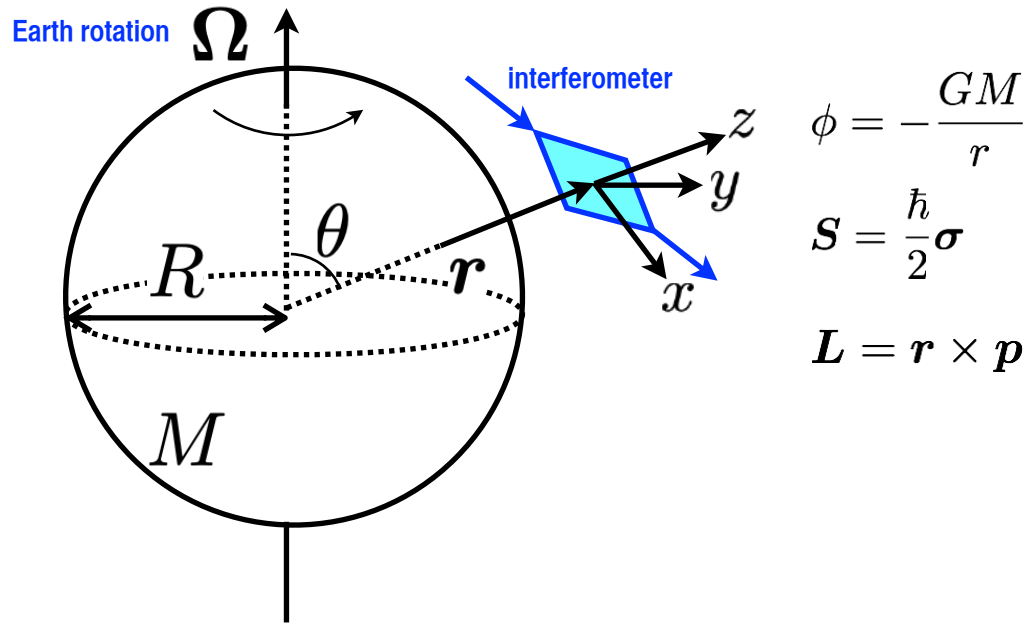
Neutron interferometer

Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

COW experiment (Neutron Phase induced by Earth's Gravity)

$a=0.2\text{cm}$
 $d=3.5\text{cm}$
 $\theta=22.1^\circ$
 $\lambda=0.1445\text{nm}$





$$\phi = -\frac{GM}{r}$$

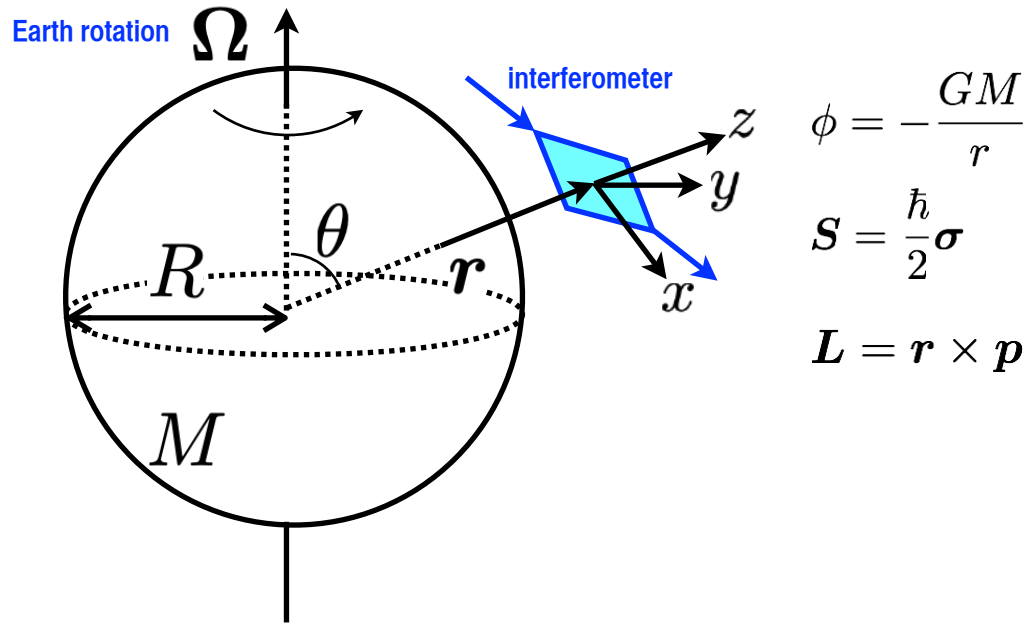
$$\mathbf{S} = \frac{\hbar}{2}\boldsymbol{\sigma}$$

$$\mathbf{L} = \mathbf{r} \times \mathbf{p}$$

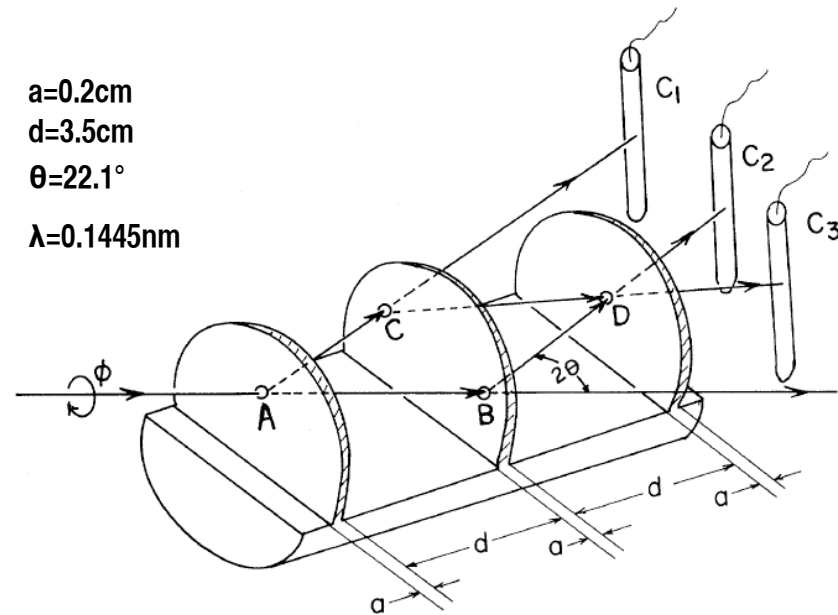
$$\mathcal{H} = \frac{\mathbf{p}^2}{2m} + m\phi - \boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S}) \quad \text{Newtonian terms}$$

$$+ \frac{1}{c^2} \left(-\frac{\mathbf{p}^4}{8m^3} + \frac{m}{2}\phi^2 + \frac{3}{2m}\mathbf{p} \cdot (\phi\mathbf{p}) + \frac{3GM}{2mr^3}\mathbf{L} \cdot \mathbf{S} + \frac{4GMR^2}{5r^3}\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S}) + \frac{6GMR^2}{5r^5}\mathbf{S} \cdot (\mathbf{r} \times (\mathbf{r} \times \boldsymbol{\Omega})) \right)$$

post-Newtonian terms



Collela, Overhauser, Werner, Phys. Rev. Lett. 34 (1975) 1472

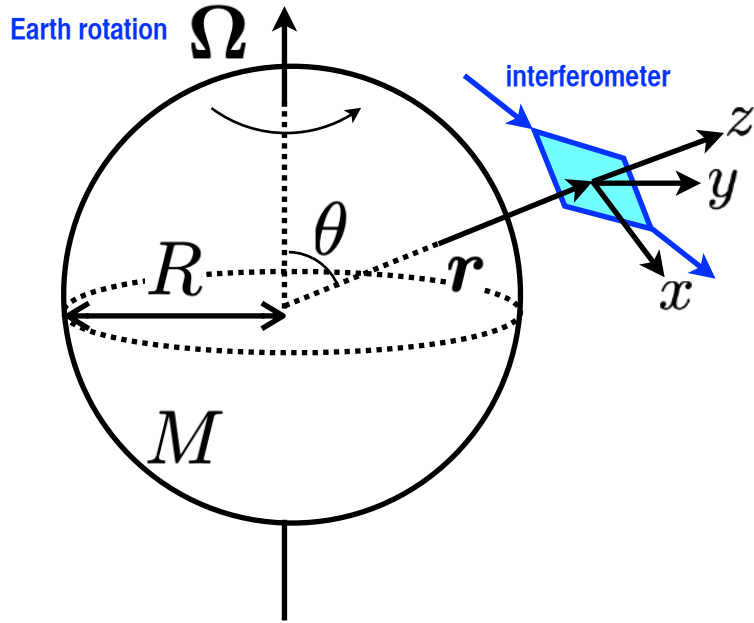


$$\mathcal{H} = \frac{p^2}{2m} + \boxed{m\phi} - \Omega \cdot (L + S) \quad \text{Newtonian terms}$$

$$+ \frac{1}{c^2} \left(-\frac{p^4}{8m^3} + \frac{m}{2}\phi^2 + \frac{3}{2m}p \cdot (\phi p) + \frac{3GM}{2mr^3}L \cdot S + \frac{4GMR^2}{5r^3}\Omega \cdot (L + S) + \frac{6GMR^2}{5r^5}S \cdot (r \times (r \times \Omega)) \right)$$

post-Newtonian terms

S. A. Werner, et. al., Phys. Rev. Lett. 42 (1979) 1103.



$$\phi = -\frac{GM}{r}$$

$$S = \frac{\hbar}{2}\sigma$$

$$L = r \times p$$

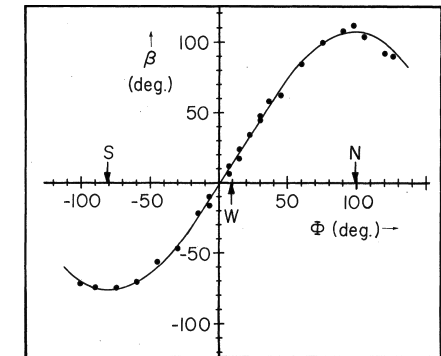
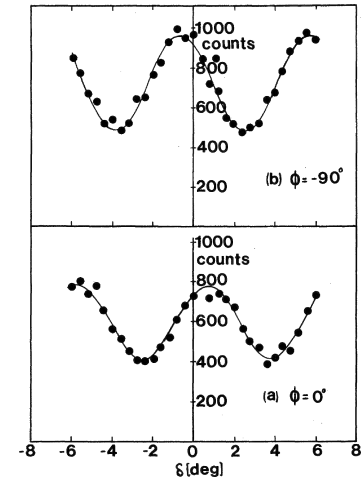
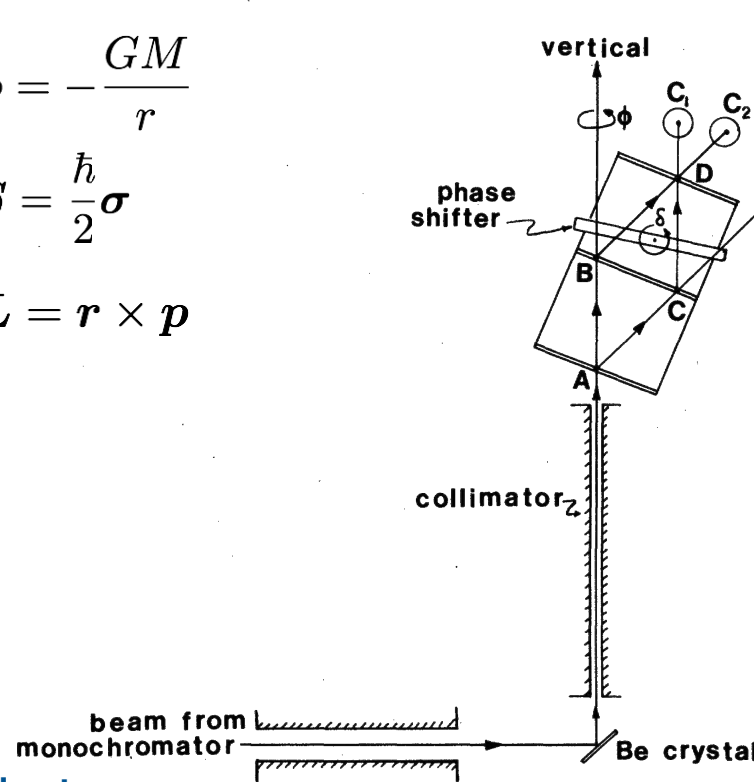
$$\mathcal{H} = \frac{p^2}{2m} + \boxed{m\phi} - \boxed{\Omega \cdot (L + S)}$$

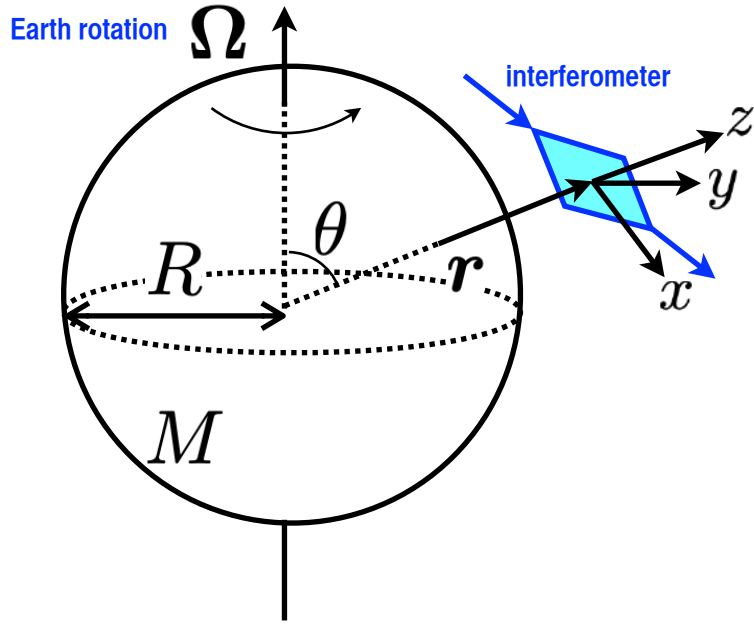
COW Sagnac effect

Newtonian terms

$$+ \frac{1}{c^2} \left(-\frac{p^4}{8m^3} + \frac{m}{2}\phi^2 + \frac{3}{2m}p \cdot (\phi p) + \frac{3GM}{2mr^3}L \cdot S + \frac{4GMR^2}{5r^3}\Omega \cdot (L + S) + \frac{6GMR^2}{5r^5}S \cdot (r \times (r \times \Omega)) \right)$$

post-Newtonian terms





$$\phi = -\frac{GM}{r}$$

$$\mathbf{S} = \frac{\hbar}{2}\boldsymbol{\sigma}$$

$$\mathbf{L} = \mathbf{r} \times \mathbf{p}$$

	$m\phi$	$\frac{4GMR^2\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})/5r^3c^2}{10^{-10}}$
$\lambda \sim 0.1\text{nm}, A \sim 1\text{cm} \times 1\text{cm}$	5	10^{-10}
$\lambda \sim 1.0\text{nm}, A \sim 1\text{m} \times 1\text{m}$	10^5	10^{-6}

accessible with J-PARC

$$\mathcal{H} = \frac{\mathbf{p}^2}{2m} + \boxed{m\phi} - \boxed{\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})} \quad \text{Newtonian terms}$$

$$+ \frac{1}{c^2} \left(-\frac{\mathbf{p}^4}{8m^3} + \frac{m}{2}\phi^2 + \frac{3}{2m}\mathbf{p} \cdot (\phi\mathbf{p}) + \frac{3GM}{2mr^3}\mathbf{L} \cdot \mathbf{S} + \boxed{\frac{4GMR^2}{5r^3}\boldsymbol{\Omega} \cdot (\mathbf{L} + \mathbf{S})} + \frac{6GMR^2}{5r^5}\mathbf{S} \cdot (\mathbf{r} \times (\mathbf{r} \times \boldsymbol{\Omega})) \right)$$

post-Newtonian terms

Lense-Thirring

Multilayer Neutron Interferometer

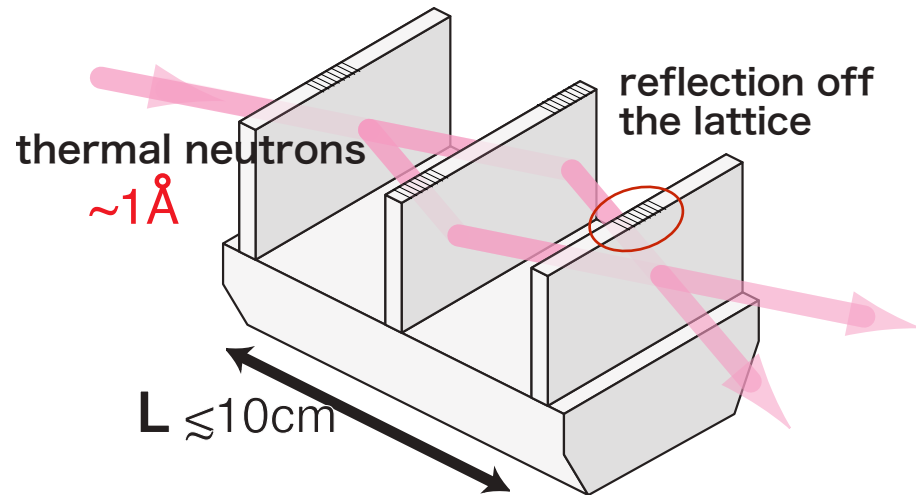
phase change

$$\Delta\varphi = 2\pi \frac{m_n L}{h^2} \lambda_n \Delta E$$

path length

energy difference between two paths

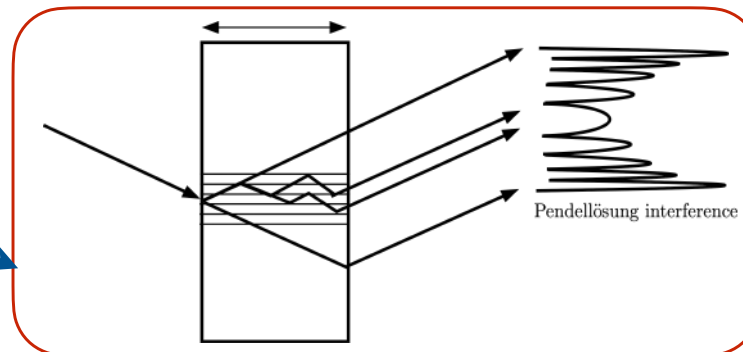
neutron wavelength



λ : limited by the lattice constant

L : limited by the size of available crystal

dynamical diffraction in the diffraction blades



Multilayer Neutron Interferometer

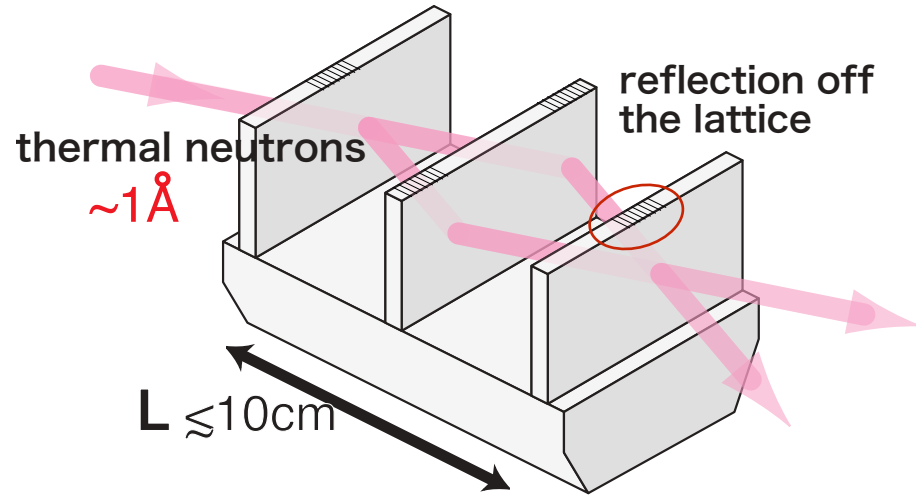
phase change

$$\Delta\varphi = 2\pi \frac{m_n L}{h^2} \lambda_n \Delta E$$

path length

energy difference between two paths

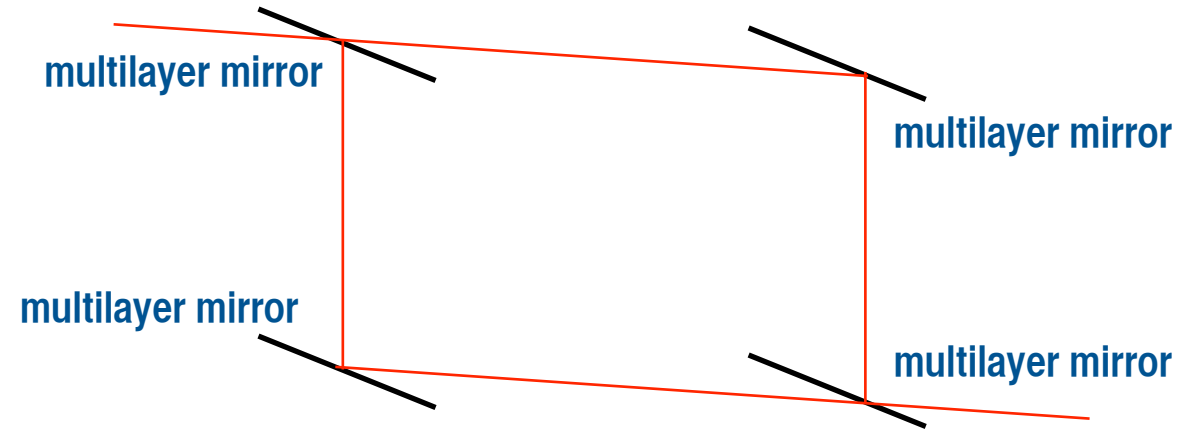
neutron wavelength



λ : limited by the lattice constant

L : limited by the size of available crystal

dynamical diffraction in the diffraction blades

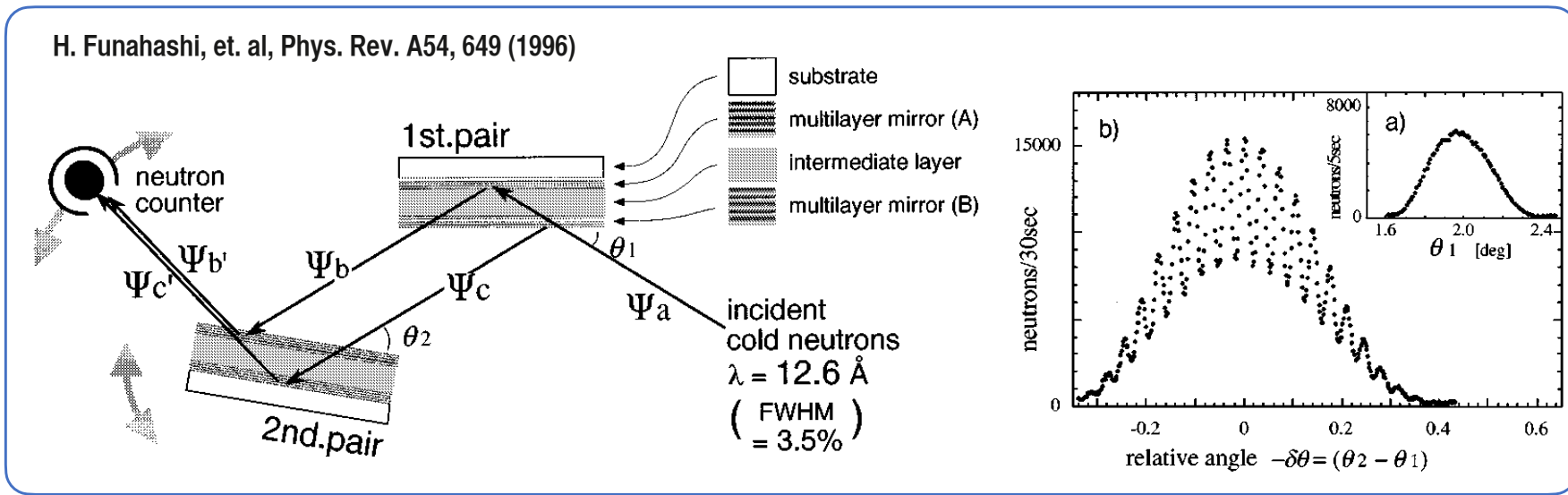
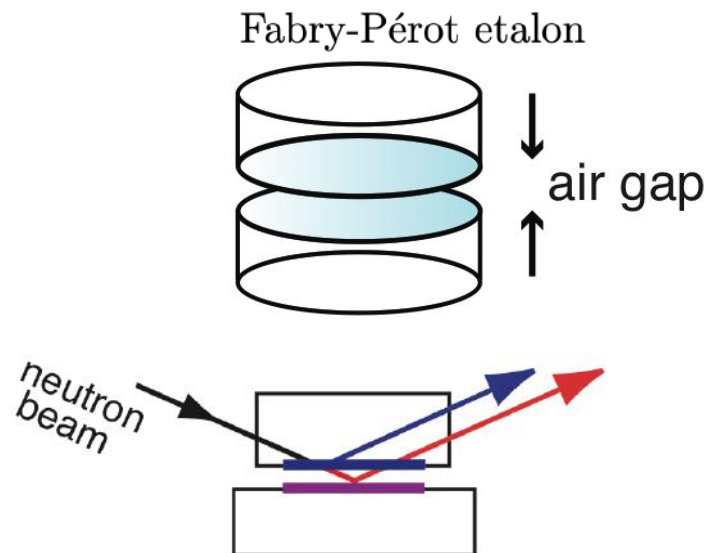


λ : not limited by the lattice constant

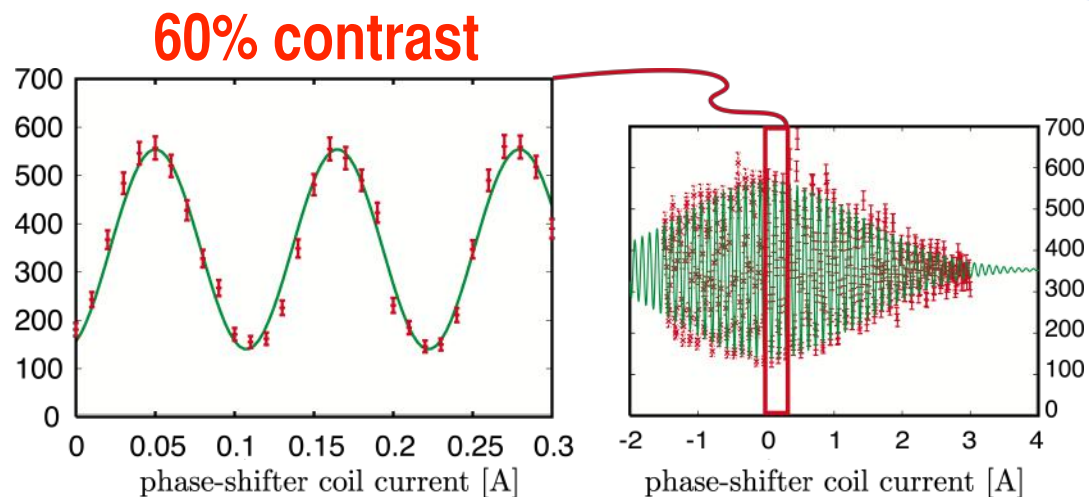
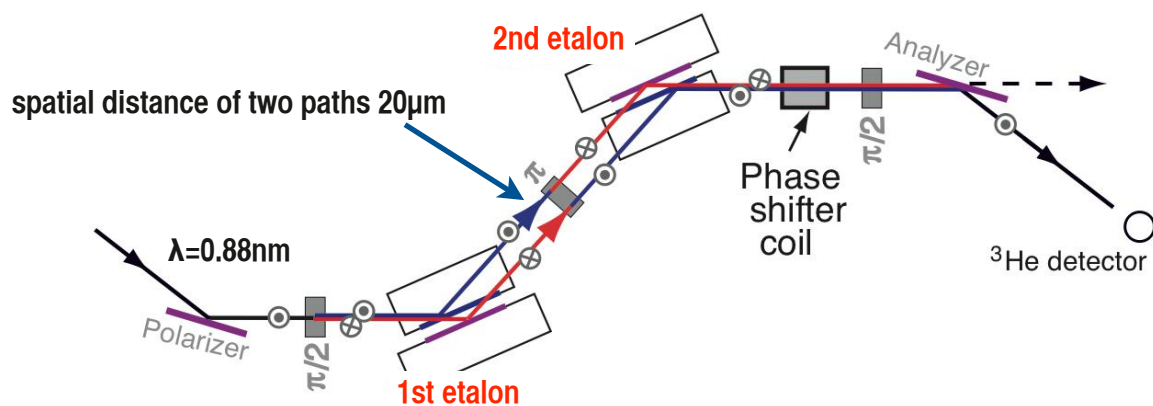
L : not limited by the size of available crystal but mirror alignment

suppressed dynamical diffraction

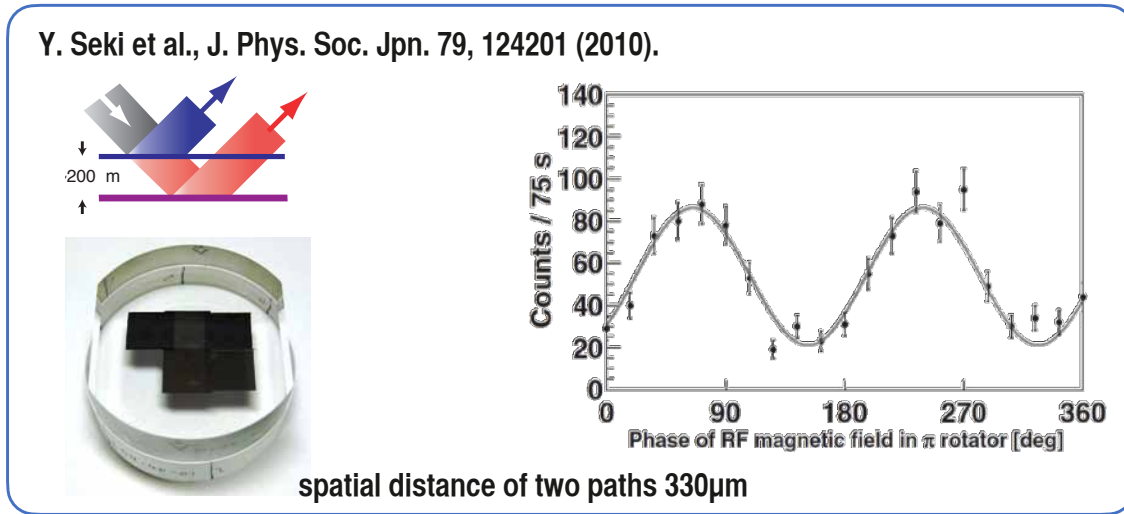
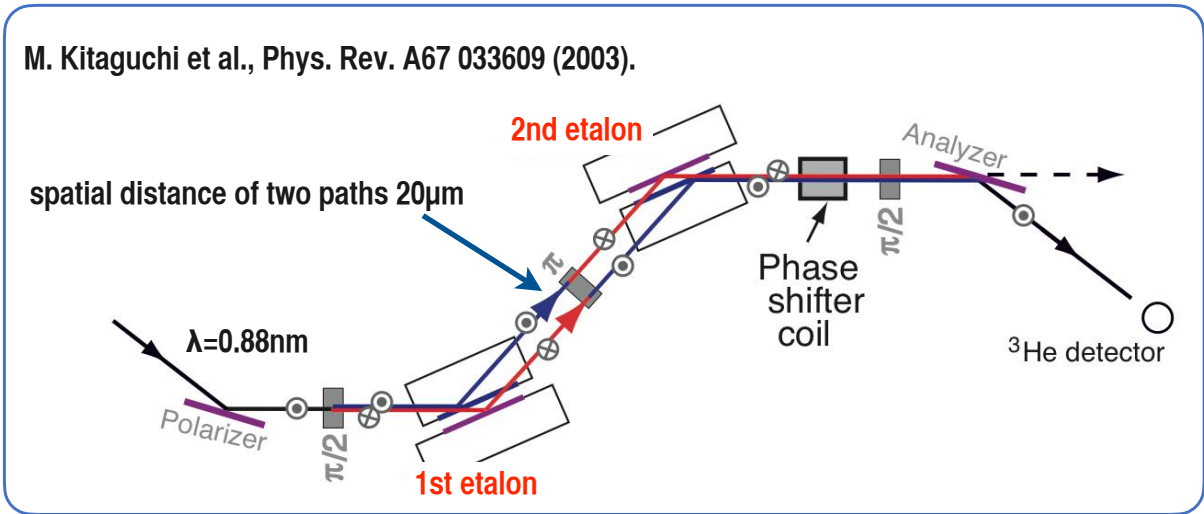
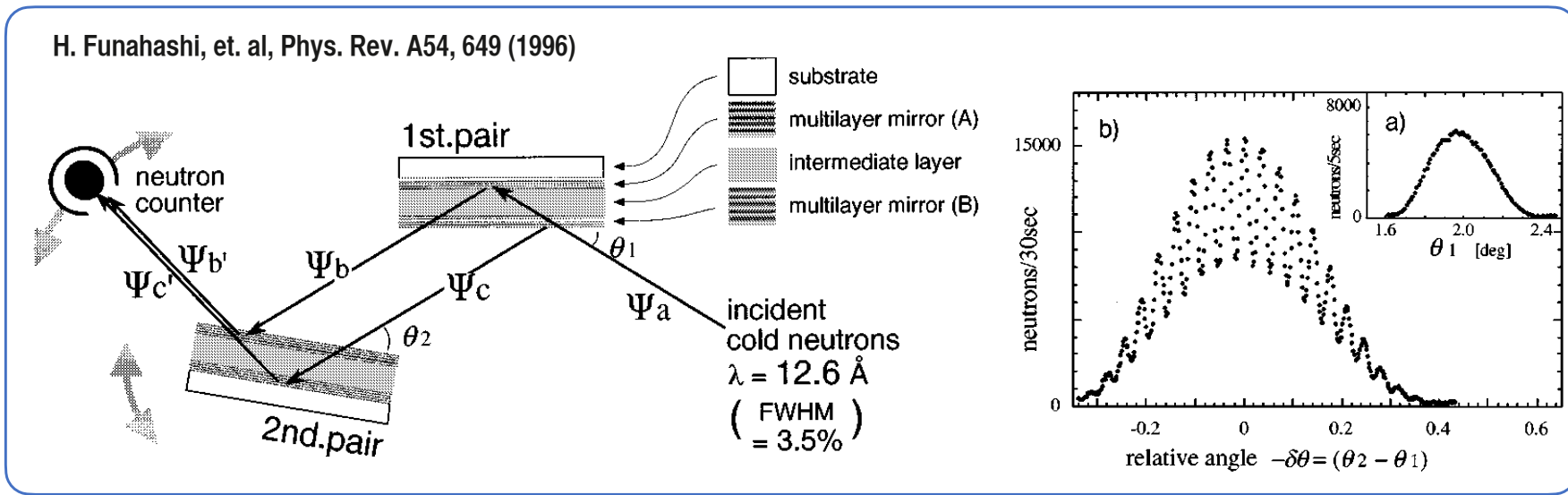
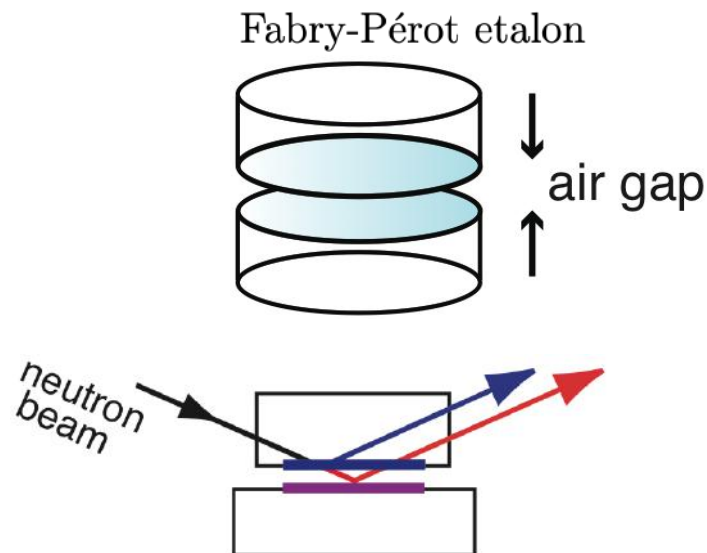
Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)



M. Kitaguchi et al., Phys. Rev. A67 033609 (2003).



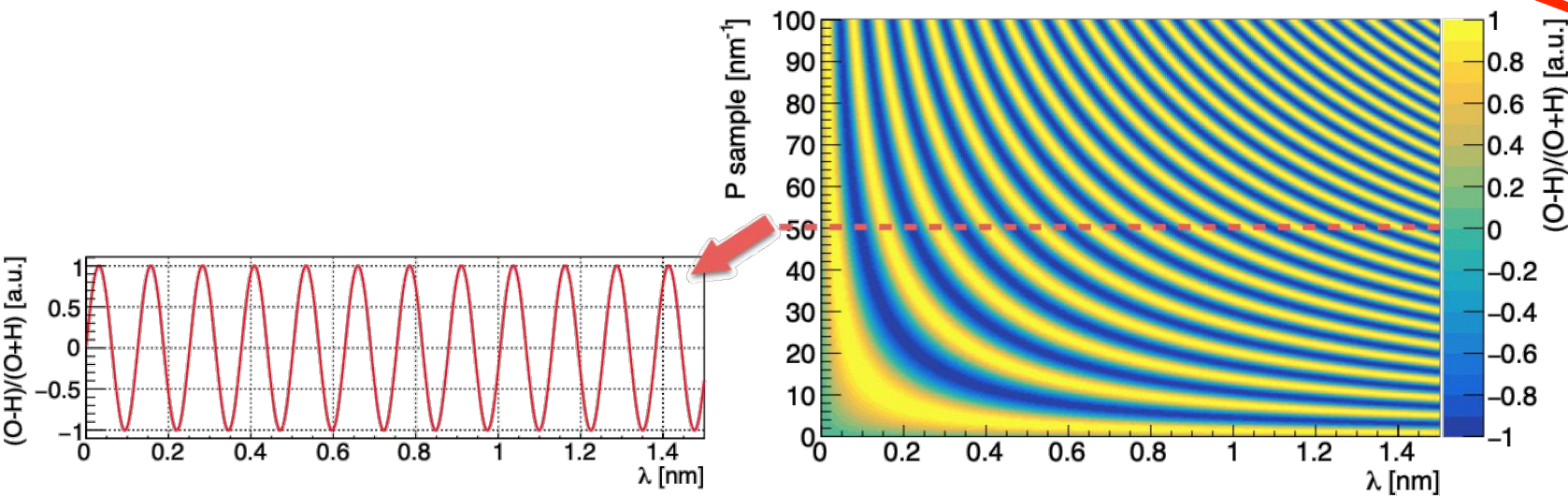
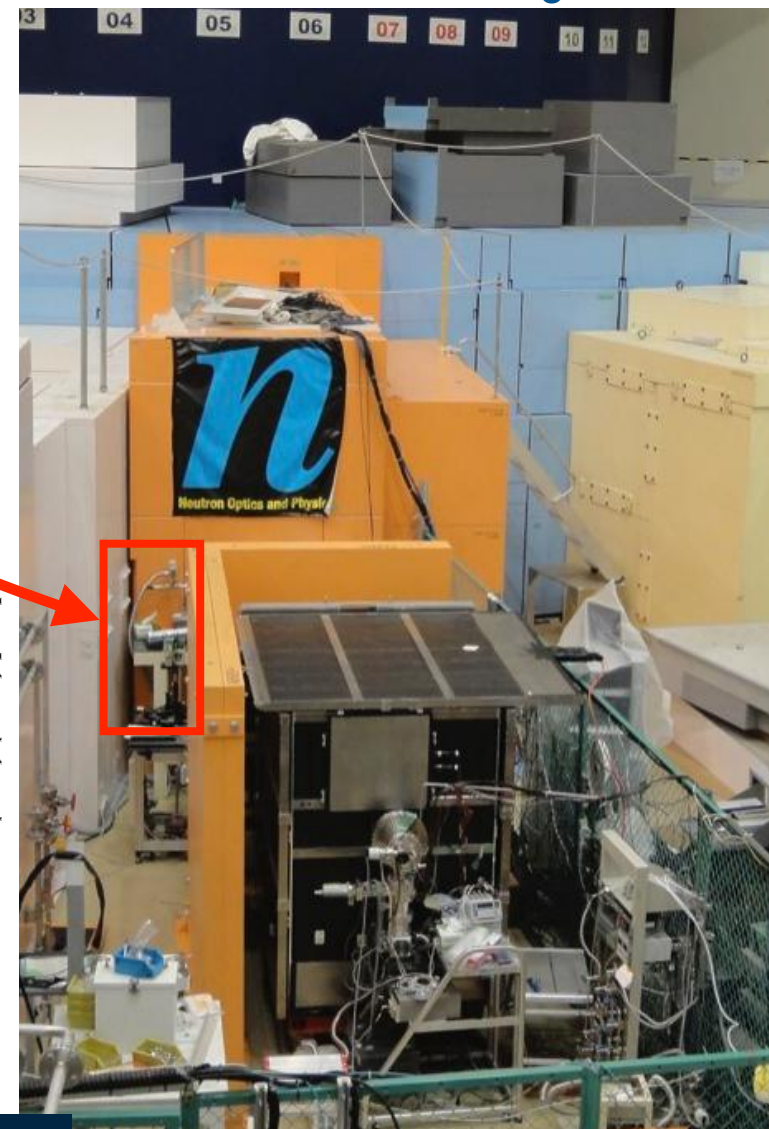
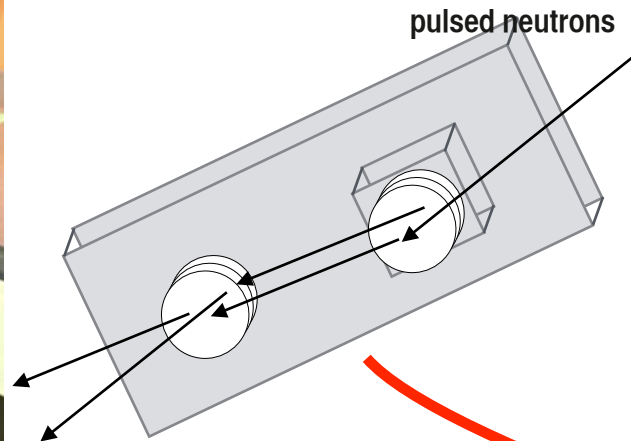
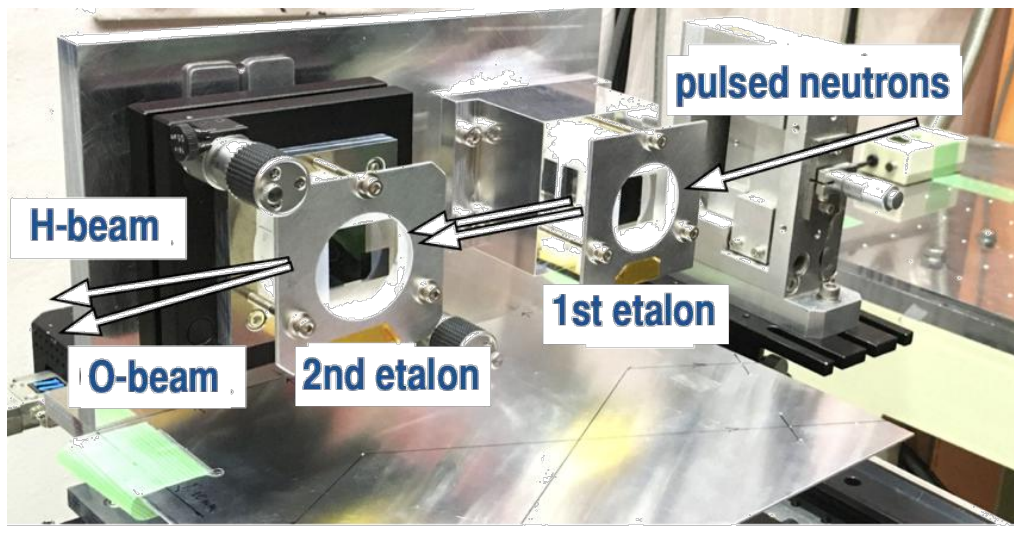
Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)



Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)

T.Fujiie, M.Hino, T.Hosobata, G.Ichikawa, M.Kitaguchi, K.Mishima, Y.Seki, H.M.Shimizu, Y.Yamagata

J-PARC MLF BL05 Low Divergence Branch



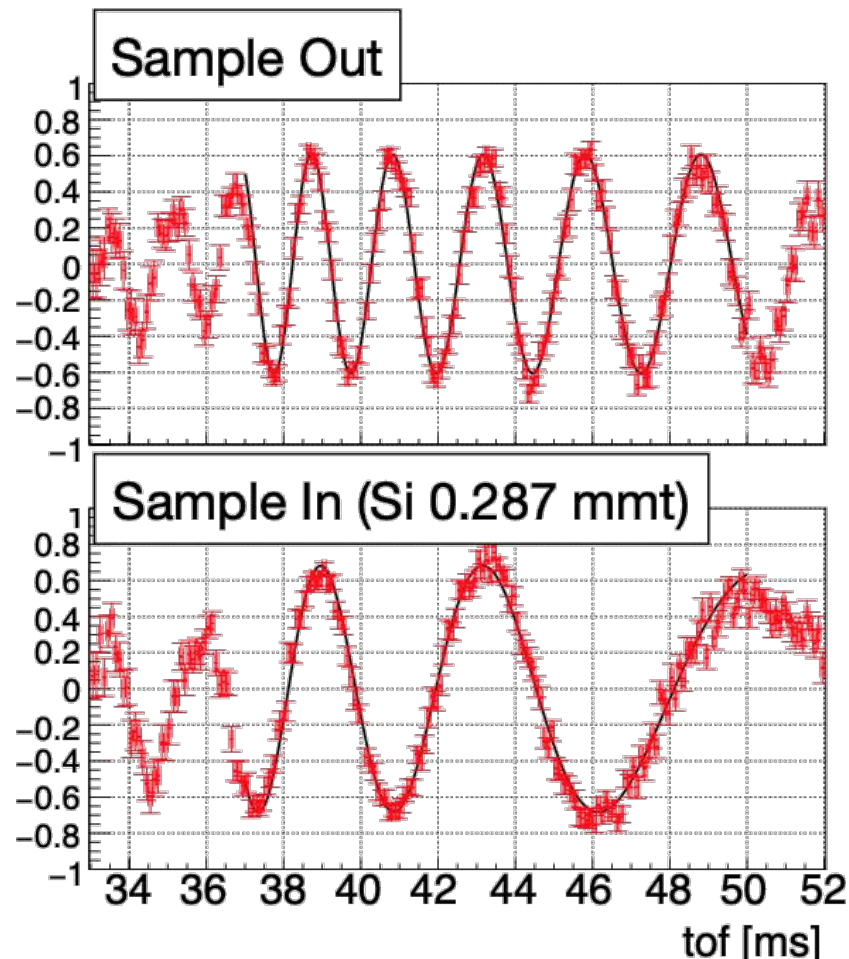
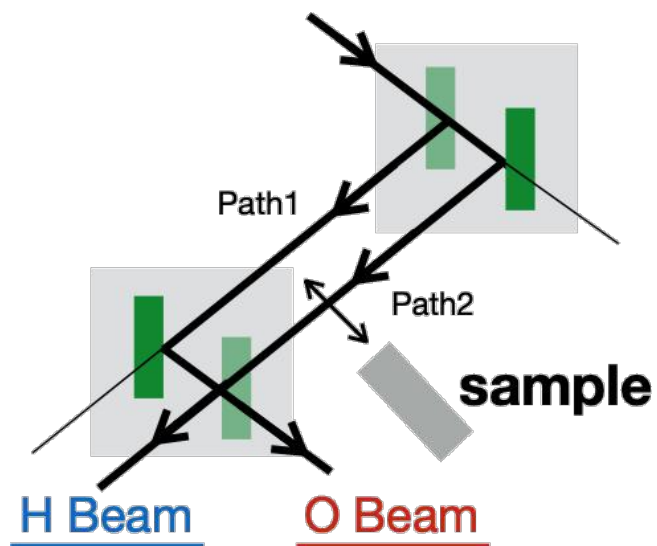
The phase sensitivity is stabilized by extracting phase shift in the 2-dim. interference pattern.

Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)

T.Fujiie, M.Hino, T.Hosobata, G.Ichikawa, M.Kitaguchi, K.Mishima, Y.Seki, H.M.Shimizu, Y.Yamagata

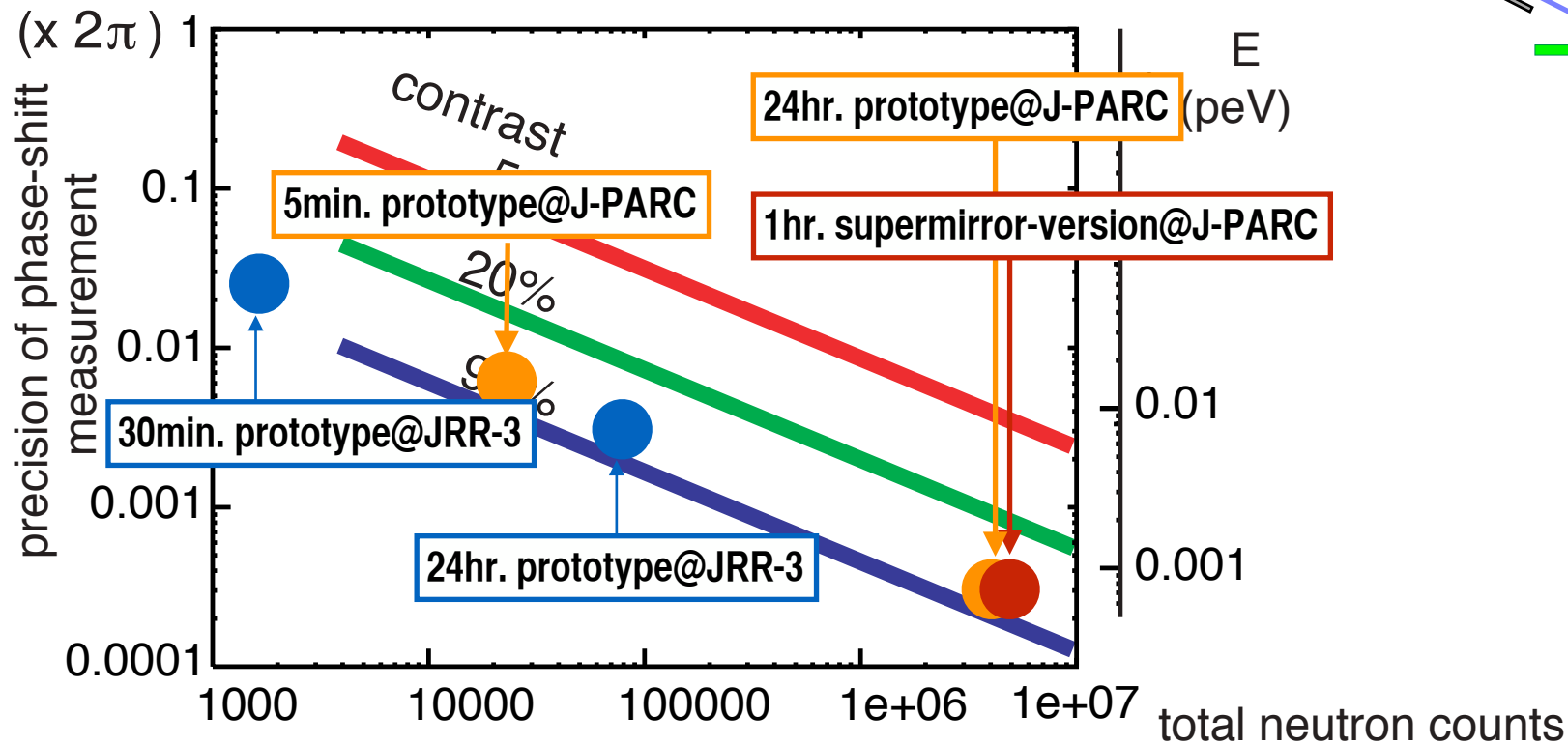
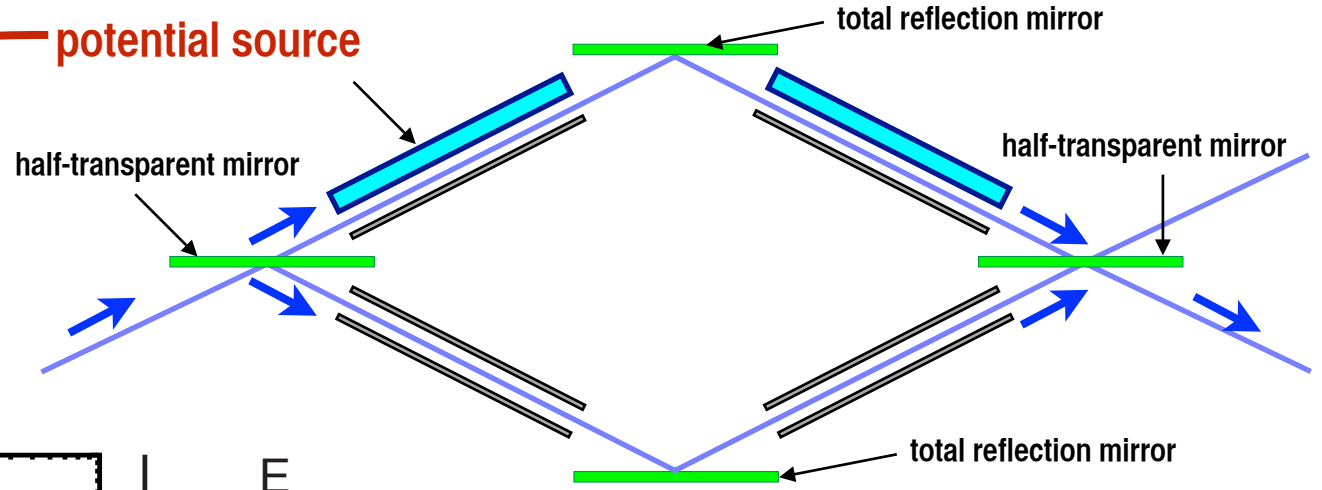
J-PARC MLF BL05 Low Divergence Branch

being applied for the measurement of neutron scattering length



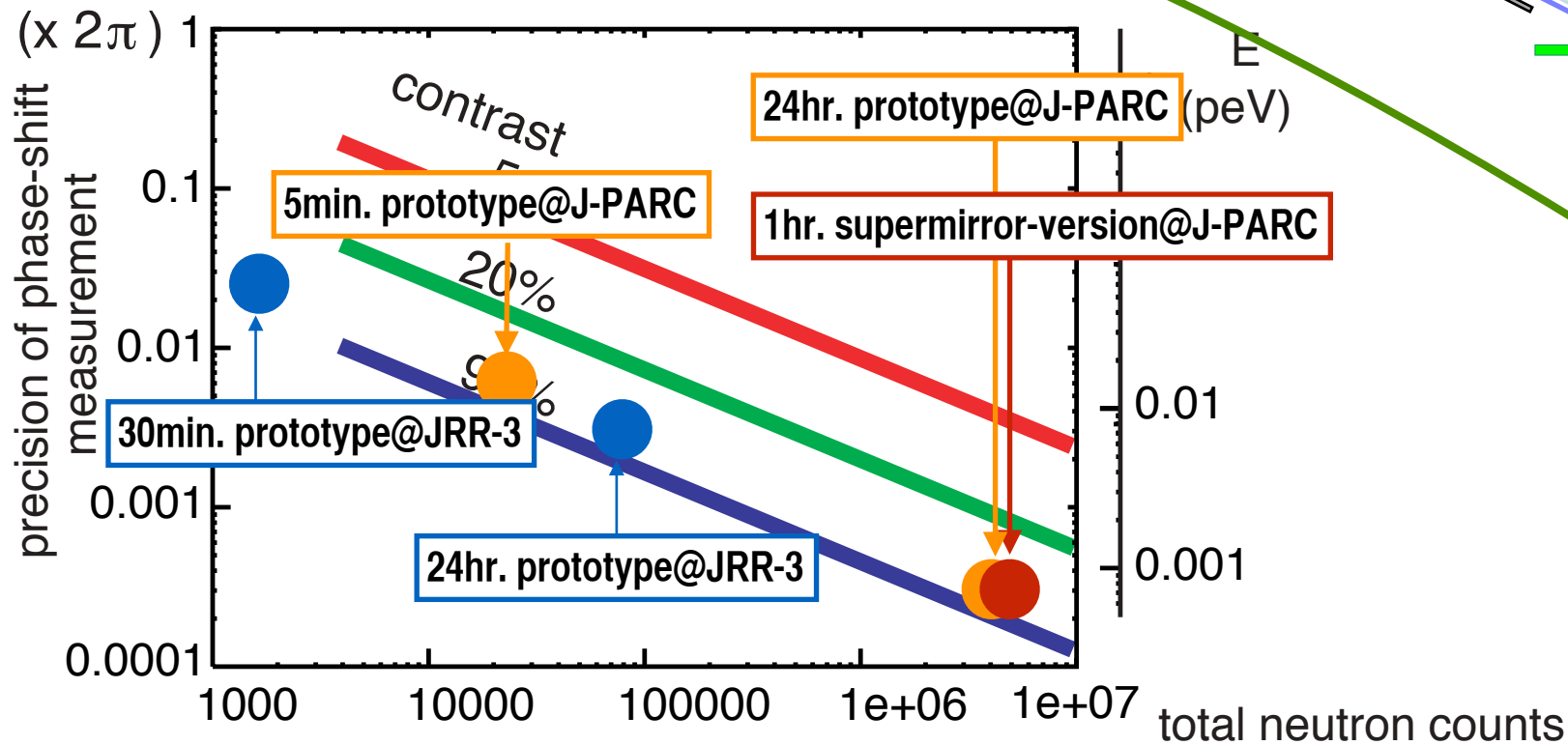
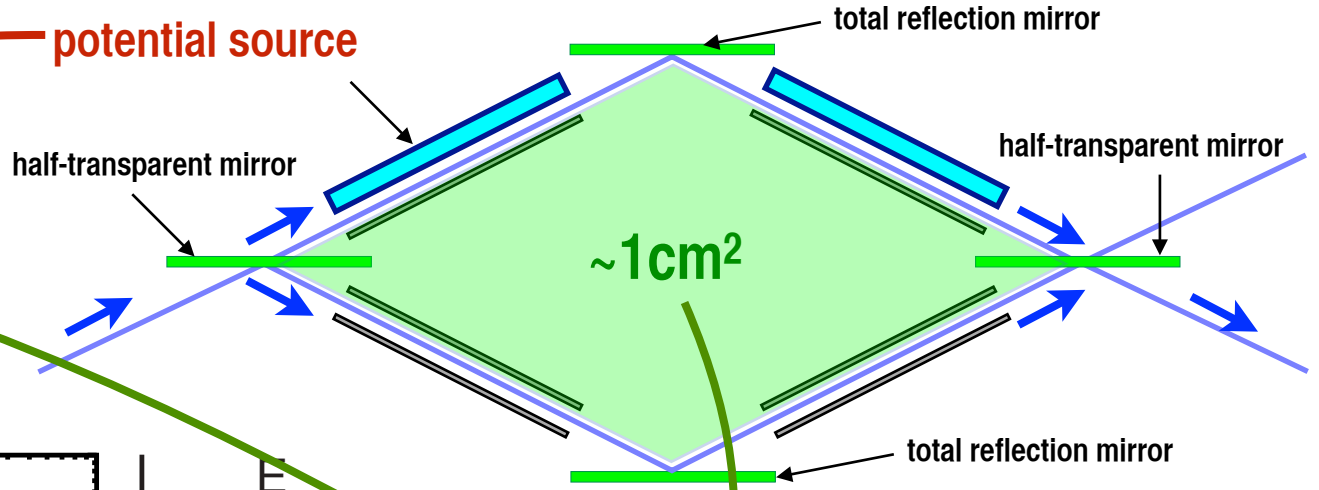
Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)

scattering length
 anomalous short-range gravity
 dark energy (via chameleon mechanism) K. Li, et. al., Phys. Rev. D 93, 062001 (2016)
 post-Newtonian effects (laboratory test of general relativity)
 ...



Multilayer Neutron Interferometer with etalon configuration (BSE: Beam-Splitting Etalon)

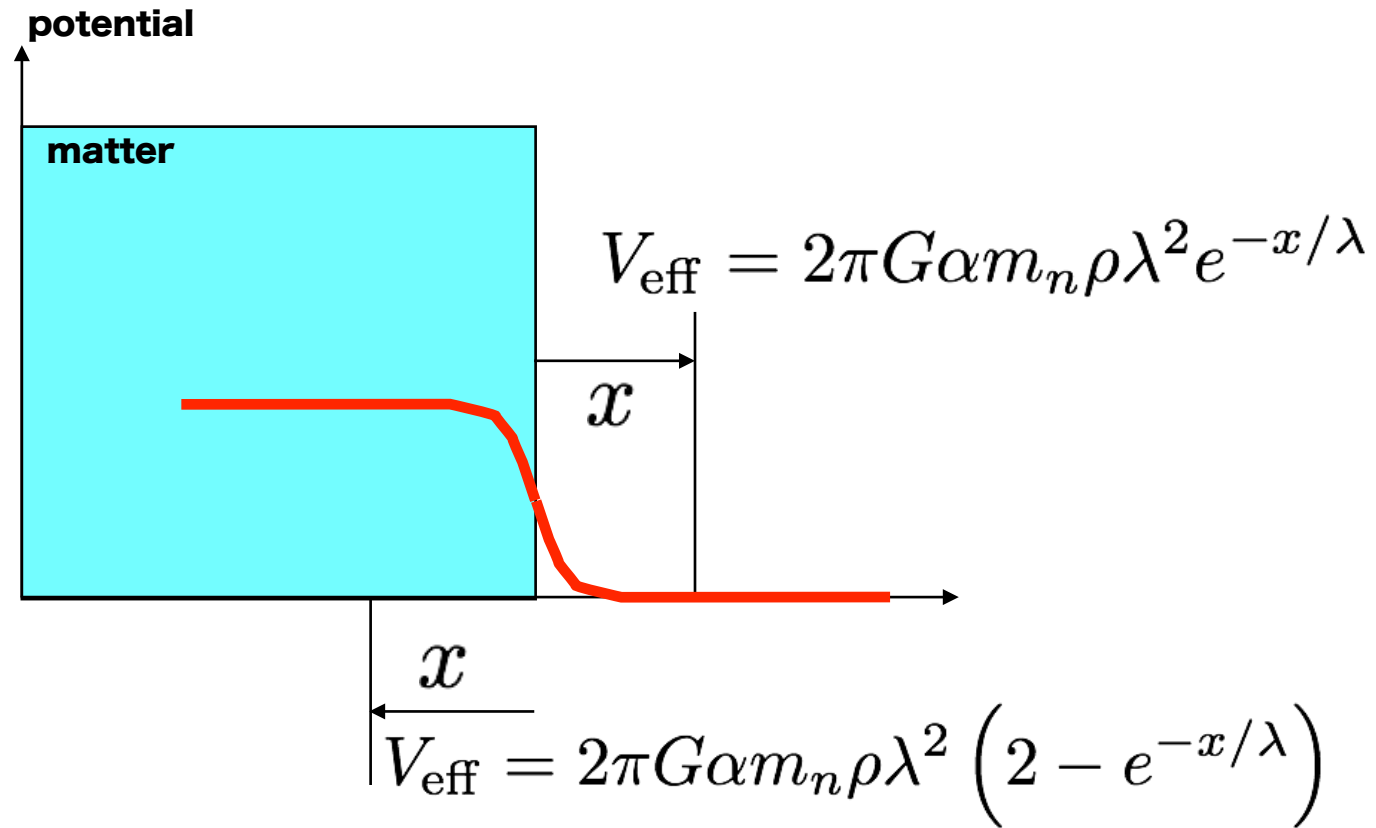
scattering length
 anomalous short-range gravity
 dark energy (via chameleon mechanism) K. Li, et. al., Phys. Rev. D 93, 062001 (2016)
 post-Newtonian effects (laboratory test of general relativity)
 ...



Parametric Resonance

Anomalous Gravity in the vicinity of Material Surface

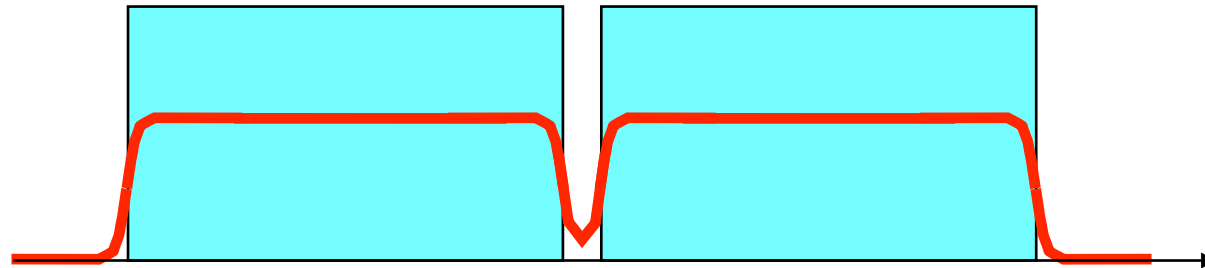
$$V_G(r) = -\frac{GM}{r} \alpha e^{-r/\lambda}$$



Anomalous Gravity in the vicinity of Material Surface

$$V_G(r) = -\frac{GM}{r} \alpha e^{-r/\lambda}$$

$$V_{\text{eff}} = k_0^2 + 2\alpha^2 e^{-L/2\lambda} \cosh\left(\frac{x}{\lambda}\right)$$



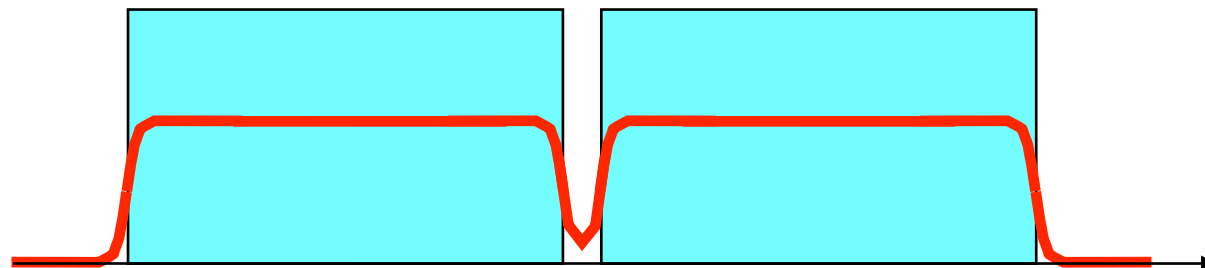
$$V_{\text{eff}} = k_0^2 + 2\alpha^2 e^{-L/2\lambda} \cosh\left(\frac{x}{\lambda}\right)$$

$$\cosh\left(\frac{x}{\lambda}\right) = \frac{\sinh(L/\lambda)}{L/\lambda} + \sum_{n=1}^{\infty} \left[\frac{2(-1)^n (L/\lambda) \sinh(L/\lambda)}{(L/\lambda)^2 + n^2\pi^2} \cos\left(\frac{n\pi x}{L}\right) \right]$$

parametric resonance

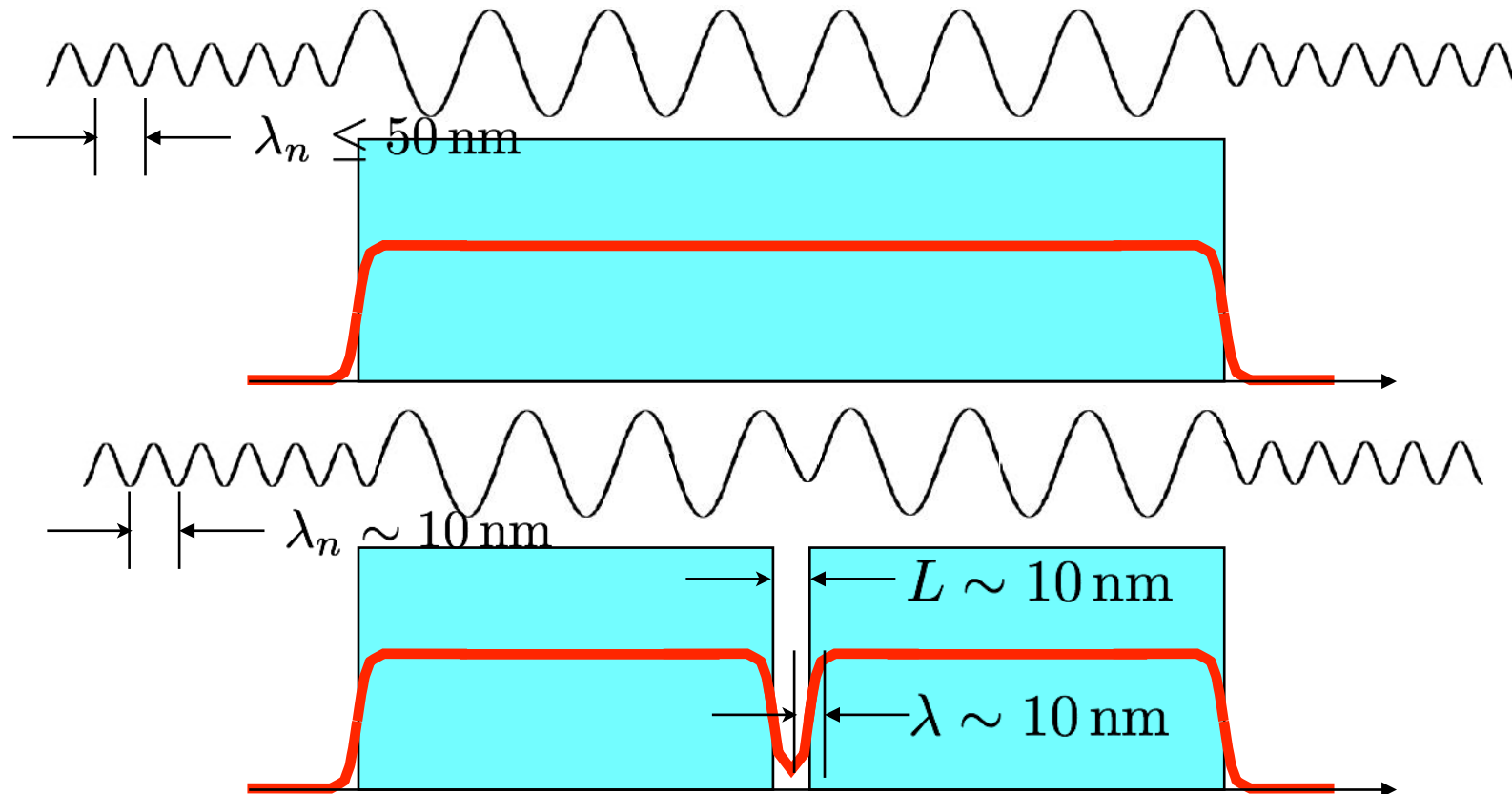
$$\frac{2k_0}{1 + \frac{2\alpha^2}{k_0^2} \exp(-L/\lambda) \frac{\sinh(L/\lambda)}{L/\lambda}} = \frac{n\pi}{L} \quad \lambda_n \simeq \frac{4L}{n} \quad (\eta \rightarrow 0)$$

$$\gamma \simeq \frac{\alpha^2 \lambda_n^2}{\pi^2} \frac{(L/\lambda) \sinh(L/\lambda)}{(L/\lambda)^2 + 16\pi^2 (L/\lambda)^2} e^{-L/(2\lambda)}$$



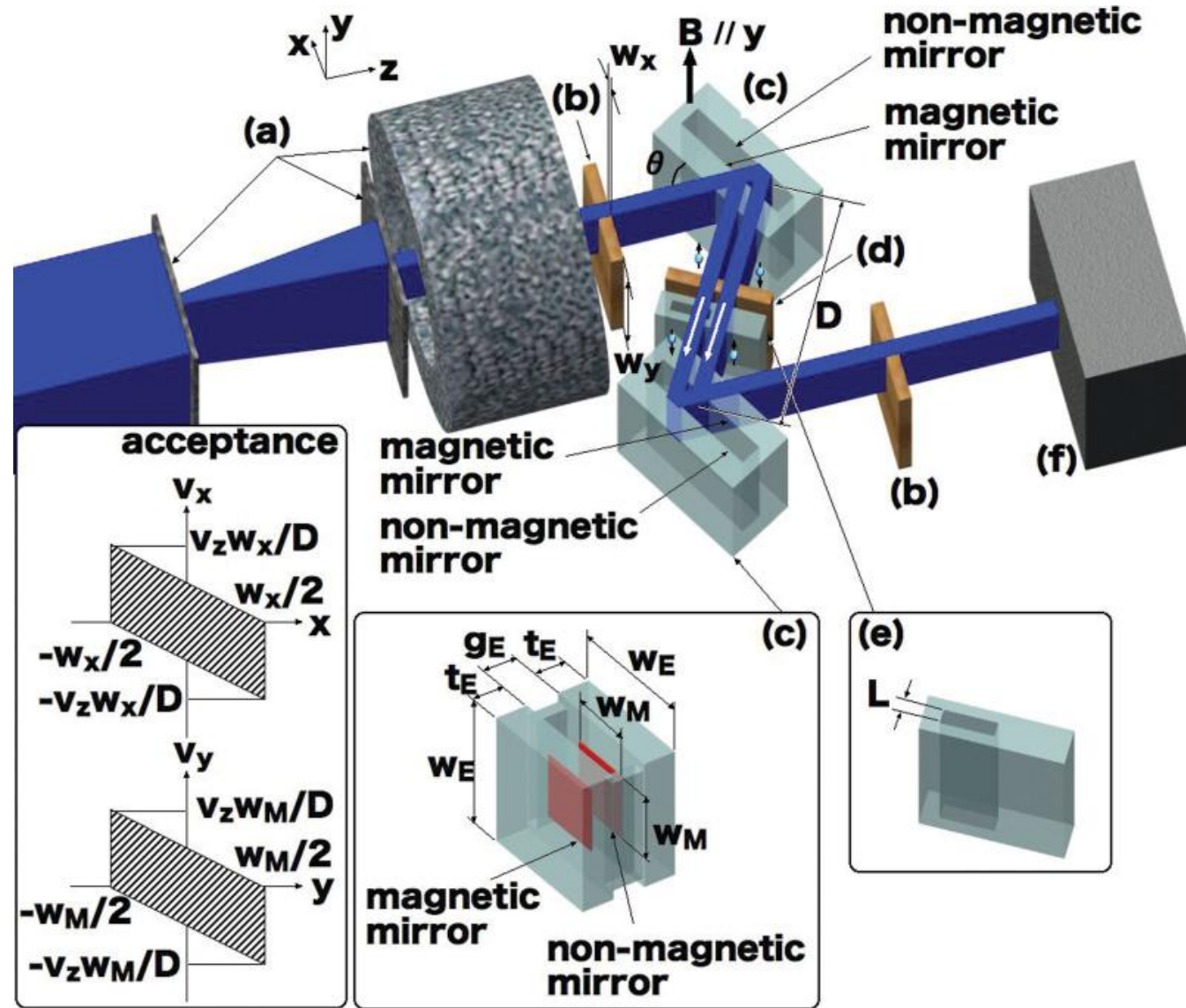
Parametric Resonance in 1-dim Potential

$$V_G(r) = -\frac{GM}{r} \alpha e^{-r/\lambda}$$

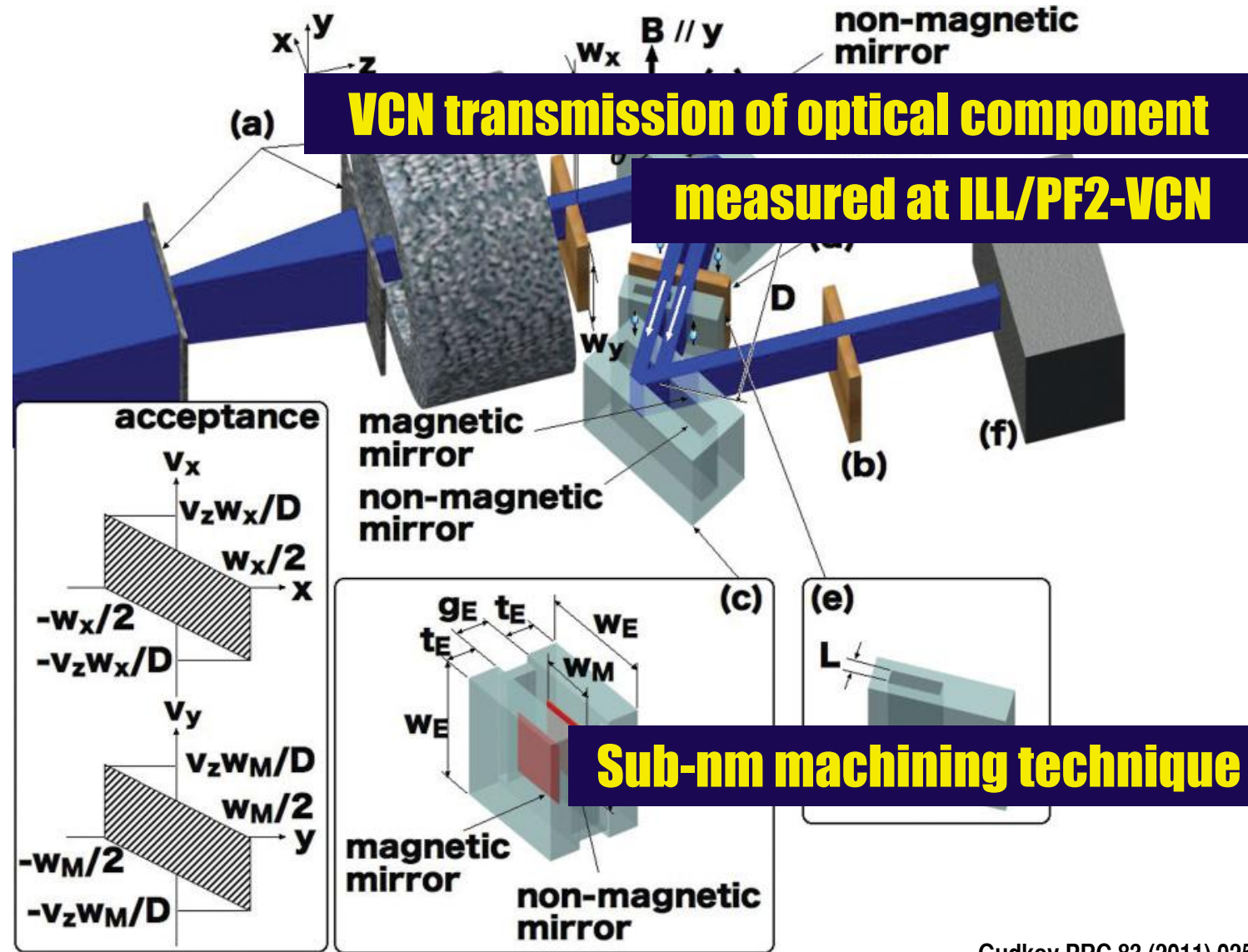


Gudkov, Shimizu, Greene, PRC 83 (2011) 025501

Experimental Apparatus of the Search for Parametric Resonance



Experimental Apparatus of the Search for Parametric Resonance



Gudkov PRC 83 (2011) 025501

Neutron Velocity Concentrator

M.Kitaguchi, Prog. Theor. Exp. Phys. (2017) 043D01

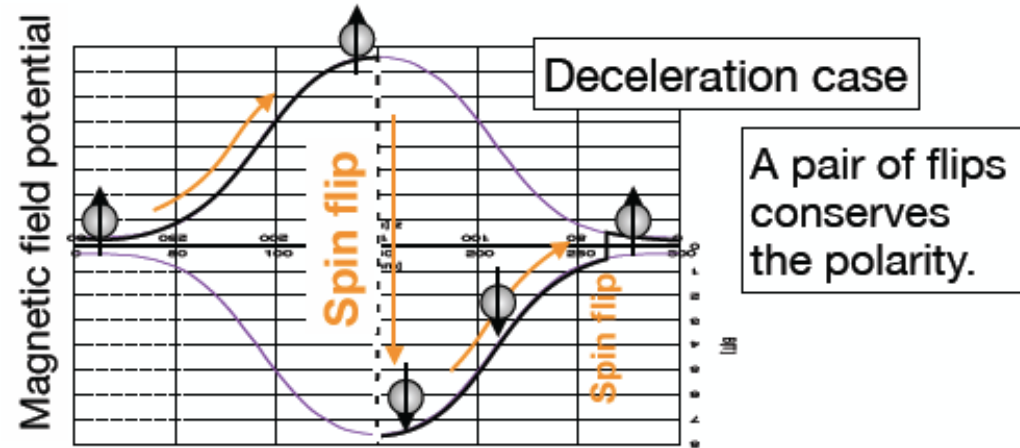
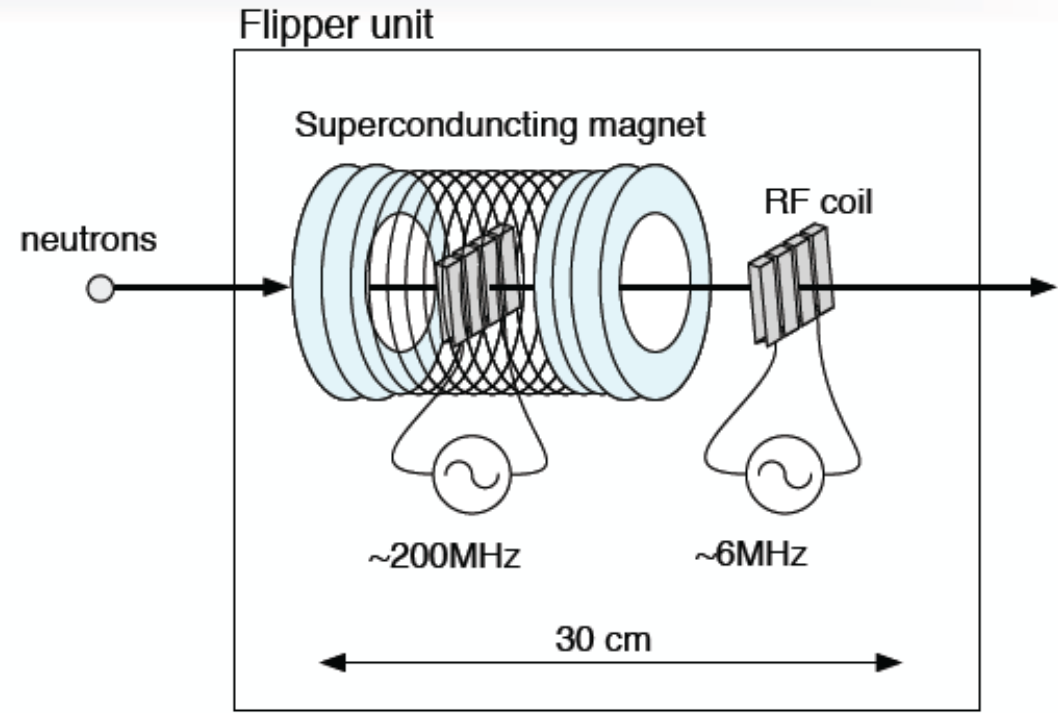
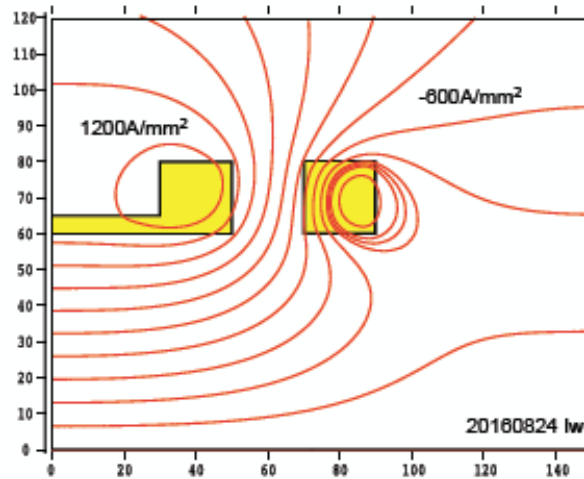
Deceleration and acceleration by spin flip

RF spin flipper

RF spin flipper (RSF) can decelerate and / or accelerate the neutrons.

RSF in 7.5 T magnetic field changes the energy of $0.9 \mu\text{eV}$.

Calculation of magnetic field



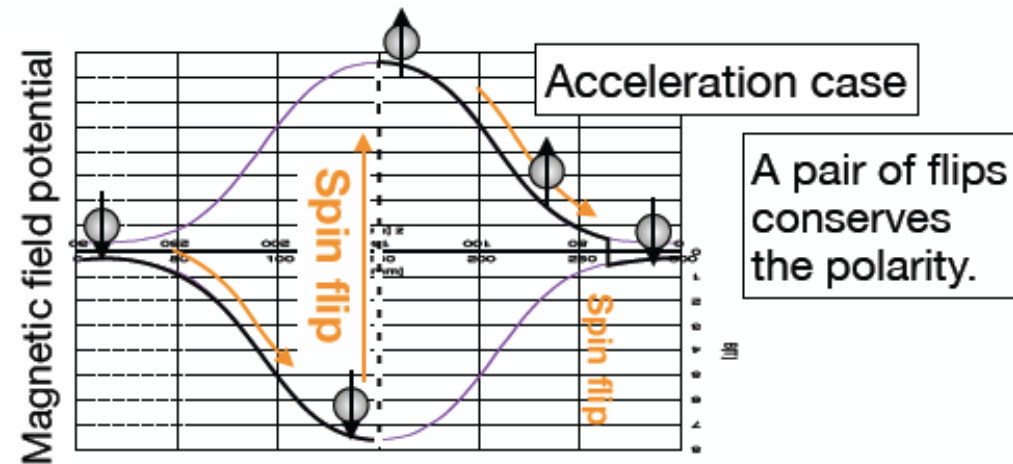
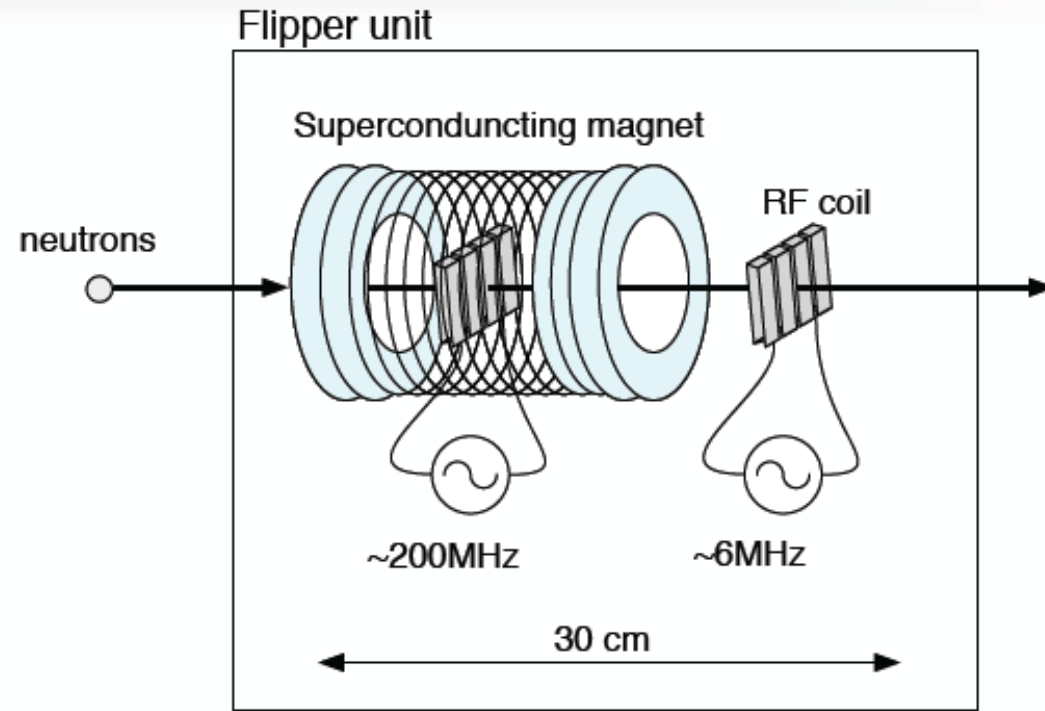
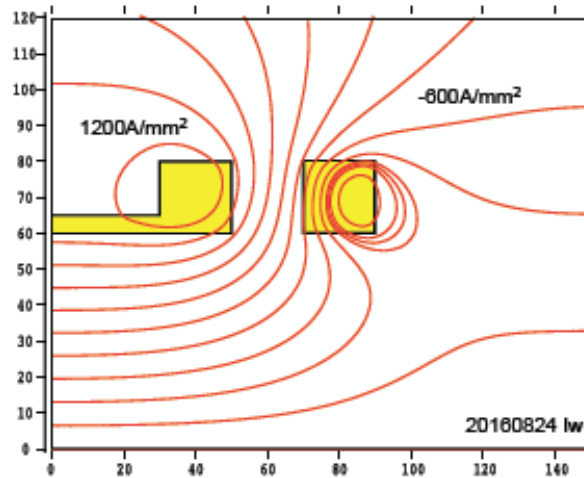
Deceleration and acceleration by spin flip

RF spin flipper

RF spin flipper (RSF) can decelerate and / or accelerate the neutrons.

RSF in 7.5 T magnetic field changes the energy of $0.9 \mu\text{eV}$.

Calculation of magnetic field

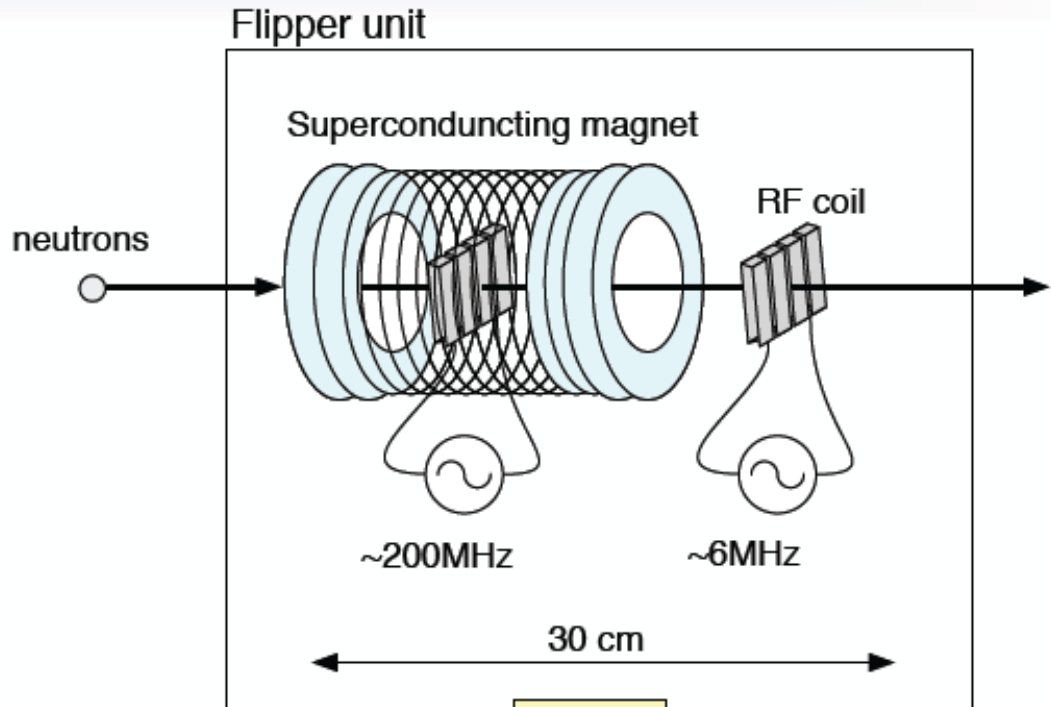


Deceleration and acceleration by spin flip

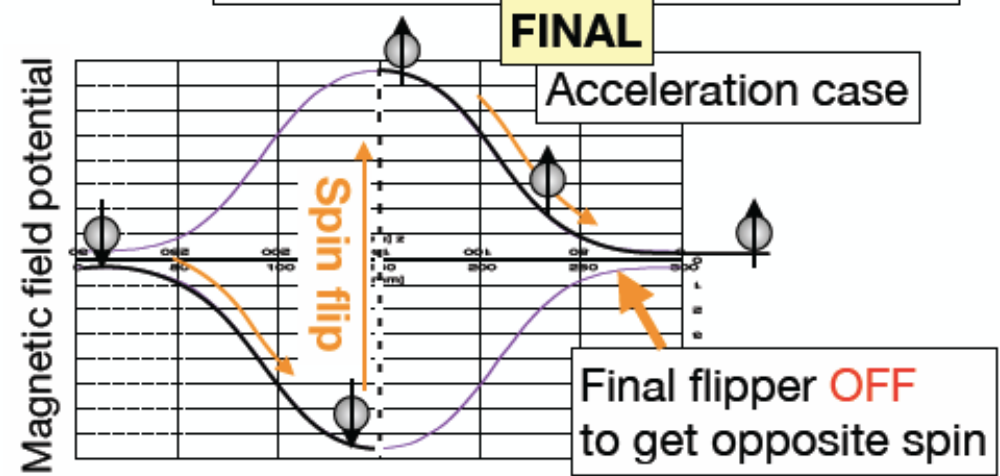
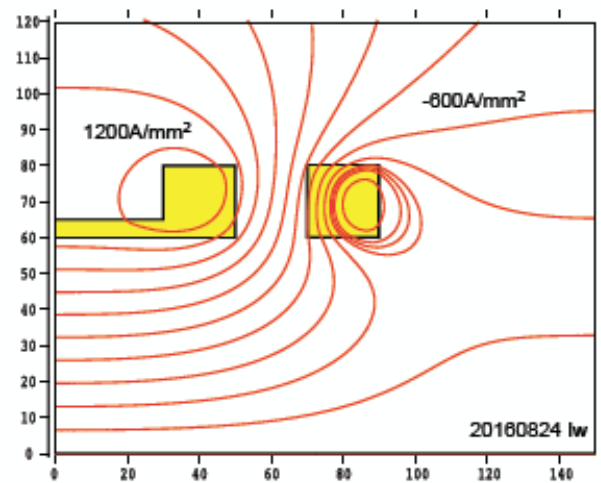
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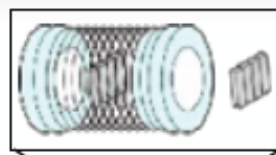


Calculation of magnetic field



Neutron Velocity Concentrator

Series of flipper units

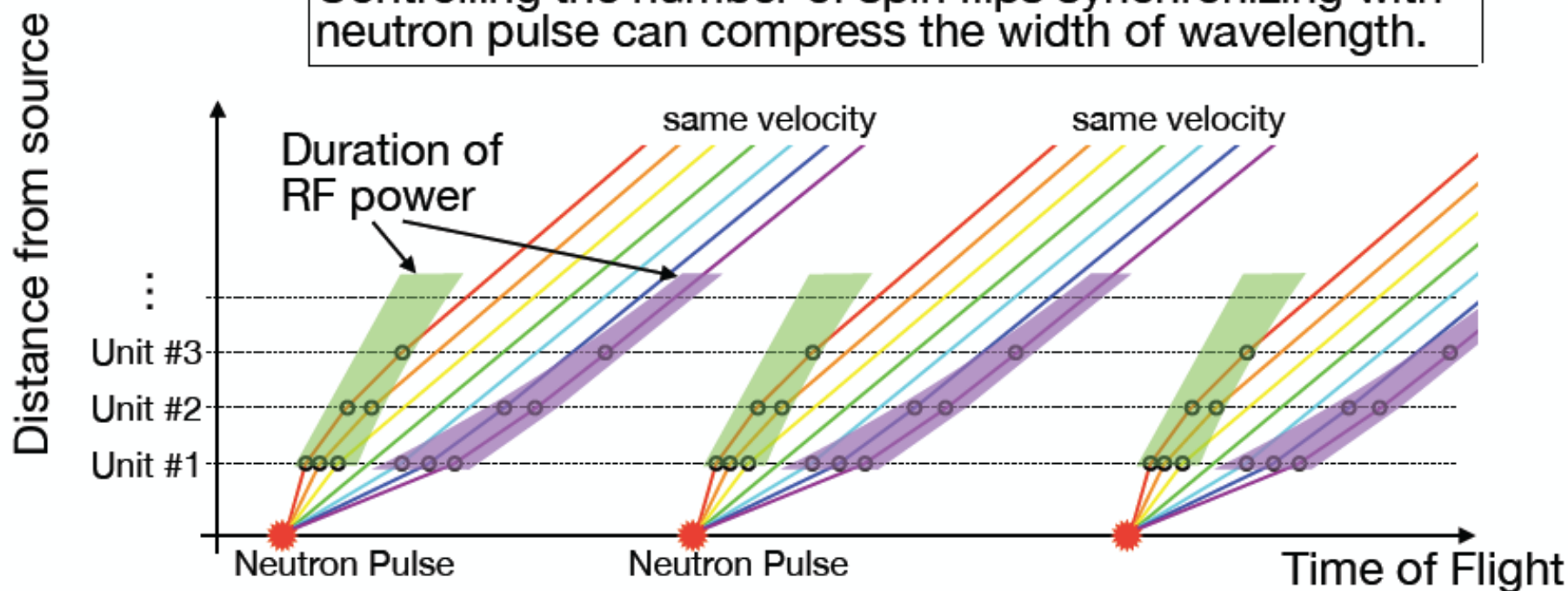


60 units = 18 m

Pulsed neutron beam from source



Controlling the number of spin flips synchronizing with neutron pulse can compress the width of wavelength.

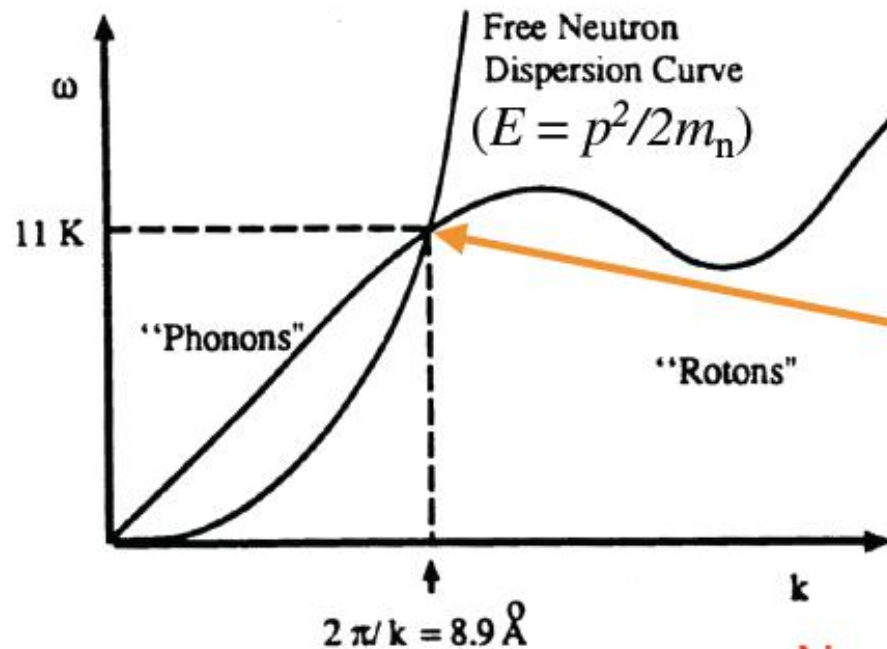


UCN production by superfluid He converter

Superthermal source

Neutron with 1 meV transfers all energy and momentum to phonon and down-scatters to UCNs in superfluid He.

Dispersion curve



UCN production

$$P_{\text{UCN}}(V_c) = N \sigma V_c \frac{k_c}{3\pi} \int_0^\infty \frac{d\phi}{d\lambda} s(\lambda) \lambda d\lambda$$

$$s(\lambda) = \hbar \int S(q, \hbar\omega) \delta(\hbar\omega - \hbar^2 k^2 / 2m_n) d\omega$$

Single phonon excitation

$$s_I(\lambda) = S^* \delta(\lambda^* - \lambda)$$

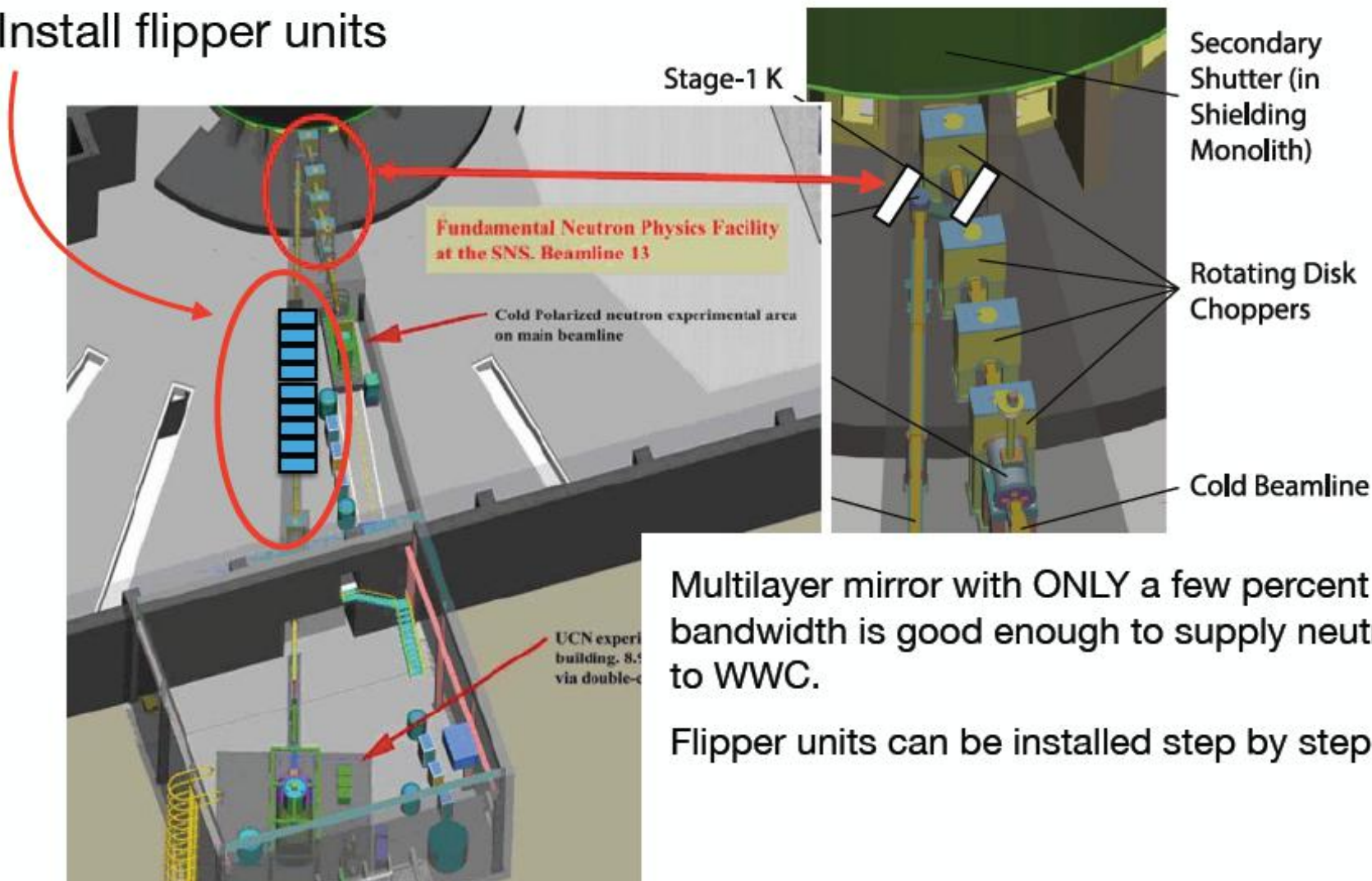
where $\lambda^* = 2\pi/q^*$

Narrow-bandwidth neutrons are required.

Possible setup for SNS-UCN beamline

N. Fomin et al. / Nuclear Instruments and Methods in Physics Research A 773 (2015) 45–51

Install flipper units



Multilayer mirror with ONLY a few percent bandwidth is good enough to supply neutrons to WWC.

Flipper units can be installed step by step.

Summary

Intense VCN beam introduces

NNBAR,

optically controlled applications,

advanced interferometry for

precise determination of scattering length,

search for new interactions,

anomalous short-range gravity, dark energy search via chameleon mechanism

laboratory test of general relativity,

etc.