



NCrystal : a library for thermal neutron transport



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- **The NCrystal project: Background, history, introduction**
 - Jupyter: Python API and core NCrystal concepts
- **Using NCrystal as backend engine**
 - Jupyter: Scatter patterns with the builtin MiniMC framework
- **NCrystal material formats and data lib.**
 - Jupyter: Data infrastructure and standard data library
- **NCrystal physics algorithms**
 - (Recap of thermal neutron scattering theory)
 - NCrystal elastic physics algorithms
 - Jupyter: Creating materials and the NCMATComposer (first half)
 - NCrystal inelastic physics algorithms
 - Jupyter: Creating materials and the NCMATComposer (second half)
- **Bits and pieces: Other features, plans, etc.**
 - Afternoon: More Jupyter-based tutorials with various examples and use-cases.



Jupyter tutorials at:

<https://github.com/mctools/ncrystal-notebooks/>

**This includes links to open in
the cloud at google Colab**

These slides also available at:

<https://indico.esss.lu.se/event/3439/>

NCrystal: background, history, brief introduction.



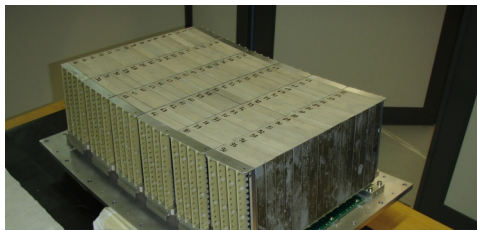
The NCrystal project: Background

<https://mctools.github.io/ncrystal/>

NCrystal

Thermal Neutron Transport

Original motivation back in ~2014 (X.X. Cai and T. Kittelmann):
Augment Geant4 with proper modelling of thermalised neutrons in crystalline materials (and avoid the usual free-gas treatment)

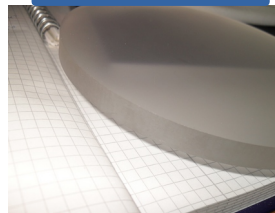


Detector frames, vessels, supports
(polycrystalline metals)

Crystalline samples



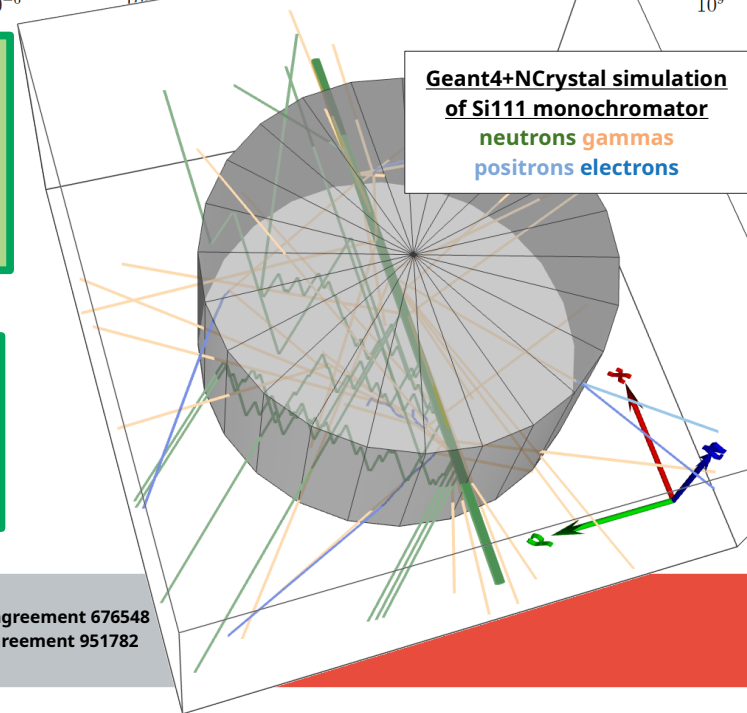
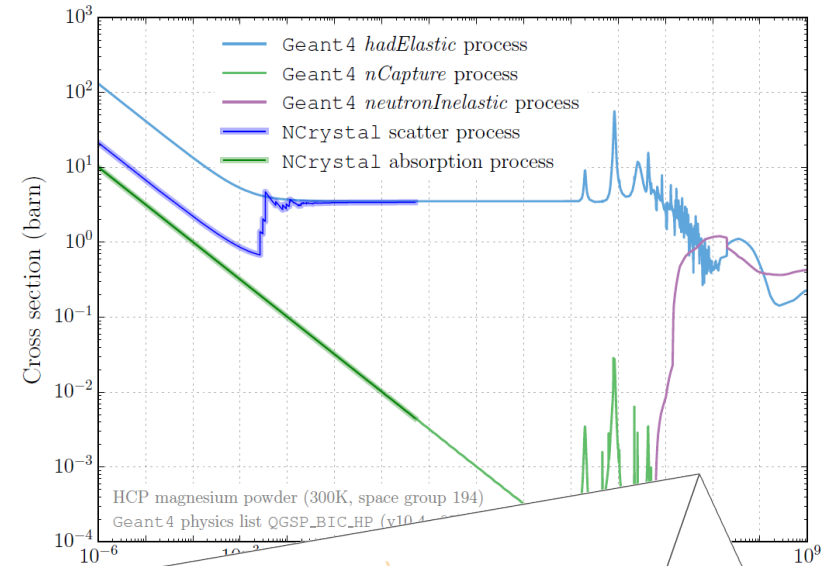
Filters
(single- or poly-crystals)



Monochromators,
analysers
(single crystals,
layered crystals)

Advanced earlier efforts in older "NXSG4" plugin
- T. Kittelmann & M Boin 2015 *Comput. Phys. Commun.* **189**, 114-118
- Geant4-specific plugin for polycrystals, no inelastic, no tools/bindings - just a thin wrapper around nxslib by M. Boin.

Scope has since expanded beyond Geant4!
And the physics scope has extended
beyond crystals and beyond Bragg diffraction!



A brief history of NCrystal

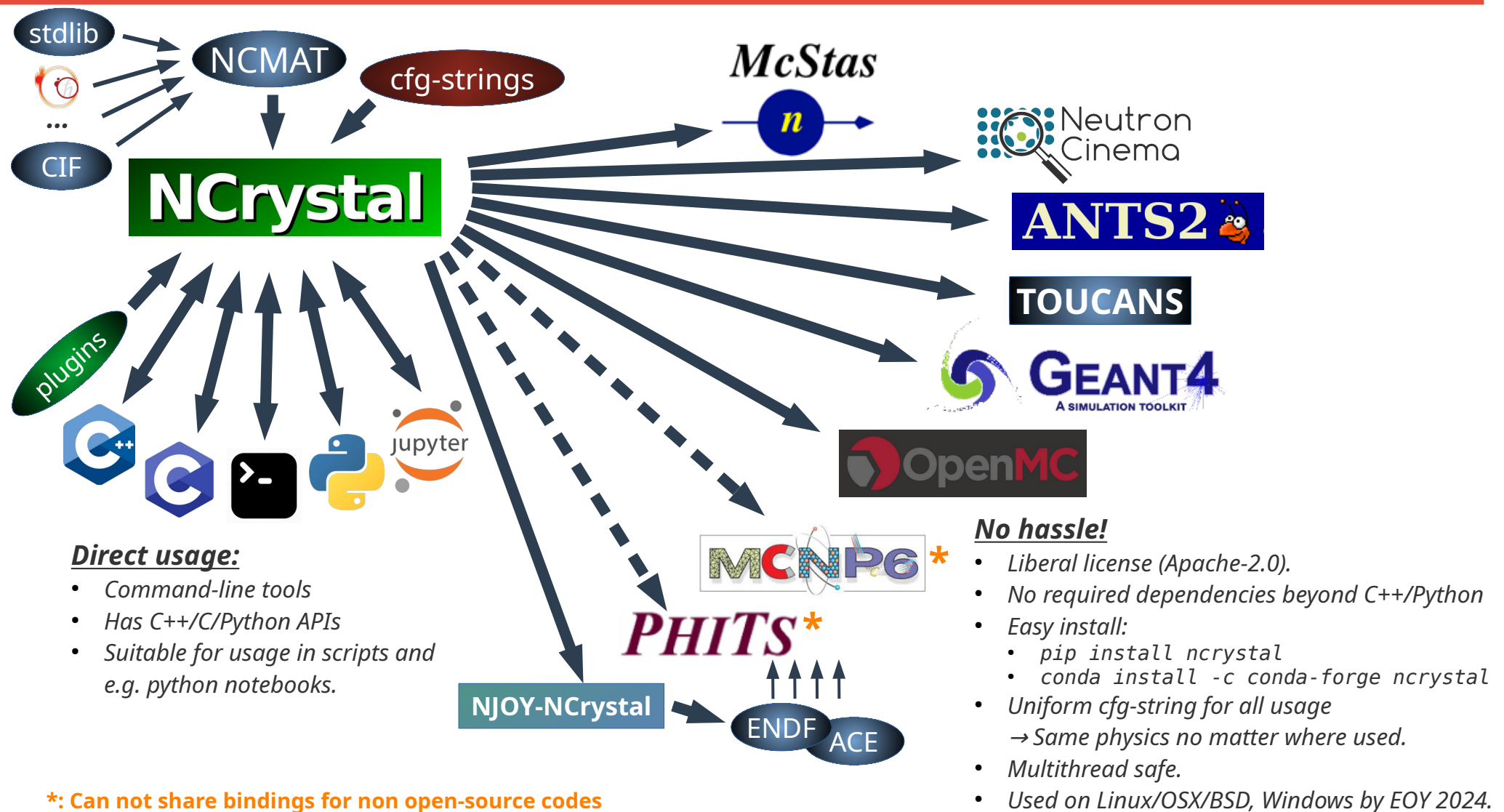
(no, this will not be on the test)



- (prehistoric: NXSG4 in 2014 by T. Kittelmann + M. Boin)
- **~2015**: T. Kittelmann + X. X. Cai of the ESS Detector Group and DTU NuTech join separate efforts aimed at adding thermal neutron physics to Geant4. Quickly decide to make it a standalone project and add support for McStas as well. Both join the Geant4 collaboration to get NCrystal integrated, and also work with P. Willendrup on McStas integration.
- **2019 (v1.0)**: After years of development and writing the first publication, release 1.0, focusing on Bragg diffraction and crystalline materials. HKL structure factors are calculated on the fly at startup. Contains minimal C++/C/Python API and hooks for Geant4 and McStas.
- **2020 (v2.0)**: with inelastic physics: scattering kernels and a unique capability to expand phonon spectra to scattering kernels on the fly.
- **2020 (fall) (v2.1-2.4)**: Support atomic/isotopic mixtures, virtual files, and a system for third-party plugins with specific new physics.
- **March 2021 (v2.5)**: Major C++11 rewrite for safe modern C++. Becomes multi-thread safe and gets a flexible data-source structure.
- **April 2021 (v2.6)**: K. Ramic, J. I. Marquez Damian, and D. DiJulio join the efforts, and most files in the data library gets phonon DOS curves added. We also begin to estimate atomic displacements from such curves.
- **May 2021 (v2.7)**: The data library grows enormously (now arguably world leading!) thanks again to collaboration with the same people. Add support for amorphous materials, add cmdline tools for adding new materials.
- **April 2022 (v3.0)**: Large update with multi-phase materials, support for SANS physics, new cfg-parameters like “density”, “one-liner materials”, etc.
- **June 2022 (v3.1)**: Focus on UCN (ultra cold neutron) production in inelastic collisions, ensuring artifact-free modelling and possibilities for biasing.
- **August 2022 (v3.2)**: Support for easily configuring gas-mixtures.
- **Aug-Dec 2022 (v3.3-3.5)**: Improve CMake layer and introduce ncrystal-config command. Improve integrations with McStas (with P. Willendrup and M. Bertelsen) and Geant4. Bindings for OpenMC in OpenMC 13.3 release. NCrystal appears on conda-forge. CI tests improves with help of M. Klausz.
- **May 2023 (v3.6)**: Large improvement of python API, many utilities for creating new materials from a variety of sources. Publish Jupyter tutorials.
- **July 2023 (v3.7)**: NCrystal appears on PyPI, “pip install ncrystal” now works! ESS DMSC supports NCrystal.
- **December 2024 (v3.8)**: NCrystal components move into McStas itself, NCrystal+McStas integration improves via conda (work with P. Willendrup).
- **August 2024 (v3.9)**: NCrystal ships with “MiniMC” for fast simple diffraction patterns.
- **October 2024 -** : NCrystal work supported by APRENDE EURATOM grant (T.K. with J. I. Marquez Damian, and D. DiJulio).
- Along the way, supported by: two EU projects, EURATOM, got physics in external plugins (Thanks N. Rizzi, S. Xu, CSNS), and were supported in various fashions by many people not mentioned already, in particular: T. R. Nielsen, V. Santoro, R.H.Wilton, K.Kanaki, A. Morozov, E. Klinkby, E. Knudsen, ...
- Many ongoing ideas and developments at ESS (in various groups), and CSNS in particular.

Not such an old project, but a lot of activity and many people contributing in many ways!
Always looking for more contributions!

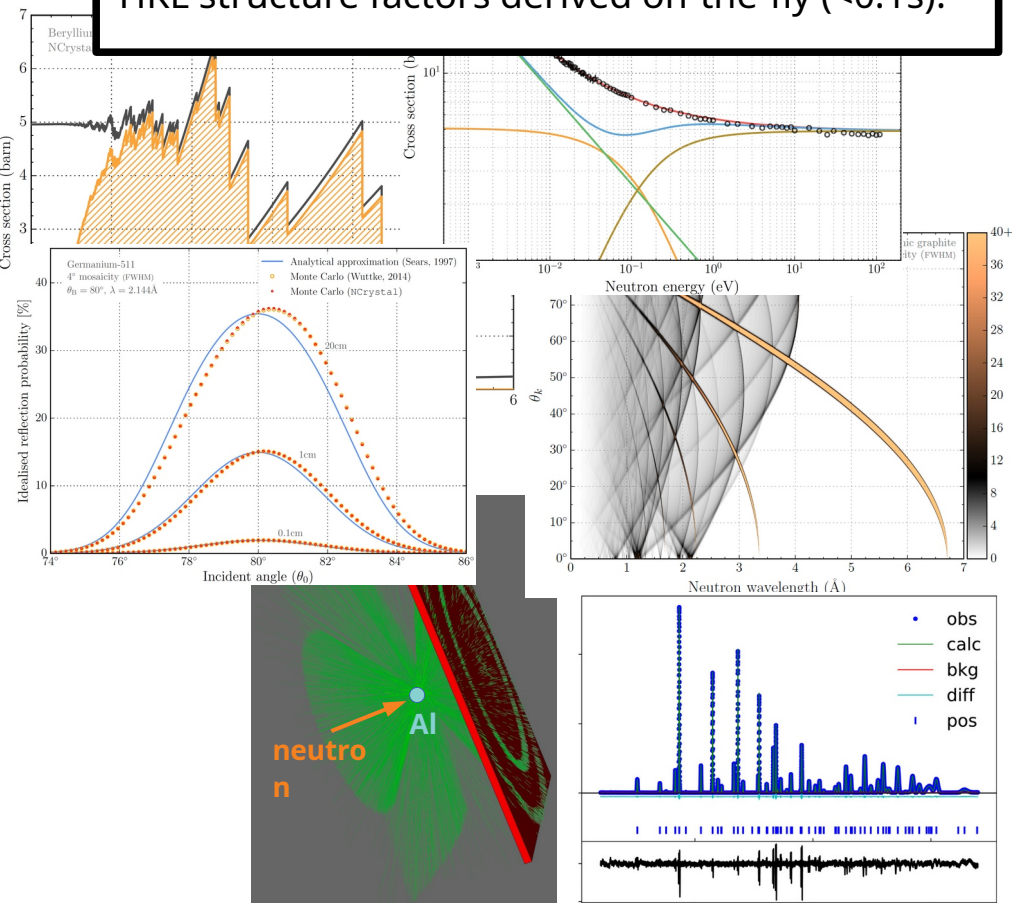
NCrystal: Open Source backend providing thermal neutron scattering to MC codes



Standard physics in NCrystal (crystals/liquids/amorphous solids/gasses)

Elastic ($\Delta E=0$) components

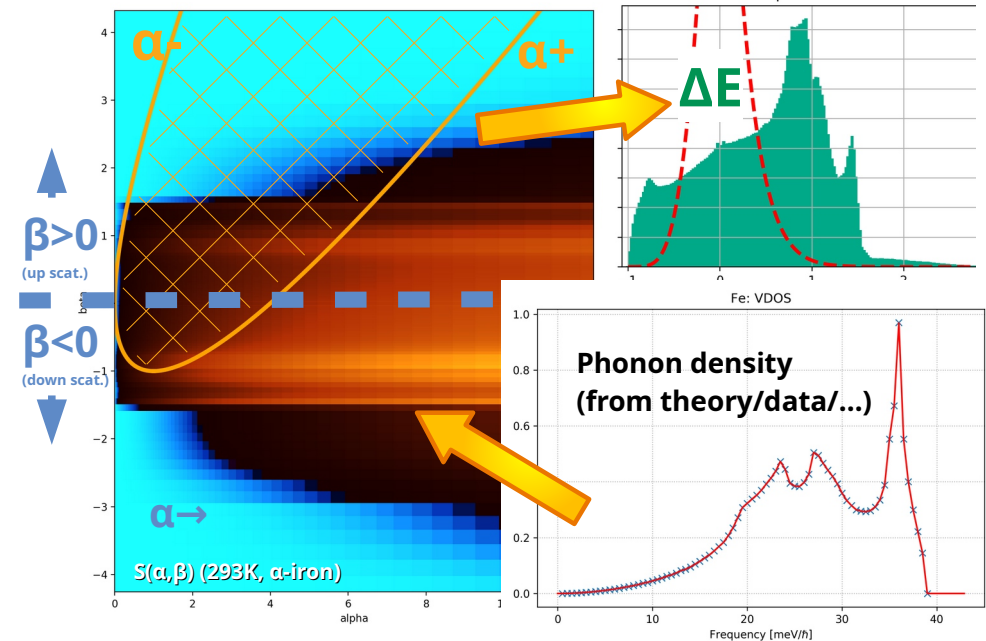
Bragg diffraction, incoherent, single crystals, isotropic materials (powders), HOPG.
HKL structure factors derived on-the-fly (<0.1s).



Inelastic ($\Delta E \neq 0$) components

Scattering kernel based:

- Initialise from external kernel
- Or from phonon density curve (~0.1s).
- Using incoherent approximation (for now!)



More info about NCrystal

NCrystal

Thermal Neutron Transport

Forum for questions/discussions, issue tracker, wiki, data library page at:
<https://github.com/mctools/ncrystal>

Embedded documentation:
Entire Python API has doc-strings.
Command-line tools have -h / --help flags



Jupyter tutorials at:
<https://github.com/mctools/ncrystal-notebooks/>

General info:
DOI 10.1016/j.cpc.2019.07.015

Details about elastic models:
DOI 10.1016/j.cpc.2021.108082

Core NCrystal concepts

All other features, tools, hooks, etc. are built upon these.

NCrystal

Thermal Neutron Transport

Inputs

cfg-strings

```
"Al_sg225.ncmat"  
"Y2SiO5_sg15_Y50.ncmat;dcutoff=0.5Aa"  
"gasmix::0.7xCO2+0.3xAr/1.5atm/250K"  
""phases<0.1*PbS_sg225_LeadSulfide.ncmat  
&0.9*Epoxy_Araldite506_C18H2003.ncmat>""  
"Rubber_C5H8.ncmat;temp=200;vdoslux=4"  
"LiquidHeavyWaterD20_T293.6K.ncmat"
```

data

Preferred native format is the NCMAT (.ncmat) format.

Can reside in actual files, or as content in memory.

Can be hand-crafted, auto-converted, or generated on-demand by plugins.

Outputs

Info
(object)

Densities, compositions
Phases
Scattering lengths
Crystal structures, HKL factors
Dynamics info like phonon DOS

Scatter
process
(object)

Provides integrated scattering cross sections when queried with neutron state.
Can perform Monte Carlo sampling of outgoing states.

Absorption
process
(object)

Provides integrated absorption cross sections when queried with neutron state.
Presently only implements simple $1/v$ model.

Apply after "filename" part, separated with semicolons:

```
"Al_sg225.ncmat;density=2.6gcm3;temp=250K;comp=elas"
```

- **Temperature:**

- Examples: `temp=100`, `temp=100K`,
`temp=-10C`, `temp=100F`

- All materials have a temperature. The `temp` parameter does exactly what you think it does. By default it assumes the value is in kelvin, but a unit can be added (must be one of `K`, `C`, or `F`).

- **Density**

- Examples: `density=2.0gcm3`, `density=3.4kgm3`, `density=0.9x`.

- Also does what you think it does. The last example scales the density by a factor of 0.9.

- **Scattering component toggling**

- Current recognised component names are `coh_elas` (alias `bragg`), `incoh_elas`, `sans`, and `inelas`. `elas` refers to all components except `inelas`.

- Syntax: `<compname>=0` (disable component), `comp=<compname1>, ..., <compnamen>` (disable all but the listed components).

- Examples: `...;comp=inelas,sans` (only inelastic and SANS), `...;inelas=0` (without inelastic), `...;inelas=0;comp=inelas` (actually removes all components)

- **Modify atomic compositions**

- Examples: `atomdb=H is D`, `atomdb=Al:is:0.9:Al:0.1:Cr`,
`atomdb=Si29:28.97649466525u:4.7fm:0.001b:0.101b, ...`

- **Single crystal parameters**

- Single crystal models and orientations are primarily controlled by the parameters `mos`, `dir1`, `dir2`, and `dirtol`. Refer to the documentation linked above, and see examples in the notebooks.

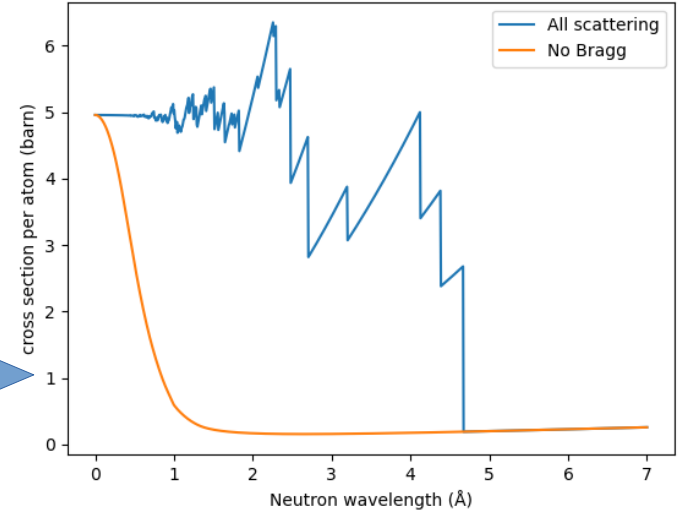
Whitespace in cfg-strings is allowed (and ignored).

Python API



```
#Plot beryllium-oxide cross sections
import NCrystal as NC
import matplotlib.pyplot as plt
import numpy
scBeO = NC.createScatter('BeO_sg186.ncmat')
scBeO_nobragg = NC.createScatter('BeO_sg186.ncmat;bragg=0')
wls = numpy.linspace(0.0,7.0,1000)
plt.plot( wls, scBeO.xsect(wl=wls), label='All scattering' )
plt.plot( wls, scBeO_nobragg.xsect(wl=wls), label='No Bragg' )
plt.xlabel('Neutron wavelength (Å)')
plt.ylabel('cross section per atom (barn)')
plt.legend()
plt.show()
```

*Universal cfg-strings
→ Same cfg in McStas, Geant4, ...*



...or just do: NC.load('Beo_sg186.ncmat').plot()

```
#Can also extract more detailed info:
info_BeO = NC.createInfo('BeO_sg186.ncmat')
info_BeO.dump()
print('Density [g/cm3]: %g'%info_BeO.density)
print('Number density [atoms/Å³]: %g'%info_BeO.numberdensity)
for fraction,atom in info_BeO.composition:
    print(f'Has {fraction*100}% {atom}')
for hkl in [ hkl for hkl in info_BeO.hklObjects()
            if ( 1.1 < hkl.d < 1.17) ]:
    print(f'N={hkl.mult} d={hkl.d:g}Å F²={hkl.f2:g}barn',
          list(zip(hkl.h,hkl.k,hkl.l)))
```

Prints all info to terminal

 **Jupyter tutorials available at:**
<https://github.com/mctools/ncrystal-notebooks/>

**conda install -c conda-forge ncrystal
or pip install ncrystal**

```
Density [g/cm3]: 3.00836
Number density [atoms/Å³]: 0.144868
Has 50.0% Be=Be(cohSL=7.79fm cohXS=7.62579barn incXS=0.0018barn absXS=0.0076barn
Has 50.0% O=O(cohSL=5.803fm cohXS=4.2317barn incXS=0.0008barn absXS=0.00019barn
N=6 d=1.16827Å F²=1.66027barn [(2, 0, 0), (2, -2, 0), (0, 2, 0)]
N=12 d=1.14858Å F²=3.49424barn [(2, -1, 2), (2, -1, -2), (1, 1, 2), (1, 1, -2),
N=12 d=1.1288Å F²=0.772761barn [(2, 0, 1), (2, 0, -1), (2, -2, 1), (2, -2, -1),
```

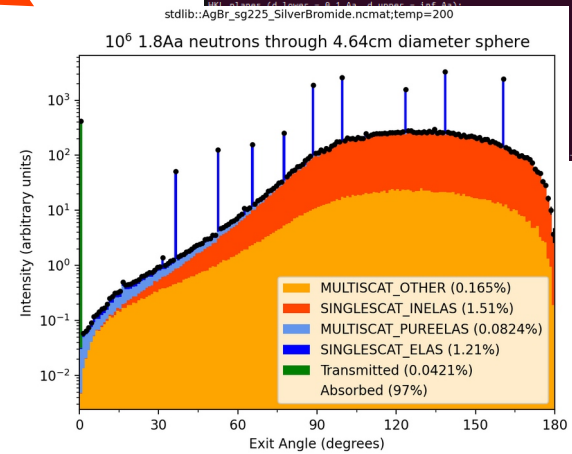
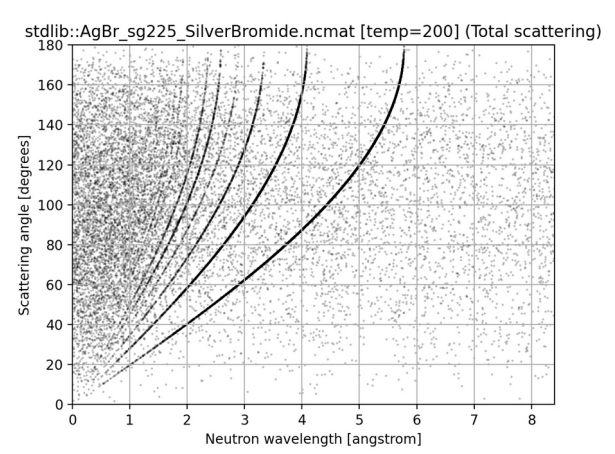
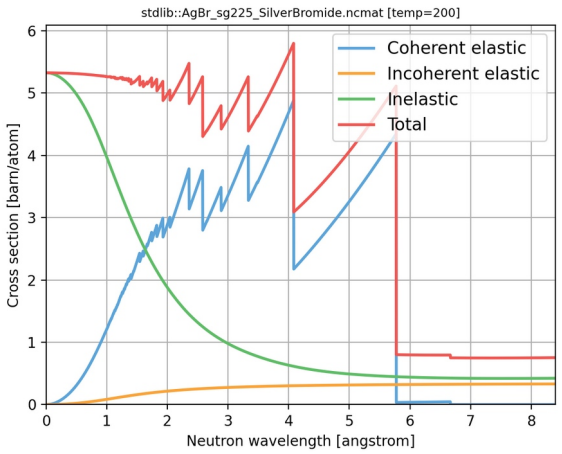
Command-line interface (CLI)

The `nctool` command allows inspection of physics resulting from a given `cfg-string`, browsing of data files, and more.

```
$> nctool --dump 'AgBr_sg225_SilverBromide.ncmat;temp=200K'
```

```
$> nctool 'AgBr_sg225_SilverBromide.ncmat;temp=200K'
```

```
..... NCrystal Material Info .....
Data source: stdlib:AgBr_sg225_SilverBromide.ncmat
Density : 6.47734 g/cm3, 0.0415477 atoms/Aa^3
Composition (by mole): 50% Br 50% Ag
Composition (by mass): 42.5535% Br 57.4465% Ag
Atom data:
Br = Br(cohSL=6.795fm cohXS=5.88215barn incXS=0.1barn absXS=6.9barn mass=79.9035u Z=35)
Ag = Ag(cohSL=5.922fm cohXS=4.40784barn incXS=0.58barn absXS=63.3barn mass=107.868u Z=47)
Averaged quantities:
Atomic mass : 93.8850u
Absorption XS at 2200m/s : 35.1 barn
Free scattering XS : 5.32549 barn
Scattering length density : 2.64181 10^-6/Aa^2
Temperature : 200 kelvin
State of matter: Solid (crystalline)
Space group number : 225
Lattice spacings [Aa] : 5.7745 5.7745 5.7745
Lattice angles [deg] : 90 90 90
Unit cell volume [Aa^3] : 192.55
Atoms / unit cell : 8
Atoms in unit cell (total 8):
4 Br atoms [I_Debye=123.347K, MSD=0.0241933Aa^2]
4 Ag atoms [I_Debye=103.372K, MSD=0.0254376Aa^2]
Atomic coordinates:
Br 0 0 1/2
Br 0 1/2 0
Br 1/2 0 0
Br 1/2 1/2 1/2
Ag 0 0 0
Ag 0 1/2 1/2
Ag 1/2 0 1/2
Ag 1/2 1/2 0
Dynamic info for Br (50%):
type: S(alpha,beta) [From VDOS]
VDOS Source: 2038 points
VDOS E_max: 18.0877 meV
Dynamic info for Ag (50%):
type: S(alpha,beta) [From VDOS]
VDOS Source: 2038 points
VDOS E_max: 18.0877 meV
HKL info type: SymEqGroup
```



Other scripts provided, mostly for conversions: `ncrystal_cif2ncmat`, `ncrystal_endf2ncmat`, `ncrystal_ncmat2hkl`, `ncrystal_hfg2ncmat`, `ncrystal-config`, ...

The Python API provides everything provided by the cmdline scripts, but sometimes a quick command in the terminal is convenient.



Time to look at the first notebook:

"Introduction to NCrystal and the Python API"



Jupyter tutorials at:

<https://github.com/mctools/ncrystal-notebooks/>



Using NCrystal as a backend engine (examples)



NCrystal in McStas



- **Works “out of the box” as long as NCrystal is installed.**
 - Automatically installs NCrystal if installing McStas from conda.
 - Automatically installs NCrystal if installing McStas from “app bundle” for Windows/MacOS, or Debian packages.
- **Several ways to use:**
 - With dedicated `NCrystal_sample.comp` gives multiple-scattering and absorption effects in single volume (box/cylinder/sphere).
 - As a physics engine in McStas Union’s advanced geometry system.



NCrystal in McStas



Standard McStas non-Union example (.instr)

```
COMPONENT mysample = NCrystal_sample(cfg="Al203_sg167_Corundum.ncmat",  
                                       radius=0.01, yheight=0.05)  
AT (0, 0, 0) RELATIVE PREVIOUS
```

McStasScript + Union example (Python)

```
import mcstasscript.tools.ncrystal_union as ncunion  
ncunion.add_ncrystal_union_material(instr,  
                                     name="myAl",  
                                     cfgstr="Al_sg225.ncmat;temp=10C")  
  
#... usual mcstasscript code for creating volume "myvol" here  
myvol.set_parameters(radius=0.01,  
                     yheight=0.01,  
                     material_string=' "myAl" ',  
                     priority=1)
```

Simply use NCrystal cfg-strings
when creating materials

Can of course also use Union+NCrystal in .instr and NCrystal_sample in McStasScript.

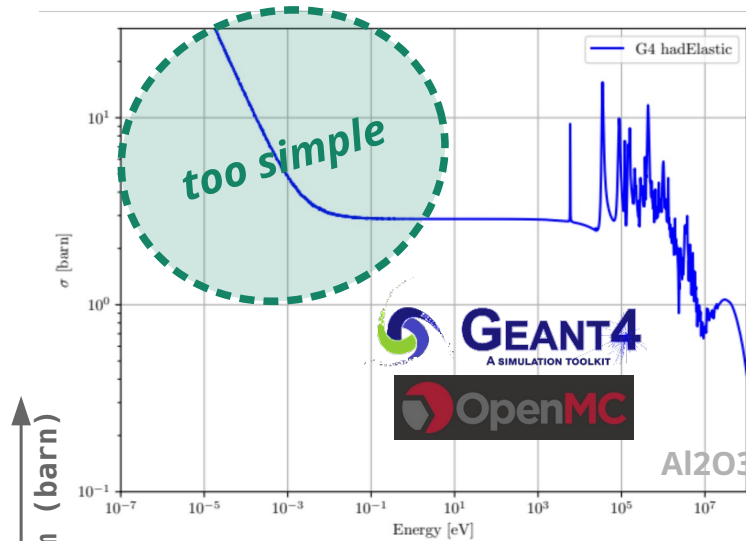


NCrystal + OpenMC/Geant4

Combining two regimes of neutron scattering

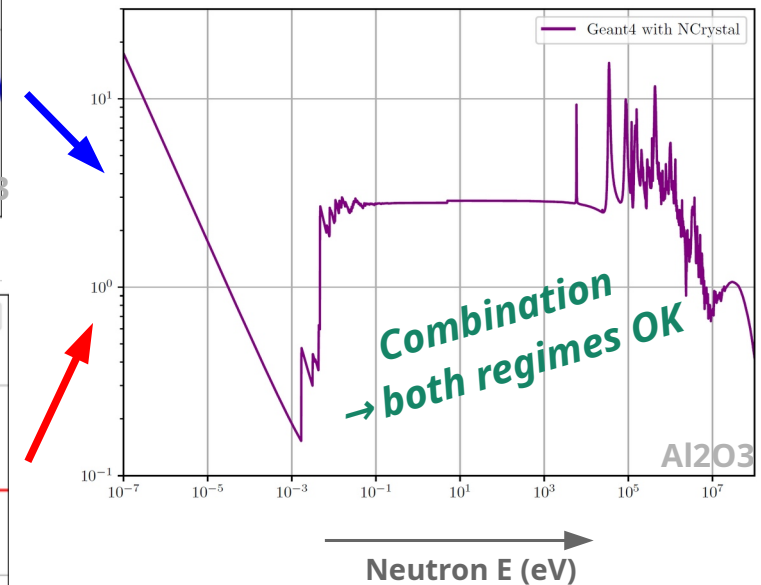
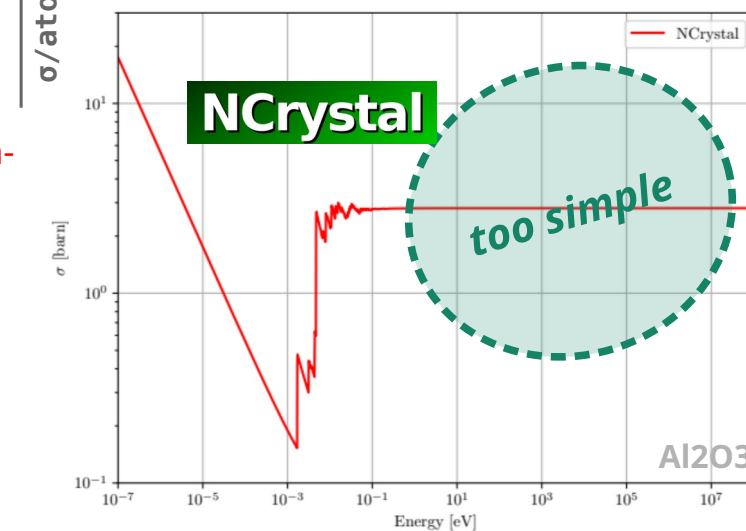
Higher energy ($\gg eV$):

- Complex neutron-nuclei interactions with energy dependent strength.
- Not sensitive to material structure.



Low energy ($\ll eV$):

- Simple (point-like) neutron-nuclei interactions with constant strength.
- Very sensitive to material structure.



NCrystal in OpenMC



```
import openmc
# Materials
openmc_mat = openmc.Material.from_ncrystal('Polyethylene_CH2.ncmat;temp=50C')
# Geometry
s1 = openmc.Sphere(r=10, boundary_type='vacuum')
c1 = openmc.Cell(region=-s1, fill=openmc_mat)
geometry = openmc.Geometry([c1])
# Execution settings
settings = openmc.Settings()
settings.source = openmc.Source(energy=openmc.stats.Discrete(x=[10.0], p=[1.0]))
settings.run_mode = 'fixed source'
settings.batches = 10
settings.particles = 10000
# Write xml files
model = openmc.model.Model(geometry=geometry, settings=settings)
model.export_to_xml()
#Now launch openmc
#Check resulting materials.xml (we could of course actually RUN OpenMC here instead)
import pathlib
print(pathlib.Path('materials.xml').read_text())
```

Simply use NCrystal cfg-strings
when creating materials

Currently needs OpenMC built with
-DOPENMC_USE_NCRYSTAL=0n

Plan is to enable this in
OpenMC conda packages.



NCrystal in Geant4



```
//Include the relevant header:  
#include "G4NCrystal/G4NCrystal.hh"
```

```
//...
```

```
//Create materials directly from cfg-strings:
```

```
G4Material * mat_aluminium = G4NCrystal::createMaterial("Al_sg225.ncmat");
```

```
//...
```

```
//Currently the NCrystal process must then be injected in the following way:
```

```
g4runManager->Initialize();
```

```
G4NCrystal::installOnDemand();
```

```
g4runManager->BeamOn(1000)
```

Simply use NCrystal cfg-strings
when creating materials



Somewhat unusual initialisation
(plan to improve this)



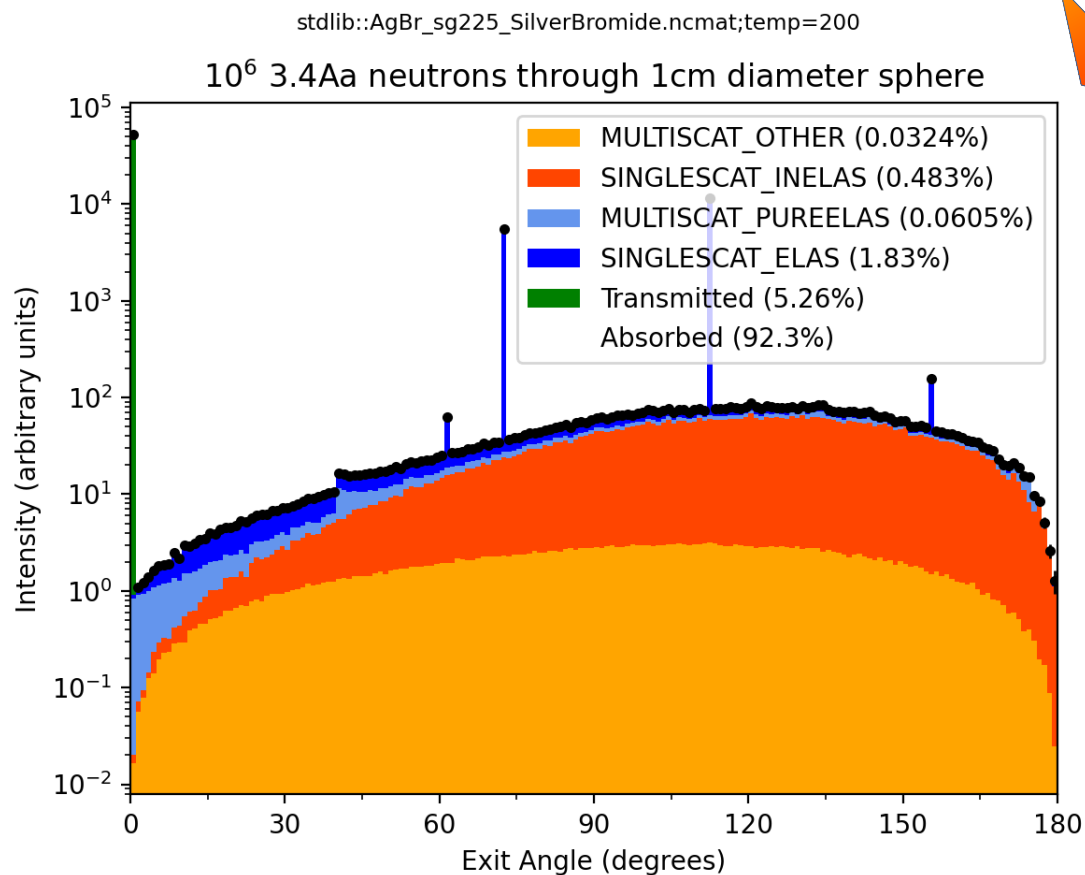
Currently needs custom build of NCrystal with:
-DNCRYSTAL_ENABLE_GEANT4=On

Plan to migrate to standalone package and
make it work out of the box in conda.



Built-in "Mini MC" for scatter patterns with multiple-scattering effects

```
$> nctool --mc 3.4Aa 1cm 'stdlib::AgBr_sg225_SilverBromide.ncmat;temp=200K'
```



Runs multithreaded and vectorised, for fast results (ultimately intended for possible usage in diffraction analysis)

Time for this particular simulation on my laptop:

Load material: 140ms
Run simulation: 170ms
Total: 310ms

Note: 10⁶ src neutrons → >10⁷ tally entries due to some variance reduction tricks.



Try it in the notebook:
"Using the built-in MiniMC framework
for generating scatter patterns"



Jupyter tutorials at:
<https://github.com/mctools/ncrystal-notebooks/>



NCrystal material formats and data library



The NCMAT data format for materials

<https://github.com/mctools/ncrystal/wiki/NCMAT-format>

NCrystal

Thermal Neutron Transport

- NCrystal supports multiple input formats
- But NCMAT (.ncmat) is the native one.
- Can load from on-disk file, memory buffers, data generated by plugins, ...

Info

Native NCrystal format (static or dynamic)

.ncmat loader

Optional formats added for McStas community

.nxs loader

.laz/.lau loader

Info

inelastic

Bragg (powder)

Bragg (single crystal)

Incoherent elastic

Absorption

NCMAT loader

```
NCMAT v7 Ge_sg227.ncmat
#Comments here (not shown)
@CELL
cubic 5.65735
@SPACEGROUP
227
@ATOMPOSITIONS
Ge 1/2 1/2 1/2
Ge 1/4 1/4 3/4
Ge 1/2 0 0
Ge 1/4 3/4 1/4
Ge 0 1/2 0
Ge 3/4 1/4 1/4
Ge 0 0 1/2
Ge 3/4 3/4 3/4
@DYNINFO
element Ge
fraction 1
type vdos
vdos_egrid .0037709 .0377897
vdos_density .0064216 .0067183 .0070150
.0074164 .0078883 .0078611 .0078339
#(-50 lines here not shown)
.032778 .02264 .012923 .002484 0
```

```
----- NCrystal Material Info -----
Data source: Ge_sg227.ncmat
Density : 5.3288 g/cm3, 0.0441826 atoms/Aa^3
Composition (by mole): 100% Ge
Composition (by mass): 100% Ge
Atom data:
Ge = Ge(cohSL=8.185fm cohXS=8.41874barn incXS=0.18barn absXS=2.2barn mass=72.6322u Z=32)
Averaged quantities:
Atomic mass : 72.6322u
Absorption XS at 2200m/s : 2.2 barn
Free scattering XS : 8.3648 barn
Scattering length density : 3.61634 10^-6/Aa^2
Temperature : 293.15 kelvin
State of matter: Solid (crystalline)
Space group number : 227
Lattice spacings [Aa] : 5.65735 5.65735 5.65735
Lattice angles [deg] : 90 90 90
Unit cell volume [Aa^3] : 181.067
Atoms / unit cell : 8
Atoms in unit cell (total 8):
8 Ge atoms [T_Debye=295.348K, MSD=0.00692135Aa^2]
Atomic coordinates:
Ge 0 0 1/2
Ge 0 1/2 0
Ge 1/4 1/4 3/4
Ge 1/4 3/4 1/4
Ge 1/2 0 0
Ge 1/2 1/2 1/2
Ge 3/4 1/4 1/4
Ge 3/4 3/4 3/4
Dynamic info for Ge (100%):
type: S(alpha,beta) [from VDOS]
VDOS Source: 425 points
VDOS E_max: 37.7897 meV
HKL info type: SymEqvGroup
HKL planes (d_lower = 0.1 Aa, d_upper = inf Aa):
H K L d_hkl[Aa] Mult. FSquared[barn]
1 1 1 3.26627 8 20.896
2 2 0 2.00018 12 40.0457
3 1 1 1.70576 24 19.5165
4 0 0 1.41434 6 37.4019
3 3 1 1.29789 24 18.2281
```

Conversions from/to other formats supported by Python/CLI tools: CIF, ENDF, .laz/.lau, ...

Neutron interactions (scatter processes), Based on this "Info" object.

NCrystal data library

Browse with performance plots at: <https://github.com/mctools/ncrystal/wiki/Data-library>

AcrylicGlass_C502H8.ncmat
AgBr_sg225_SilverBromide.ncmat
Ag_sg225.ncmat
Al2O3_sg167_Corundum.ncmat
Al4C3_sg166_AluminiumCarbide.ncmat
ALN_sg186_AluminumNitride.ncmat
Al_sg225.ncmat
Ar_Gas_STP.ncmat
Au_sg225.ncmat
BaF2_sg225_BariumFluoride.ncmat
BaO_sg225_BariumOxide.ncmat
Ba_sg229.ncmat
Be3N2_sg206_BerylliumNitride.ncmat
BeF2_sg152_BerylliumFluoride.ncmat
BeO_sg186.ncmat
Be_sg194.ncmat
Bi_sg166.ncmat
CaCO3_sg62_Aragonite.ncmat
CaF2_sg225_CalciumFluoride.ncmat
CaH2_sg62_CalciumHydride.ncmat
CaOH2_sg164_CalciumHydroxide.ncmat
CaO_sg225_CalciumOxide.ncmat
Ca_sg225.ncmat
Ca_sg229_Calcium-gamma.ncmat
CaSiO3_sg2_Wollastonite.ncmat
CeO2_sg225_CeriumOxide.ncmat
Cr_sg229.ncmat
C_sg194_pyrolytic_graphite.ncmat
C_sg227_Diamond.ncmat
Cu2O_sg224_Cuprite.ncmat
Cu_sg225.ncmat
Dy2O3_sg206_DysprosiumOxide.ncmat
Epoxy_Araldite506_C18H2003.ncmat
Fe_sg225_Iron-gamma.ncmat
Fe_sg229_Iron-alpha.ncmat
GaN_sg186_GalliumNitride.ncmat
GaSe_sg194_GalliumSelenide.ncmat
Ge3Bi4012_sg220_BismuthGermanate.ncmat
Ge_sg227.ncmat
He_Gas_STP.ncmat
HfO2_sg14_HafniumOxide.ncmat
Ho2O3_sg206_HolmiumOxide.ncmat
Kapton_C22H10N2O5.ncmat
KBr_sg225_PotassiumBromide.ncmat
KF_sg225_PotassiumFluoride.ncmat
KOH_sg4_PotassiumHydroxide.ncmat
Kr_Gas_STP.ncmat
K_sg229.ncmat
LaBr3_sg176_LanthanumBromide.ncmat
Li2O_sg225_LithiumOxide.ncmat
Li3N_sg191_LithiumNitride.ncmat
LiF_sg225_LithiumFluoride.ncmat
LiH_sg225_LithiumHydride.ncmat
LiquidHeavyWaterD20_T293.6K.ncmat
LiquidWaterH2O_T293.6K.ncmat
Lu2O3_sg206_LutetiumOxide.ncmat
Lu2SiO5_sg15.ncmat
Mg2SiO4_sg62_MagnesiumSilicate.ncmat
MgAl2O4_sg227_MAS.ncmat
MgCO3_sg167_MagnesiumCarbonate.ncmat
MgO2_sg136_MagnesiumDeuteride.ncmat
MgF2_sg136_MagnesiumFluoride.ncmat
MgH2_sg136_MagnesiumHydride.ncmat
MgOH2_sg164_MagnesiumHydroxide.ncmat
MgO_sg225_Periclase.ncmat
Mg_sg194.ncmat
Mo_sg229.ncmat
Na4Si3Al3012Cl_sg218_Sodalite.ncmat
NaBr_sg225_SodiumBromide.ncmat
NaCl_sg225_SodiumChloride.ncmat
NaF_sg225_SodiumFluoride.ncmat
NaI_sg225_SodiumIodide.ncmat
Na_sg229.ncmat
Nb_sg229.ncmat
Ne_Gas_STP.ncmat
Ni_sg225.ncmat
Nylon11_C11H21NO.ncmat
Nylon12_C12H23NO.ncmat
Nylon610_C16H30N2O2.ncmat
Nylon66or6_C12H22N2O2.ncmat
PbF2-beta_sg225_BetaLeadFluoride.ncmat
PbO-alpha_sg129_Litharge.ncmat
PbO-beta_sg57_Massicot.ncmat
Pb_sg225.ncmat
PbS_sg225_LeadSulfide.ncmat
Pd_sg225.ncmat
PEEK_C19H1203.ncmat
Polycarbonate_C1603H14.ncmat
Polyester_C10H8O4.ncmat
Polyethylene_CH2.ncmat
Polylactide_C3H4O2.ncmat
Polypropylene_C3H6.ncmat
Polystyrene_C8H8.ncmat
Pt_sg225.ncmat
PVC_C2H3Cl.ncmat
Rb_sg229.ncmat
Rubber_C5H8.ncmat
Sc_sg194.ncmat
SiC-beta_sg216_BetaSiliconCarbide.ncmat
SiO2-alpha_sg154_AlphaQuartz.ncmat
SiO2-beta_sg180_BetaQuartz.ncmat
Si_sg227.ncmat
Sn_sg141.ncmat
SrF2_sg225_StrontiumFluoride.ncmat
SrH2_sg62_StrontiumHydride.ncmat
Sr_sg225.ncmat
Th3N4_sg166_ThoriumNitride.ncmat
ThO2_sg225_ThoriumDioxide.ncmat
Th_sg225.ncmat
TiO2_sg136_Rutile.ncmat
TiO2_sg141_Anatase.ncmat
Ti_sg194.ncmat
TLBr_sg221_ThaliumBromide.ncmat
Tm2O3_sg206_ThuliumOxide.ncmat
UF6_sg62_UraniumHexafluoride.ncmat
UO2_sg225_UraniumDioxide.ncmat
void.ncmat
V_sg229.ncmat
W_sg229.ncmat
Xe_Gas_STP.ncmat
Y2O3_sg206_YttriumOxide.ncmat
Y2SiO5_sg15_YSO.ncmat
Y3Al5O12_sg230_YAG.ncmat
Y_sg194.ncmat
ZnF2_sg136_ZincFluoride.ncmat
ZnO_sg186_ZincOxide.ncmat
Zn_sg194.ncmat
ZnS_sg216_Sphalerite.ncmat
ZrF4-beta_sg84.ncmat
ZrO2_sg137_Zirconia.ncmat
ZrO2_sg14_Zirconia.ncmat
Zr_sg194.ncmat

132 materials (v3.9.3):
Crystals (108), amorphous solids (16), liquids, gasses, ...

Easy universal cfg:
"Al_sg225.ncmat;temp=250K"
"Rubber_C5H8.ncmat;comp=inelas"
- Same physics in all applications!
- Cfg variables documented at:
github.com/mctools/ncrystal/wiki/CfgRefDoc

Small (few kB) file sizes:
- Optionally embed in binary and avoid need for actual files.

Easy to create more:

- Hand-write NCMAT file (human readable ASCII, format well-defined & versioned) or use new NCMATComposer.
- Convert from ENDF, CIF, online crystal DB carbohydrate chemical formula, Quantum Espresso output, ...
- Request help on GitHub/ncrystal.

Can be converted to other formats:

- To .laz/.lau for McStas
- To ENDF via the NJOY-NCrystal project
- But limited by target format physics capabilities!

NCrystal data library wiki page

<https://mctools.github.io/ncrystal/> → wiki → Data-library

NCrystal

Thermal Neutron Transport

The screenshot shows the NCrystal data library wiki page. It features a table with columns for 'Data file (.ncmat)', 'Properties', and 'Plot validation'. Two materials are visible: AcrylicGlass_C502H8 and AgBr_sg225_SilverBromide. The AcrylicGlass_C502H8 entry shows properties like State: Solid (amorphous), Density: 1.18 g/cm³, and Inelastic models: 53.3% H: VDOS, 33.3% C: Debye model, 13.3% O: Debye model. The AgBr_sg225_SilverBromide entry shows State: Solid (crystalline), Structure: Fm-3m (225), Density: 6.477 g/cm³, and Inelastic models: 50% Br: VDOS, 50% Ag: VDOS. To the right of the table are two plots. The top plot shows the cross section (barn) versus energy (eV) for Ni_sg225.ncmat, with data points from R.G. Allen (1954 EXFOR 11762002) and H. Palevsky (1954 EXFOR 11355002). The bottom plot shows the cross section (barn) versus energy (eV) for Polyethylene-CH2.ncmat, with data points from Granada (1987) and Lee (2020). A callout box points to the plots with the text 'Browse derived quantities, plots, validations, ...'. Another callout box points to the table with the text 'To use in Geant4/McStas/OpenMC/Python/..., simply supply name of material file, along with relevant parameters like temperature, orientation of single crystal, etc.'

```
NCMAT v1
#Some comment here...
@CELL
  lengths 4.04958 4.04958 4.04958
  angles 90. 90. 90.
@SPACEGROUP
  225
@ATOMPOSITIONS
  Al 0. 0.5 0.5
  Al 0. 0. 0.

  Al 0.5 0. 0.5  Al_sg225.ncmat
@DEBYETEMPERATURE
```

Browse derived quantities,
plots, validations, ...

To use in Geant4/McStas/OpenMC/Python/..., simply supply name of material file, along with relevant parameters like temperature, orientation of single crystal, etc.

Alternatively browse locally with:
nctool -browse
And then:
nctool [-dump|--extract] SomeFile.ncmat

NOTE: M. Klausz is working on a much improved less static datalib website.

In-memory data

With or without a "filename"

NCrystal

Thermal Neutron Transport

Register as virtual file with filename:

```
import NCrystal as NC
content="""NCMAT v3
@CELL
  lengths 4.04958 4.04958 4.04958
  angles 90 90 90
@SPACEGROUP
  225
@ATOMPOSITIONS
  Al 0 1/2 1/2
  Al 0 0 0
  Al 1/2 1/2 0
  Al 1/2 0 1/2
@DEBYETEMPERATURE
  Al 410.4
"""
```

```
NC.registerInMemoryFileData( "MyAl.ncmat",content)
sc = NC.createScatter("MyAl.ncmat")
```

Accessing data is of course possible:

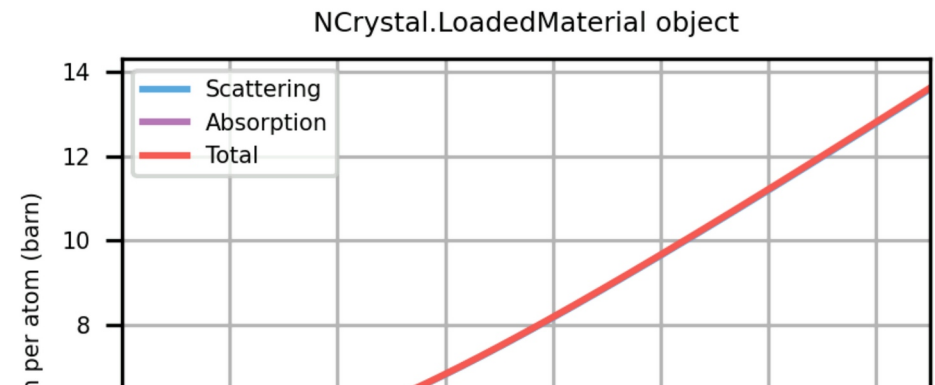
```
nctool -extract Al_sg225.ncmat
NC.createTextData('Al_sg225.ncmat')
```

NCrystal conda/pip packages use this to embed standard data lib files into libNCrystal.

(using CMake -DNCRYSTAL_ENABLE_DATA=EMBED)

Load NCMAT data directly:

```
a_string_with_ncmat_data="""NCMAT v7
#Don't use this material for anything
@DENSITY
  1.2345 g_per_cm3
@DYNINFO
  element C
  fraction 1
  type freegas
"""
NC.load(a_string_with_ncmat_data).plot()
```



Quick one-liner materials

Especially useful for gas mixtures and highly absorbing materials

NCrystal

Thermal Neutron Transport

- NCrystal's flexible data infrastructure allows plugins to provide one-liner materials, i.e. materials completely defined by their cfg-string without the need for actual NCMAT data.
- This is best for materials without the need for e.g. unit cell positions or DOS curves.
- The one-liner goes in the "filename" part of a cfg-string.
- Dedicated plugins (currently "freegas", "solid", "gasmix") analyse the "filename" and produces corresponding NCMAT data on-the-fly (run "nctool --browse" for examples).
- Examples:

```
"solid::B4C/2.52gcm3/B_is_0.95_B10_0.05_B11"  
"gasmix::0.72xC02+0.28xAr/massfractions/1.5atm/250K"  
"gasmix::0.7xC02+0.3xAr/0.001relhumidity"  
"gasmix::0.7xC02+0.3xAr/1.5atm/250K"  
"gasmix::BF3/2atm/25C/B_is_0.95_B10_0.05_B11"  
"gasmix::C02"  
"gasmix::He/1.64kgm3"  
"gasmix::He/10bar"  
"gasmix::He/He_is_He3/10bar"  
"gasmix::air"  
"gasmix::air/-10C/0.8atm/0.30relhumidity"
```



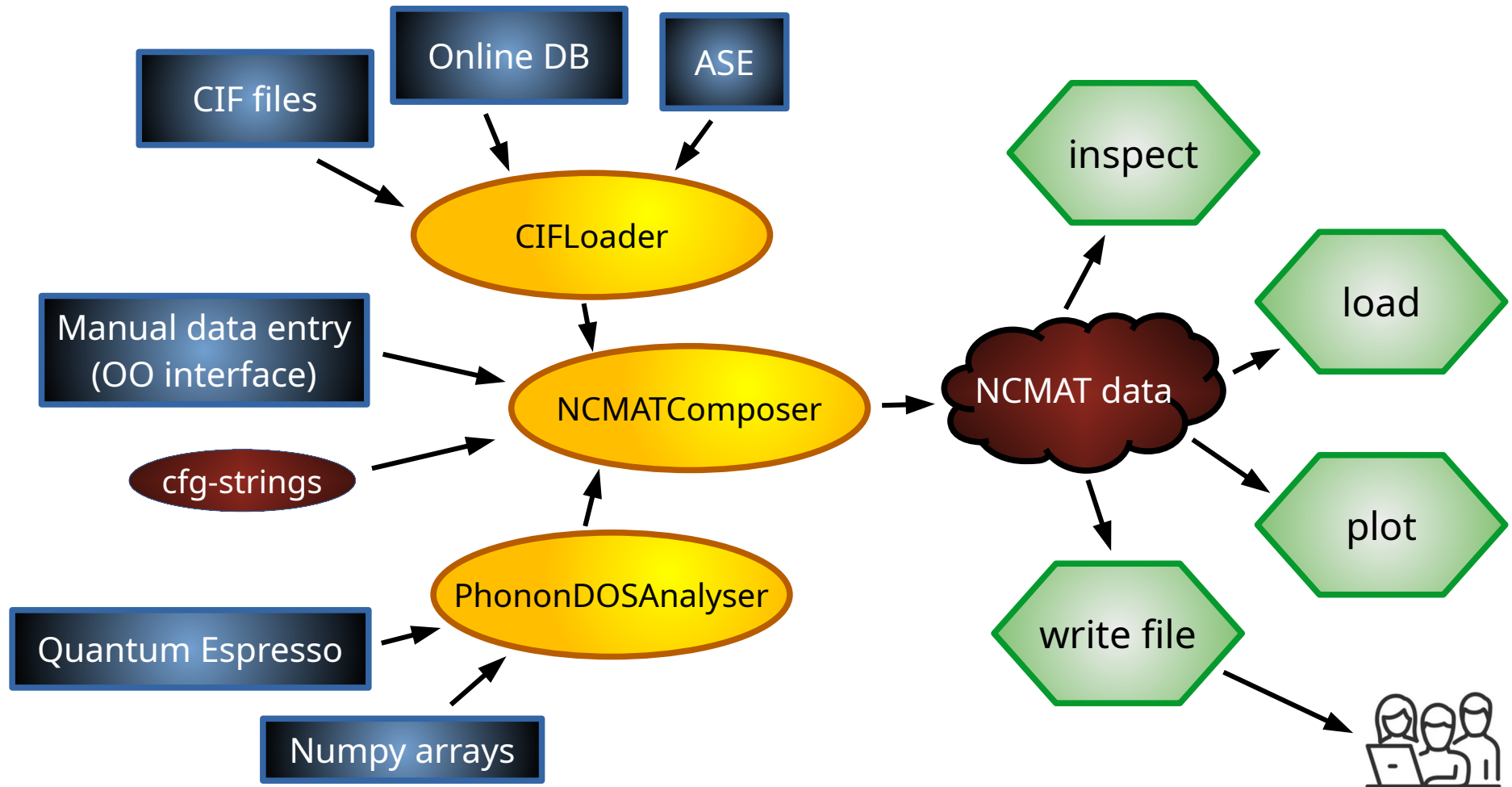
Python tools for material composition

The subject of several Jupyter notebooks.

NCrystal

Thermal Neutron Transport

- NCrystal includes Python tools for creating new materials.





Try it in the notebook:

“Data infrastructure and standard data library”



Jupyter tutorials at:

<https://github.com/mctools/ncrystal-notebooks/>



NCrystal physics algorithms

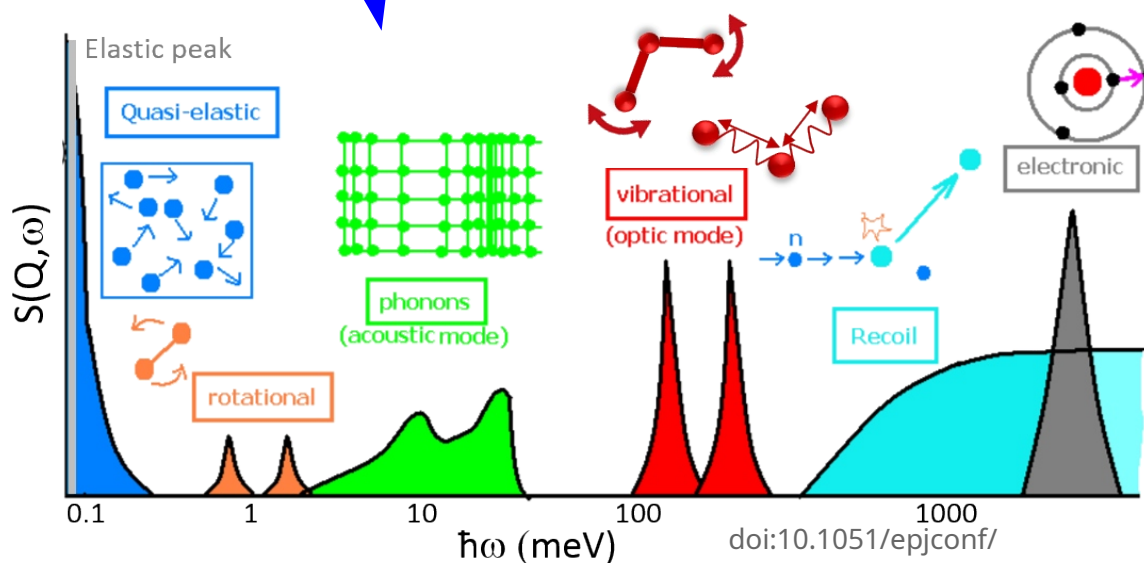
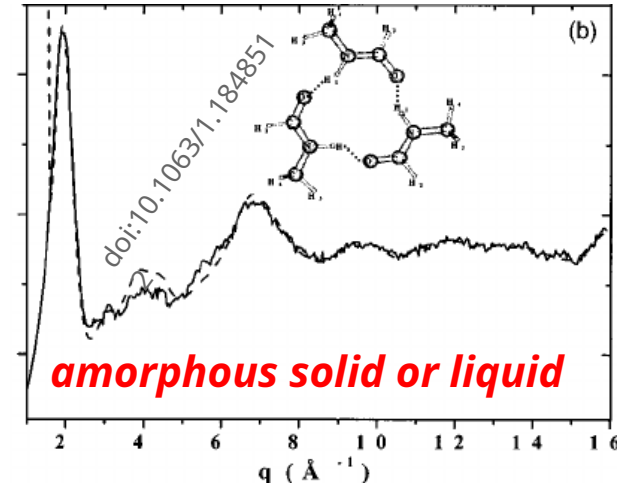
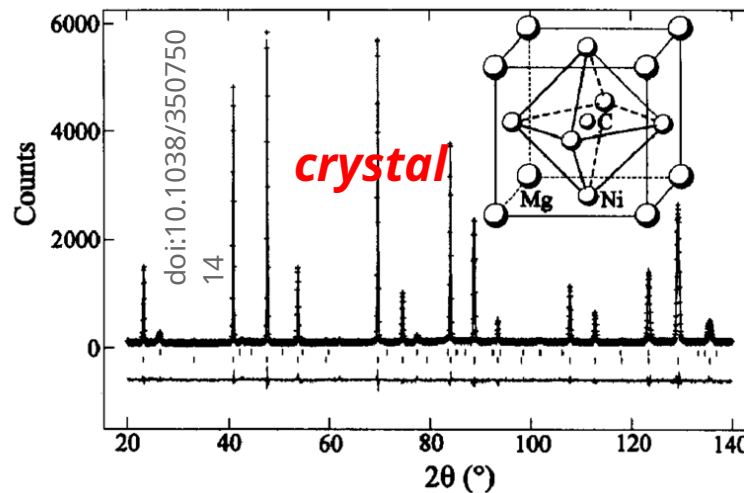
A small recap of Thermal Neutron scattering theory



Thermal neutron scattering: Rich connection to material structure

Thermal neutron wavelength
 \approx interatomic distances.
 \Rightarrow **Sensitive to atomic positions**

Thermal neutron energy
 \approx material energy levels
 \Rightarrow **sensitive to material dynamics**

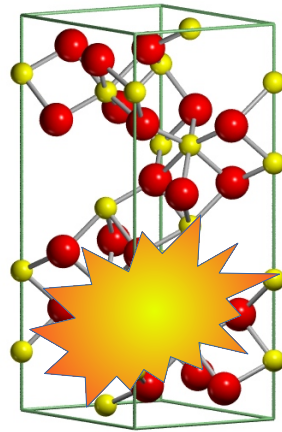
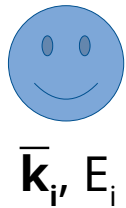


Thermal neutron scattering a uniquely useful tool for understanding material structure

On the flipside it is impossible to ignore material structure in MC simulations!

Thermal neutron scattering (ignoring polarisation)

~~POLARISATION~~



Normally OK to assume neutrons travel as free waves between interactions \Rightarrow simplifies analysis and Monte Carlo simulations!

$$\vec{k} = \vec{p}/\hbar, \quad \vec{q} \equiv \vec{k}_f - \vec{k}_i, \quad \Delta E \equiv E_f - E_i \equiv -\hbar\omega$$

$$\lambda = 2\pi/k, \quad 2E = m_n v^2 = p^2/m_n = \hbar^2 k^2/m_n$$

Probability to scatter to given $\bar{\mathbf{k}}_f$ given by differential cross section:

$$\frac{d^2\sigma_{\vec{k}_i \Rightarrow \vec{k}_f}}{d\Omega_f dE_f} = \frac{k_f}{k_i} \frac{1}{2\pi\hbar} \sum_{j,j'=1}^N b_j b_{j'} \int_{-\infty}^{\infty} dt \langle e^{-i\vec{q}\cdot\vec{R}_{j'}(0)} e^{i\vec{q}\cdot\vec{R}_j(t)} \rangle e^{-i\omega t}$$

N nuclei in target system

$S(\vec{q}, \omega)$

Scattering length of j th nucleus
(depends on isotope & spin state)

Correlate position of nucleus j at time 0 with position of nucleus j' at time t .

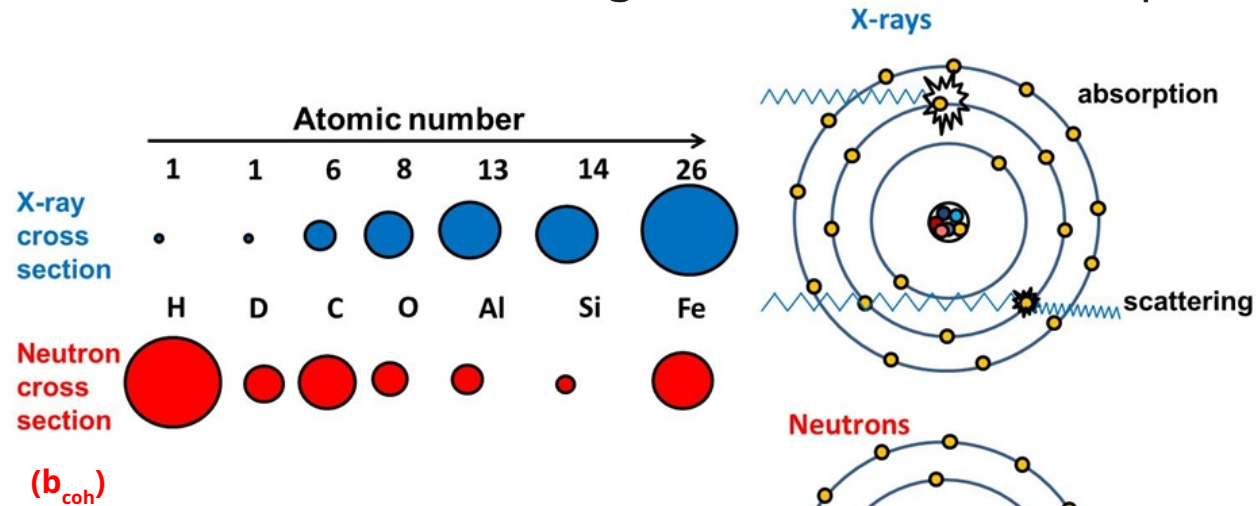
\Rightarrow Neutron X.S. depends on material structure!!

Scattering function
Depends on layout and dynamics of target particles.
Does not depend on state of incident neutron.

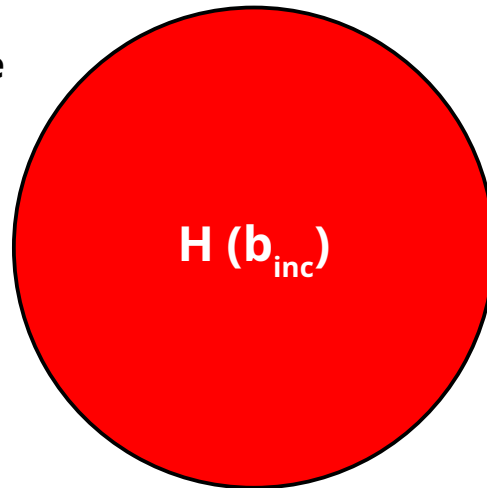
Scattering cross section depends on interference from scattering on different atoms, not just sum of 1-atom scatterings!!

Coherent scat. len. (b_{coh}) for select elements

X-ray strength increases with Z, neutron strength various across isotopes:



Note: hydrogen has huge *incoherent* scat. len. (b_{inc}):



→ Neutron scattering sensitive to structure which is otherwise inaccessible to x-rays.
→ Sample deuteration (H→D) allows tuning hydrogen scattering strength

image from <http://worldsciencereport.blogspot.com/2018/05/neutron-scattering.html>

Split in coherent / incoherent

NB: This is unique to neutrons, absent for x-ray scattering!

Most target systems can be split into statistically equivalent subsystems (e.g. unit cells for crystals). Average contribution per sub-system:

$$S(\vec{Q}, \omega) \equiv \frac{1}{2\pi\hbar} \sum_{j,j'=1}^N \overline{b_j b_{j'}} \int_{-\infty}^{\infty} dt \langle j', j \rangle e^{-i\omega t}$$

Average shorthand for $\langle e^{-i\vec{Q}\cdot\vec{R}_{j'}(0)} e^{i\vec{Q}\cdot\vec{R}_j(t)} \rangle$

(only nuclear charge (Z) important for structure, not isotope/spin state)

Using $\overline{b_j b_{j'}} = \begin{cases} \overline{b_j} \cdot \overline{b_{j'}}, & \text{for } j \neq j' \\ \overline{b_j^2}, & \text{for } j = j' \end{cases}$

and reordering terms:

$$S(\vec{Q}, \omega) = S_{\text{coh}}(\vec{Q}, \omega) + S_{\text{inc}}(\vec{Q}, \omega)$$

$$S_{\text{coh}}(\vec{Q}, \omega) \equiv \frac{1}{2\pi\hbar} \sum_{j,j'=1}^N \overline{b_j} \cdot \overline{b_{j'}} \int_{-\infty}^{\infty} dt \langle j', j \rangle e^{-i\omega t}$$

def $\equiv \overline{b_{\text{coh}}}$

$$S_{\text{inc}}(\vec{Q}, \omega) \equiv \frac{1}{2\pi\hbar} \sum_{j=1}^N \left(\overline{b_j^2} - (\overline{b_j})^2 \right) \int_{-\infty}^{\infty} dt \langle j, j \rangle e^{-i\omega t}$$

def $\equiv (\overline{b_{\text{inc}}})^2$

Coherent:

- Keep pair-correlations as in full $S(q,w)$
- Plug in per-element scat. lengths, which are the *averages* of isotopic/spin scat lens

Incoherent:

- No pair-correlation, no interference! (but still *indirect* dep. on mat. structure!)
- Just sum up separate contributions.
- Plug in per-element scat. lengths which are the *variances* of isotopic/spin scat lens

Always 0 in X-ray scattering!

Elastic versus inelastic scatterings

(in the sense of $\Delta E=0$ and $\Delta E \neq 0$)

- Mathematically speaking, elastic scattering means factors of delta-functions: $\delta(\Delta E)$
- $\delta(\Delta E)$ appears as result of static (i.e. time-independent) correlations between atomic positions:

$$S(\vec{Q}, \omega) \equiv \frac{1}{2\pi\hbar} \sum_{j,j'=1}^N \overline{b_j b_{j'}} \int_{-\infty}^{\infty} dt \langle j', j \rangle e^{-i\omega t}$$

$\langle e^{-i\vec{Q}\cdot\vec{R}_{j'}(0)} e^{i\vec{Q}\cdot\vec{R}_j(t)} \rangle$
(positional pair-correlations)

$\int_{-\infty}^{\infty} dt e^{-i\omega t} = 2\pi\hbar\delta(\hbar\omega) = 2\pi\hbar\delta(E_f - E_i)$

Fourier transform of static term gives δ -function in energy

Static correlations between atomic positions, and thus $\Delta E=0$ scatterings is a feature of solid materials (crystalline or amorphous).

Does not strictly speaking occur in liquids or gasses, although correlations in such might give rise to "quasi-elastic" scatterings peaking around $\Delta E=0$.

In summary: four $S(\bar{q},\omega)$ components

$$S(\bar{q},\omega) = S_{\text{coh,inel}}(\bar{q},\omega) + S_{\text{inc,inel}}(\bar{q},\omega) + S_{\text{coh,el}}(\bar{q},\omega) + S_{\text{inc,el}}(\bar{q},\omega)$$

solid systems only

Depending on material and neutron energy, any of these four components can dominate!

For isotropic materials: $S(\bar{q},\omega) \rightarrow S(q,\omega)$, allowing to treat scattering via 2D function (*scattering kernels*).

In practice, only inelastic scattering is modelled via 2D scattering kernels. Elastic scattering involves delta-functions and is best described by dedicated algorithms.

NCrystal elastic physics algorithms



$S_{\text{coh,el}}(\vec{q}, \omega)$ in crystals: Bragg diffraction!

Microscopic scatter function:

$$S_{\text{coh}}^{\text{el}}(\vec{Q}, \omega) = \frac{(2\pi)^3 \delta(\hbar\omega)}{V_{\text{uc}}} \sum_{hkl} \delta(\vec{Q} - \vec{\tau}_{hkl}) |F(\vec{\tau}_{hkl})|^2$$

sum over "crystal planes" $F(\vec{Q}) \equiv \sum_i \bar{b}_i e^{-W_i(\vec{Q})} e^{i\vec{Q} \cdot \vec{p}_i}$
plane normal with magnitude $2\pi/d_{hkl}$ unit cell structure factor depends on layout of atoms in unit cell
unit cell volume unit cell structure factor depends on layout of atoms in unit cell $2W = \delta^2 q^2$, $\delta = \text{atomic displacement}$

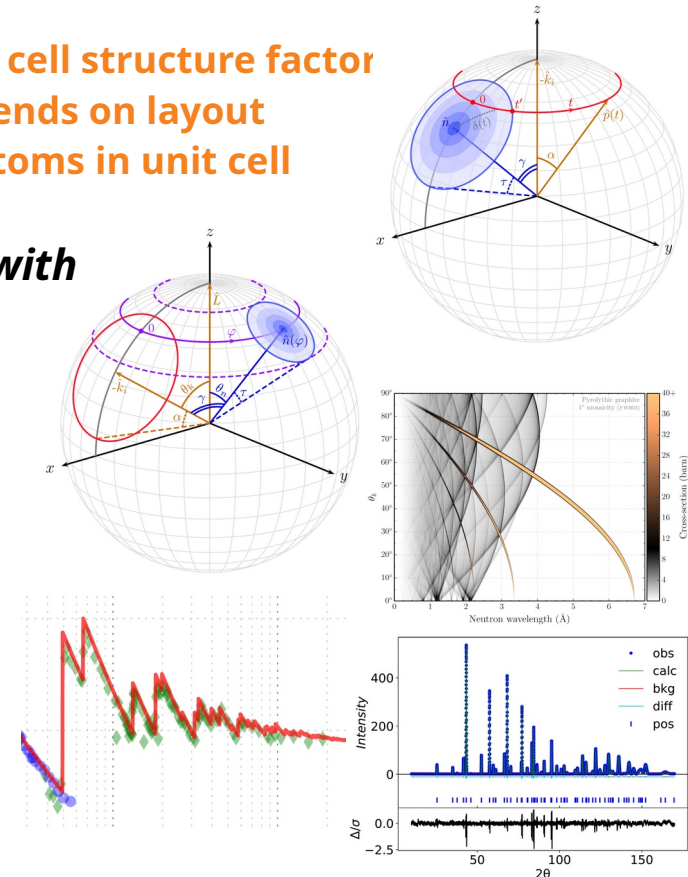
Macroscopic values are found from convoluting microscopic values with crystal grain distributions → geometrical problem!

Supported geometries in NCrystal:

- Completely disoriented layout ("powder approximation")
- Gaussian deviations from completely oriented ("Mosaic single crystals")
- Layered crystals ("rotated mosaic single crystals", pyrolythic graphite)

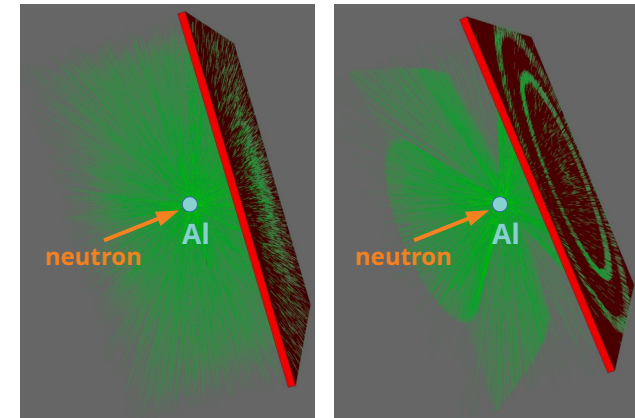
Not supported yet:

- Bent/deformed crystals, corrections for very small grain sizes.
- Textured crystals (as in most metals/polycrystals). But powder approximation OK for many use-cases! People have expressed interest in improving this though, get in touch if you want to contribute :-)

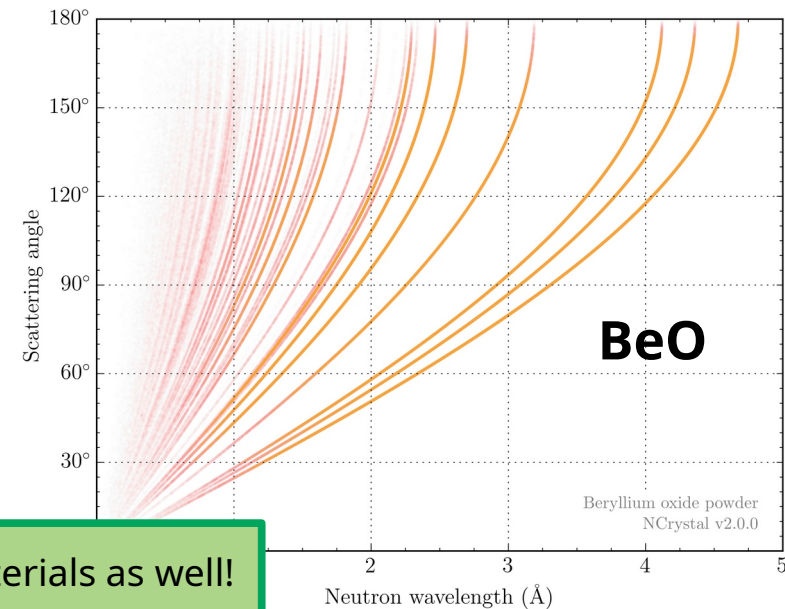
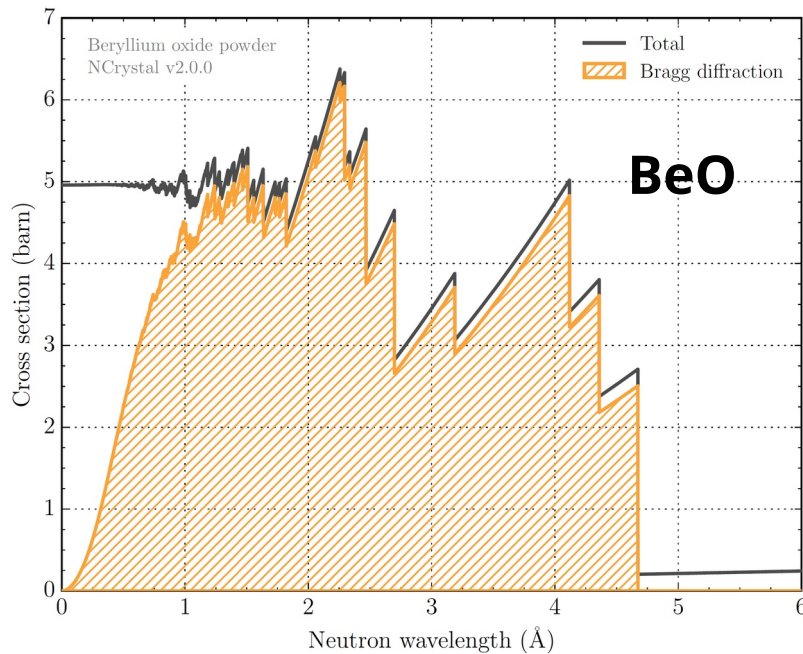


Bragg diffraction in powders (and texture-free polycrystals)

Based on provided HKL planes with d-spacings and structure factors, the implementation is straight-forward.
Care is taken to be extremely fast $O(10\text{ns}/\text{call})$, even in case of huge number of planes.
Currently no texture/grain-size effects.



Geant4 free-gas model (wrong MFP, wrong scatter) Geant4 with NCrystal \Rightarrow Debye-Scherrer cones



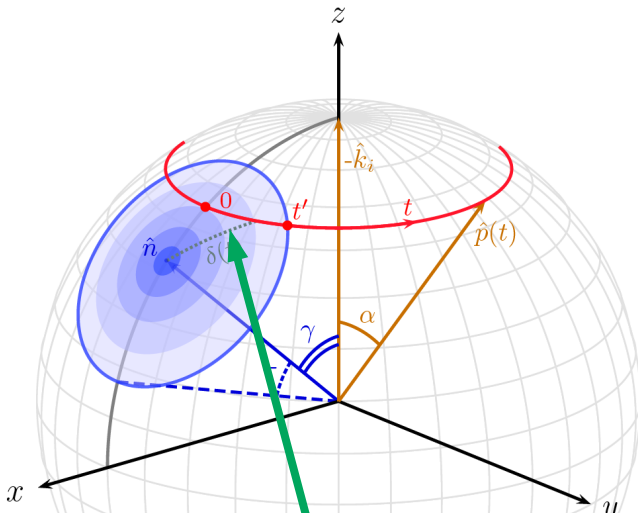
There is interest in extending this to textured materials as well!

Single Crystals with Gaussian mosaicity



Thermal Neutron Transport

Can model monochromators, analysers, filters, samples
Handles also large mosaicities and backscattering!



The tricky part* is the integration of mosaic density along circle of Bragg condition.

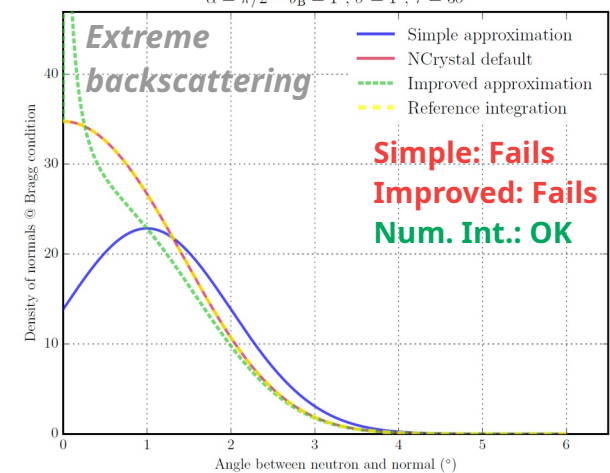
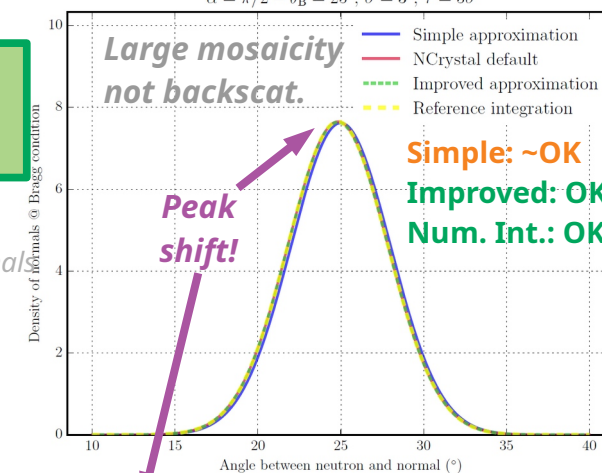
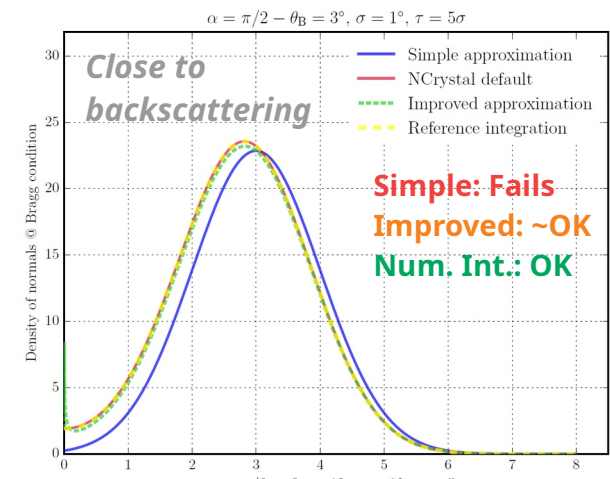
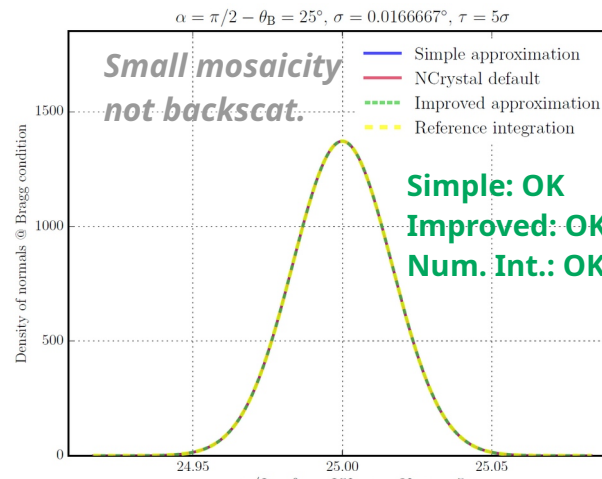
*: Once contributing normals have been identified.

Simple closed-form approx. valid for small mosaicity (and not backscattering):

$$\sigma_{\text{Bragg}}(\alpha, \gamma) = Q \times \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{1}{2}\frac{\delta_0^2}{\sigma^2}\right] \times \text{erf}\left[\frac{\sqrt{\tau^2 - \delta_0^2}}{2\sigma^2}\right] \times \sqrt{\frac{\sin \alpha}{\sin \gamma}} \times \frac{N}{1/(2\pi\sigma^2)}$$

$$\delta_0 = |\alpha - \gamma|$$

Our improved form extends validity to much larger mosaicities

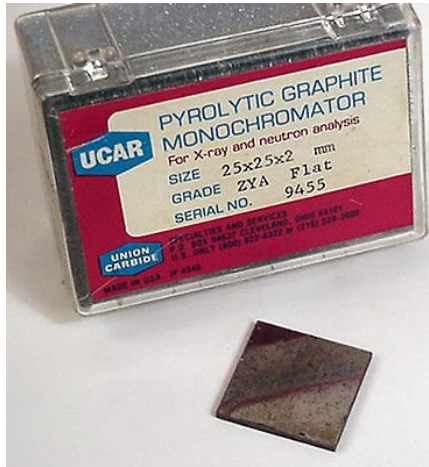


Code picks appropriate method from:

- Our closed form approximation
- Full numerical integration

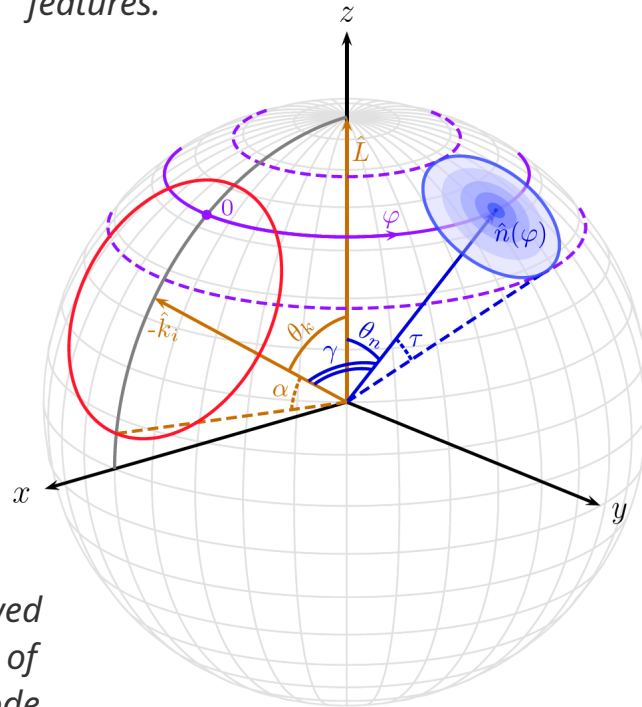
Special anisotropic model for Pyrolytic Graphite

PG often used as filters, monochromator, analyser



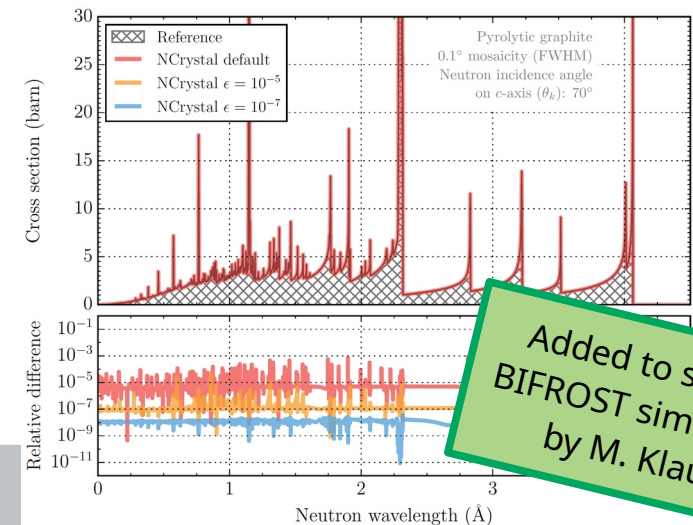
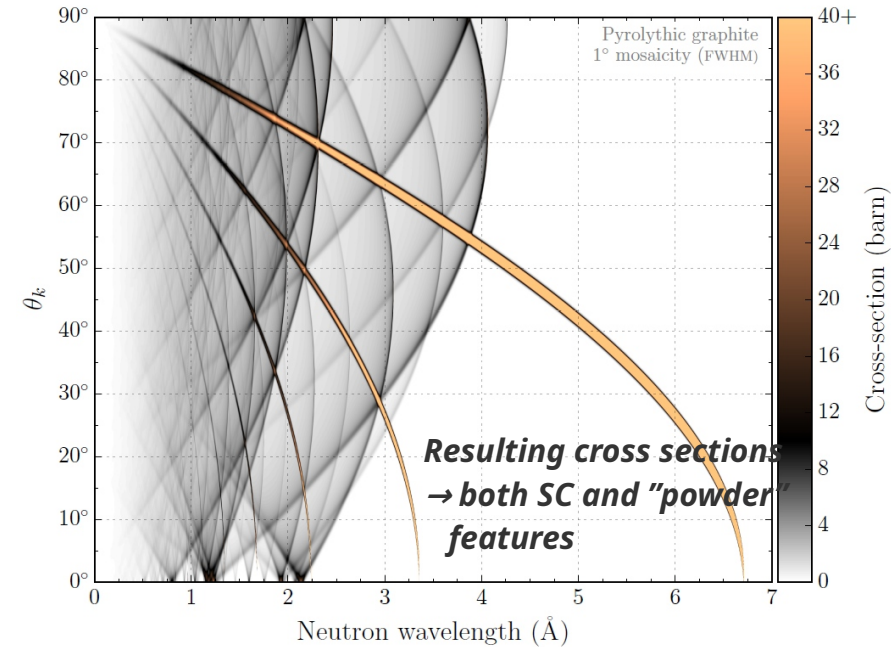
Layered crystal model:

- Usual Gaussian mosaic distribution is "smeared out" by rotation
- Exhibits both single-crystal and powder features.



Features:

- Cross-sections determined by efficient pre-search followed by fast Romberg integration of non-layered single crystal code.
- Features realistic transmission probabilities and multiple-scattering effects (incl. "zig-zag walk")

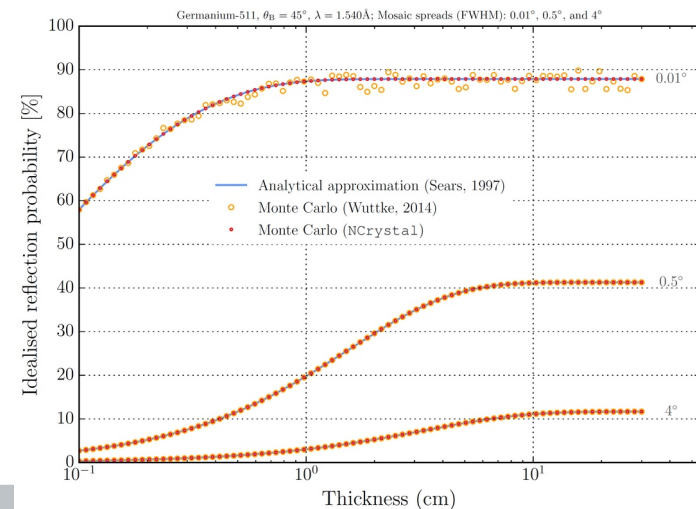
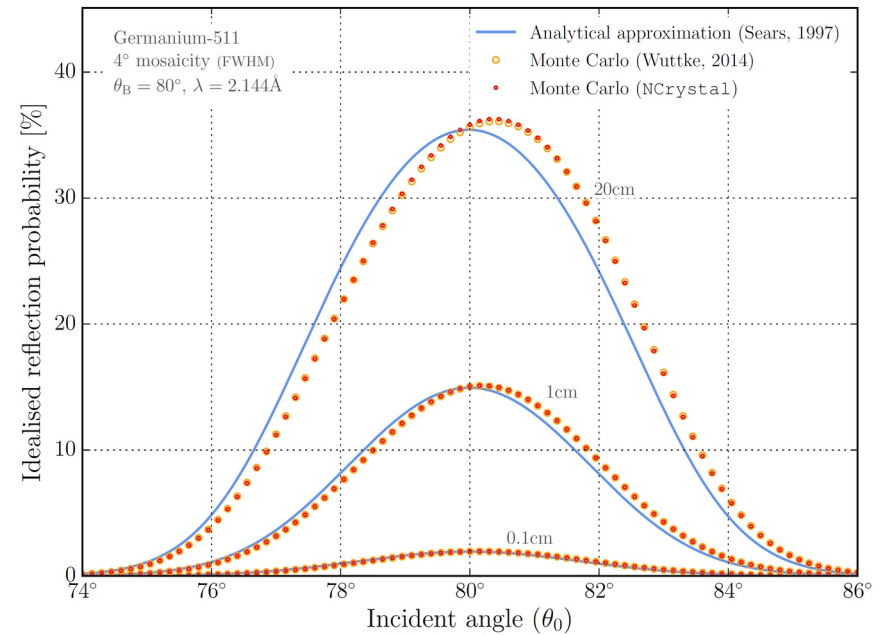
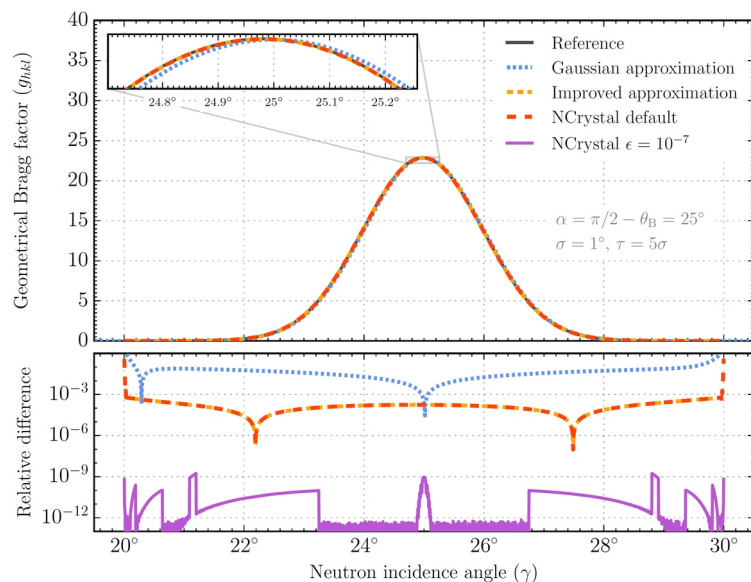


Added to support BIFROST simulations by M. Klausz.

Single crystal model validated

Validation includes:

- Against existing codes (Wuttke2014) or analytical results (Sears1997) in their domains of validity.
- Against (very) slow but simple+precise implementation (using mpmath high-precision math module)
- Technical validations (zig-zag, "powdered")

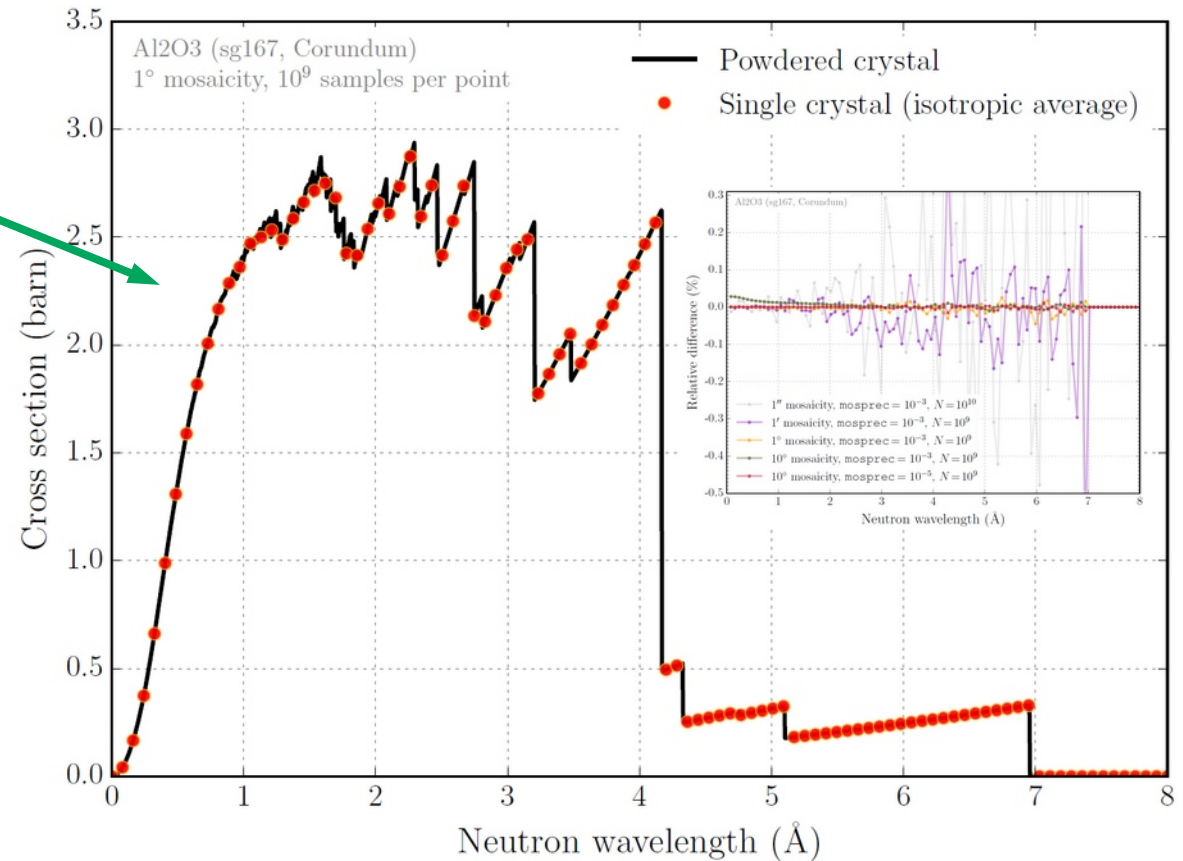


Technical checks for consistency of single crystal codes (should also hold for texture models)

In principle an isotropically illuminated single crystal should on average give powder-like cross-sections.

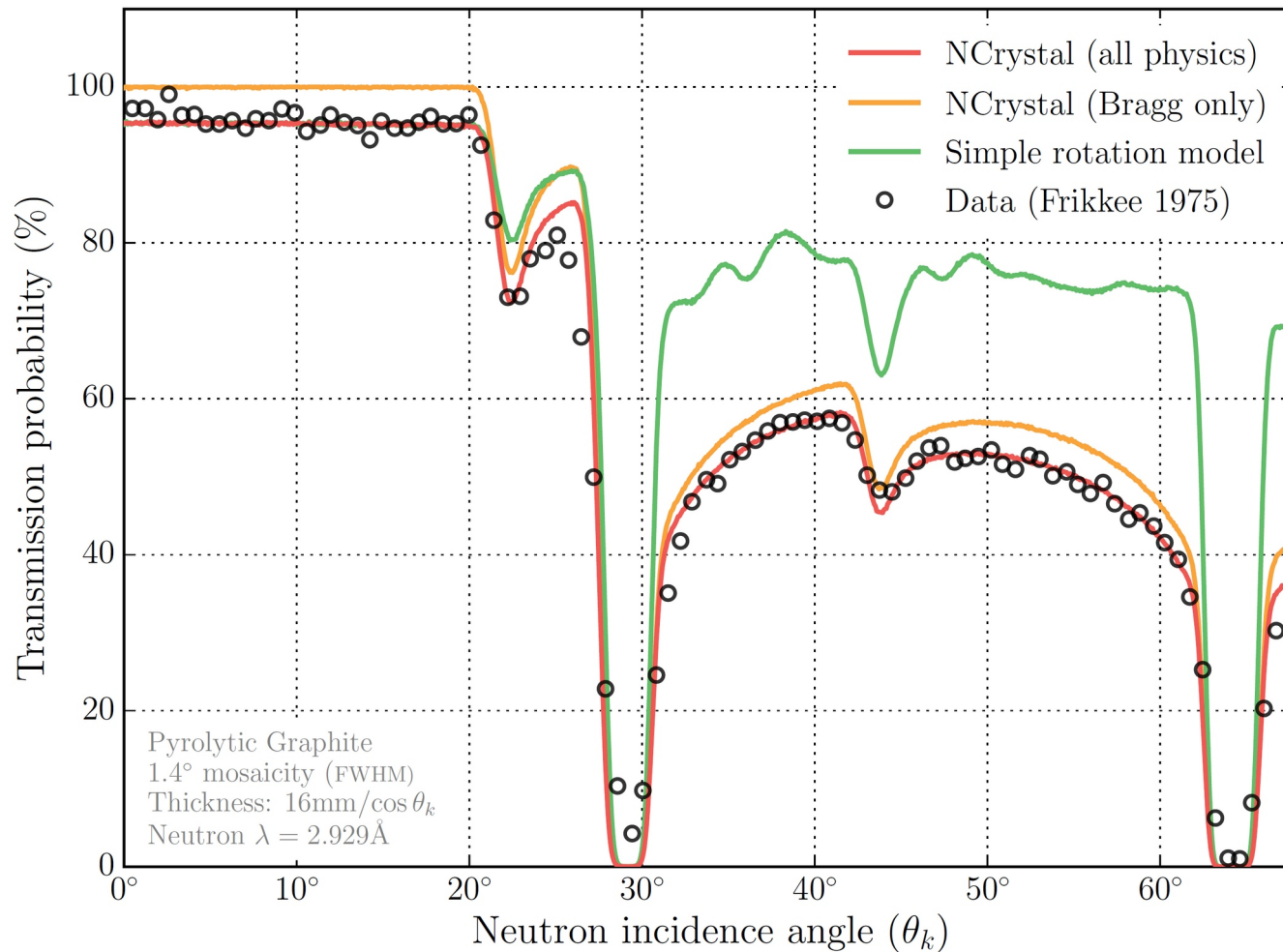
In practice, a lot of edge-cases and details have to be treated correctly in the SC code before this happens!

Another check is that consistent SC codes should provide "zig-zag walk"



Thanks to the DMSC cluster for help with this brute force validation.

Can reproduce PG transmission spectra!

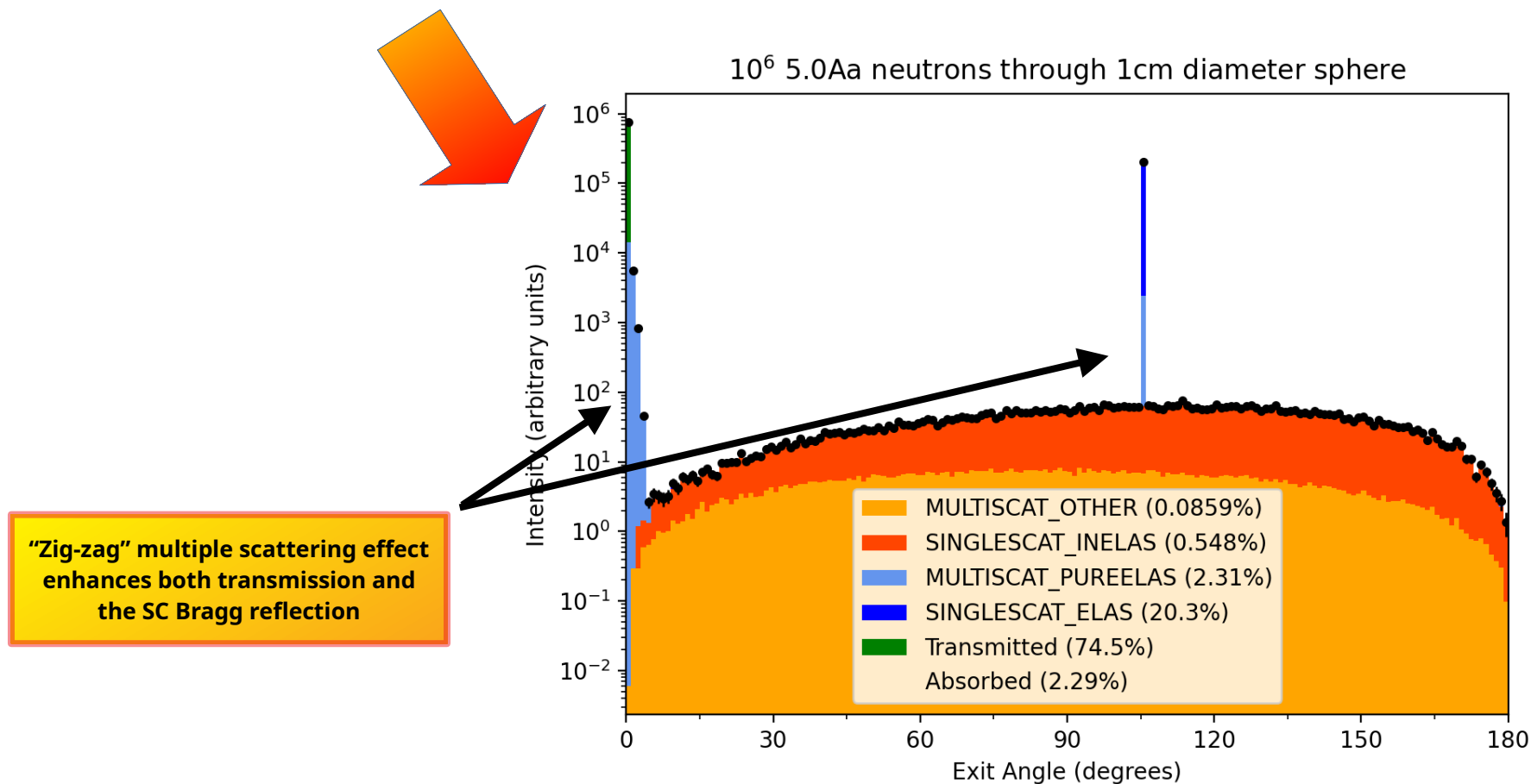


Validation also includes:

- Comparison against (very very) slow but simple+precise implementation.
- Verification that cross section maxima structure matches predictions (Frikkee1975).
- Technical validations (zig-zag, "powdered").

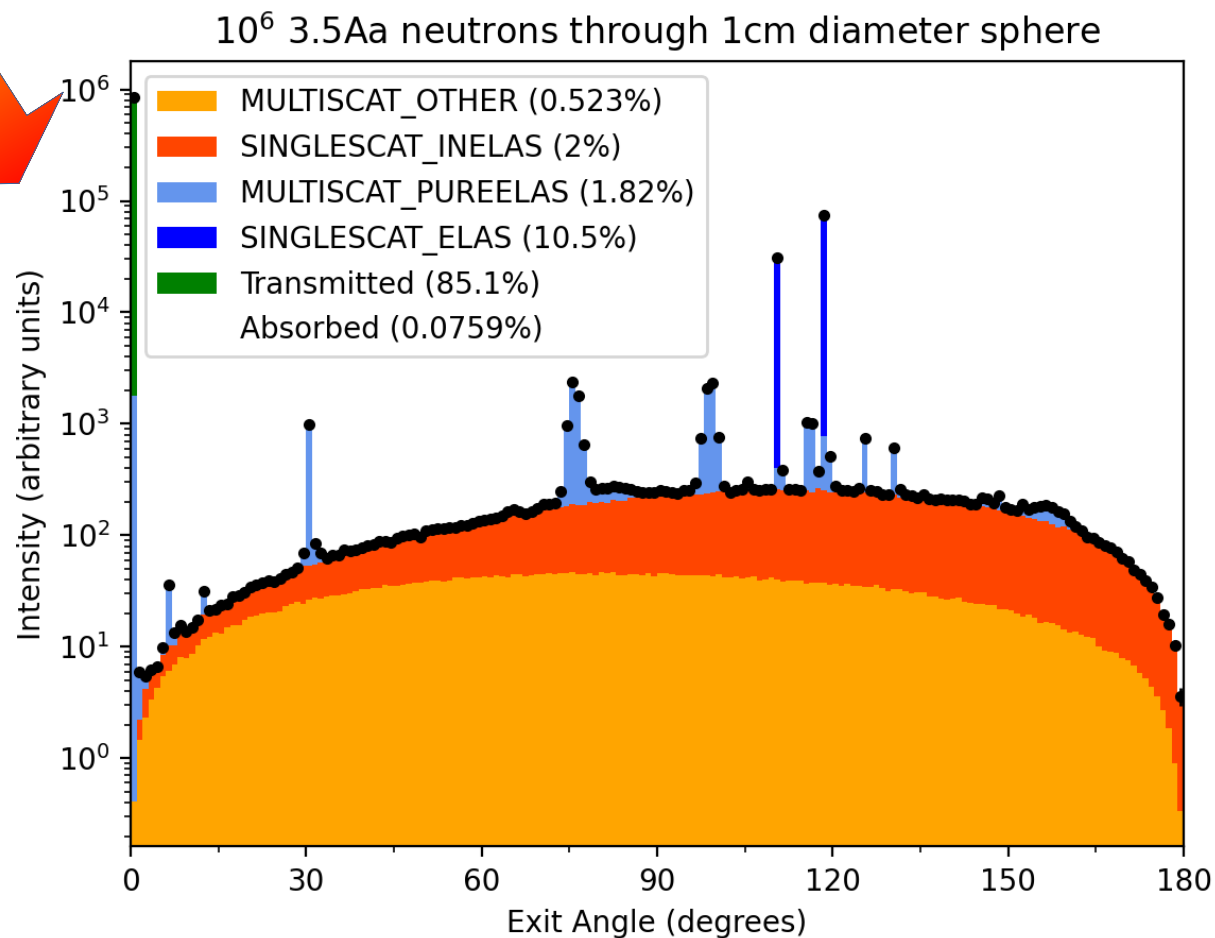
Embedded "Mini MC" also supports single crystals (here Si111 monochromator)

```
$> nctool --mc 5.0Aa 1cm \  
"Si_sg227.ncmat;dir1=@crys_hkl:1,1,1@lab:0,3,1;dir2=@crys_hkl:0,0,1@lab:0,0,1;dirtol=180deg;mos=1deg"
```



Pyrolytic graphite in "Mini MC"

```
$> nctool --mc 3.5Aa 1cm ""C_sg194_pyrolytic_graphite.ncmat
;dir1=@crys_hkl:0,0,2@lab:0,3,1;mos=0.2deg;
;dir2=@crys_hkl:1,1,1@lab:0.1,0,1;dirtol=180deg""
```



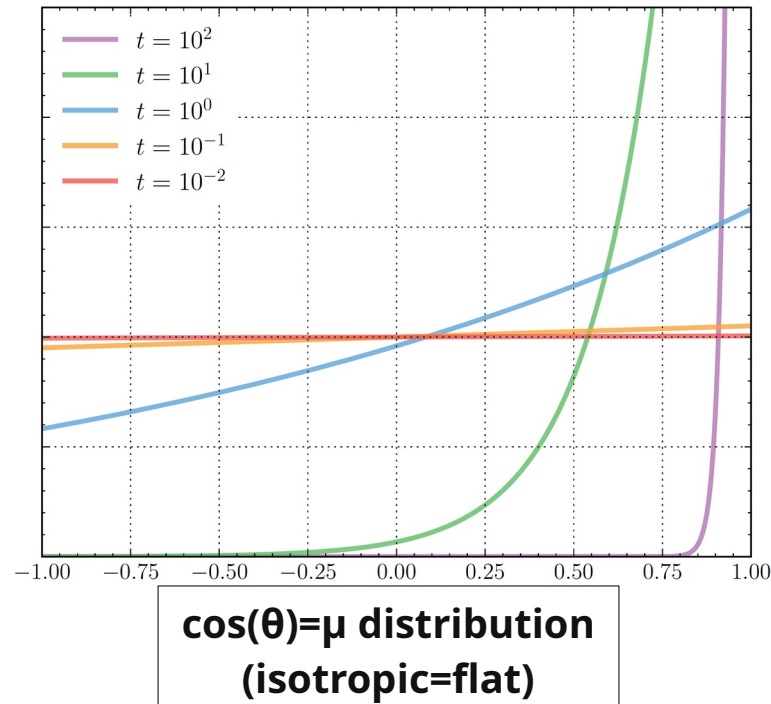
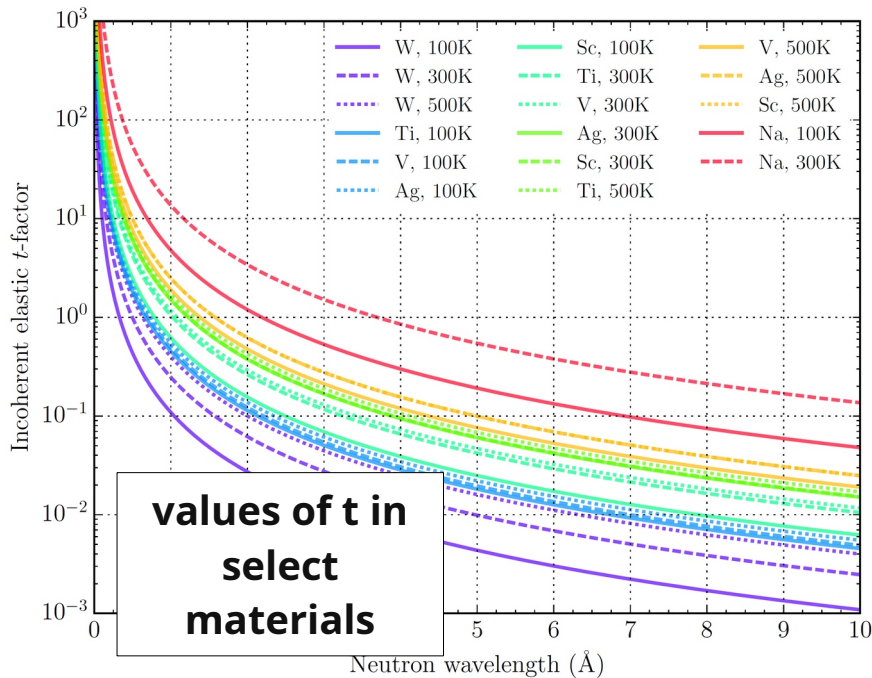
Incoherent-elastic scattering

$$\frac{d\sigma_{\vec{k}_i \rightarrow \vec{k}_f}^{\text{inc,el}}}{d\Omega_f} = \frac{1}{N} \sum_{j=1}^N \frac{\sigma_j^{\text{inc}}}{4\pi} e^{-2W_j(\vec{Q})} \longrightarrow \sigma^{\text{inc,el}}(k) = \sigma_{\text{inc}} \frac{1 - \exp(-t)}{t}$$

Get Debye-Waller factors (or δ^2) from phonon DOS (or Debye temp.).

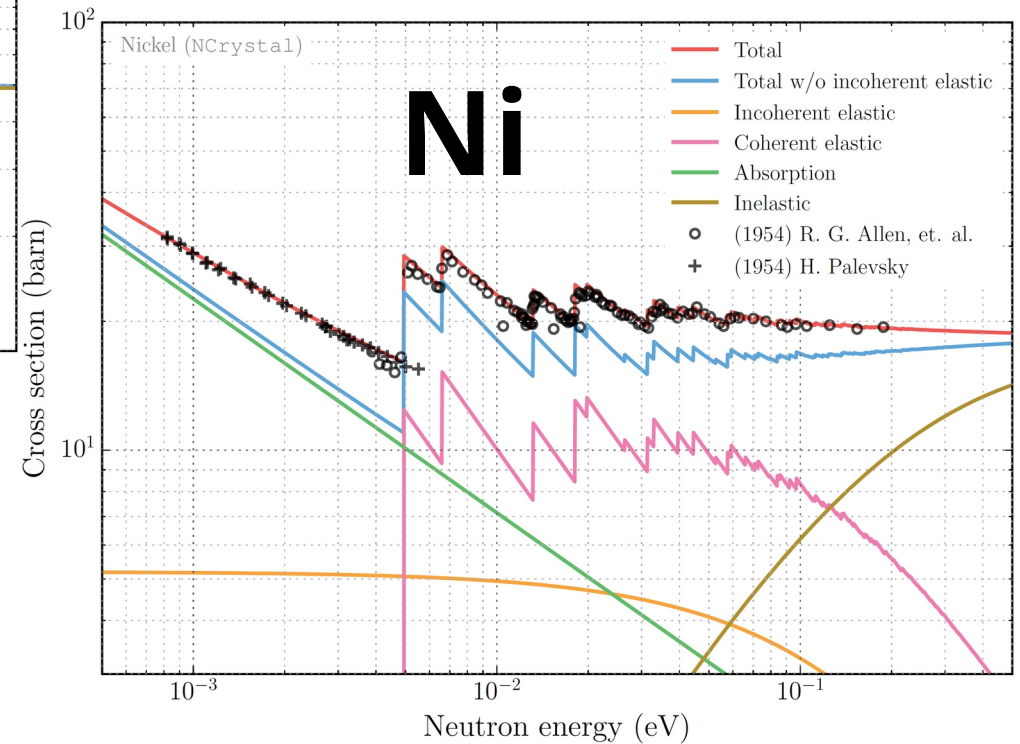
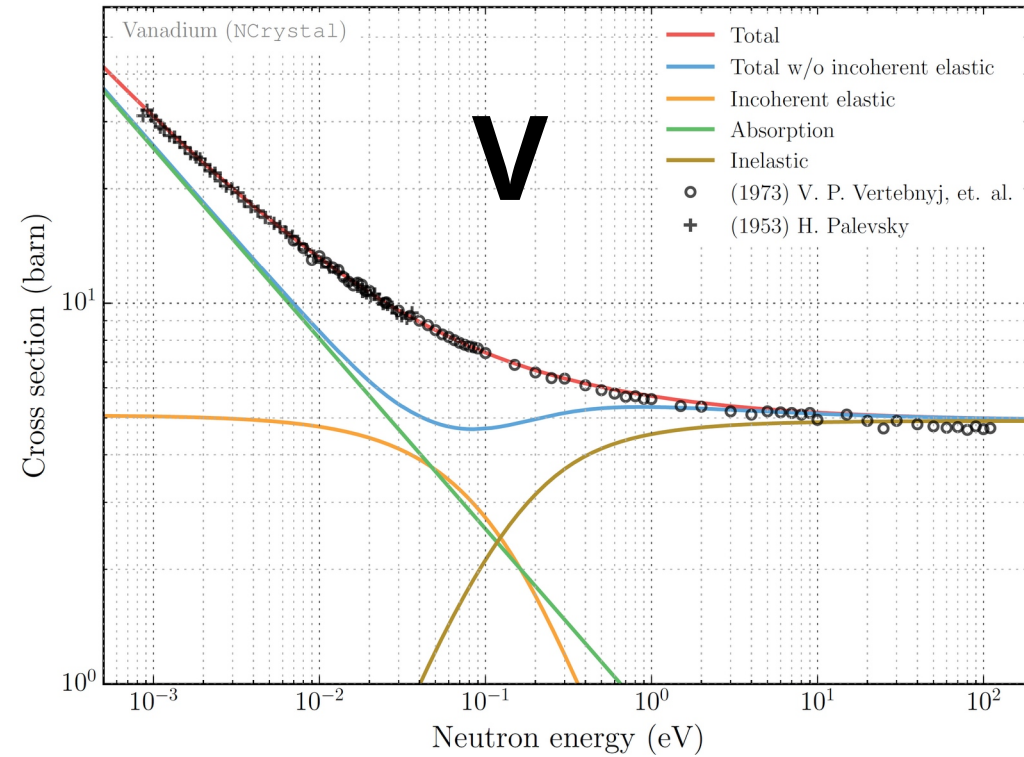
$$P(\mu) = N_t \exp\left(\frac{t\mu}{2}\right)$$

$$t \equiv (2k\delta)^2 = \left(\frac{4\pi\delta}{\lambda}\right)^2$$



→ Not always completely isotropic!!

Incoherent-elastic model → crucial for many materials





First half of the notebook: “Creating materials and the NCMATComposer”

(to “Specifying dynamic information”)

 **Jupyter tutorials at:**
<https://github.com/mctools/ncrystal-notebooks/>



NCrystal inelastic physics algorithms



Inelastic physics : Scattering kernels

$$\frac{d^2 \sigma_{\vec{k}_i \Rightarrow \vec{k}_f}}{d\Omega_f dE_f} = \frac{k_f}{k_i} S(\vec{Q}, \omega)$$

$$S(\vec{Q}, \omega) = S_{\text{coh}}(\vec{Q}, \omega) + S_{\text{inc}}(\vec{Q}, \omega)$$

$$S_{\text{coh}}(\vec{Q}, \omega) \equiv \frac{1}{2\pi \hbar} \sum_{j,j'=1}^N \bar{b}_j \cdot \bar{b}_{j'} \int_{-\infty}^{\infty} dt \langle j', j \rangle e^{-i\omega t}$$

$$S_{\text{inc}}(\vec{Q}, \omega) \equiv \frac{1}{2\pi \hbar} \sum_{j=1}^N \left(\bar{b}_j^2 - (\bar{b}_j)^2 \right) \int_{-\infty}^{\infty} dt \langle j, j \rangle e^{-i\omega t}$$

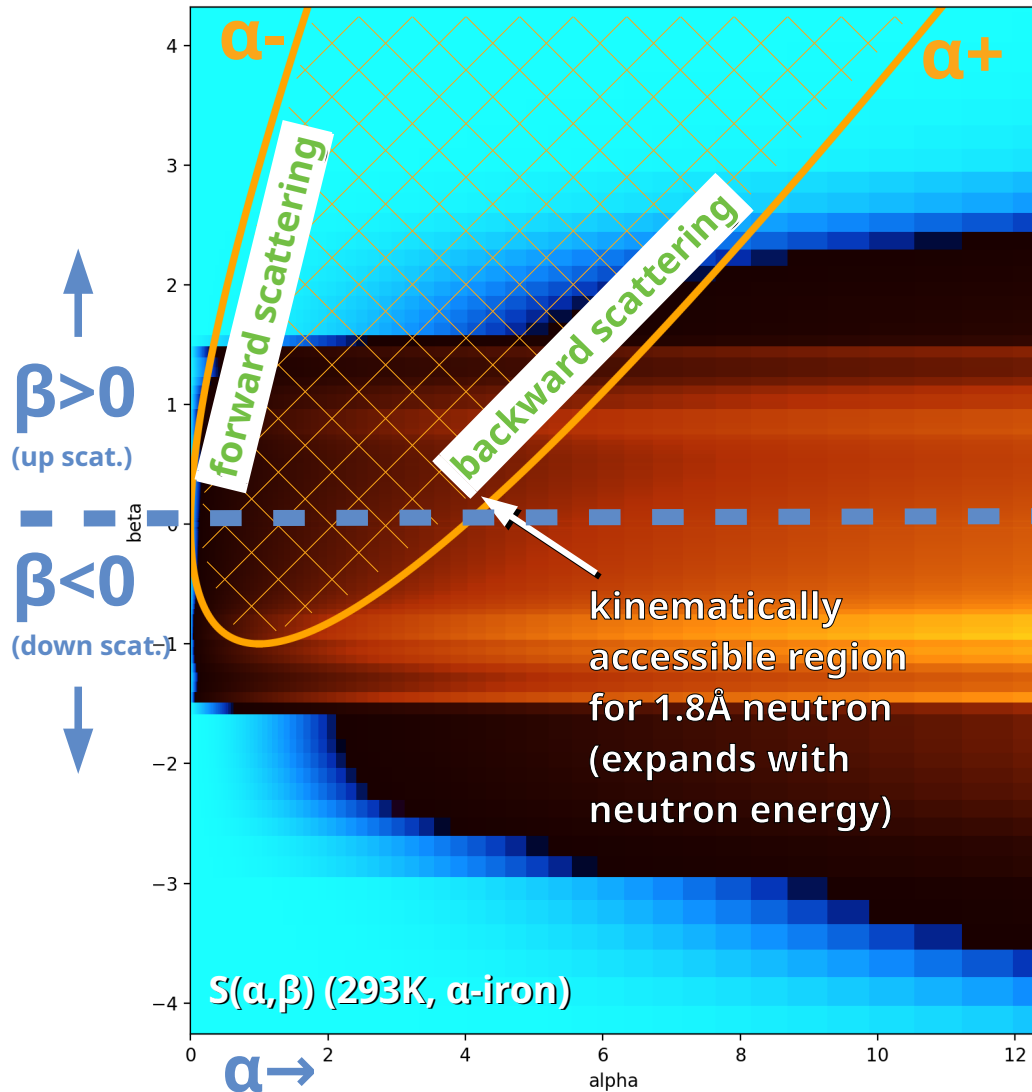
Under some assumptions $S(\vec{Q}, \omega)$ can be described with a single “smooth” 2D function (one per atom type):

- Elastic scattering is dealt with separately (as it is in NCrystal).
- *Isotropic material* (\vec{Q} dependency becomes scalar Q)
- *Incoherent approximation*: Off-diagonal entries in S_{coh} wash out when integrating over isotropic grain distribution, so $\text{shape}(S_{\text{coh}}) \approx \text{shape}(S_{\text{inc}})$.

Tabulate this function on a grid → **scattering kernel**.

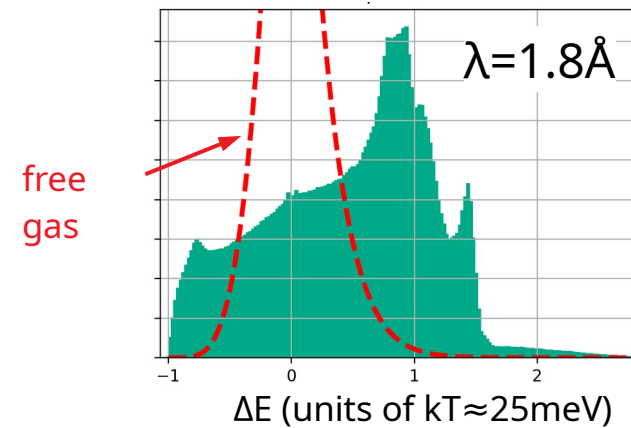
Scattering kernel and connection to neutron

$S(q, \omega) \sim S(\alpha, \beta)$; α : dimensionless q^2 , β : dimensionless ω ($\sim \Delta E$)



“Detailed balance”:
Boltzmann factor + identical strength of phonon absorption & emission \rightarrow Symmetry around $\beta=0$, given by $S(\alpha, -\beta) = \exp(\beta) \cdot S(\alpha, \beta)$

β -projection of kinematically accessible region \rightarrow energy transfer spectrum (green):



Formulation in dimensionless variables: α, β

(q, ω) preferred in neutron scattering community, (α, β) preferred in nuclear industry (incl. MCNP, ENDF, ...)

α : dimensionless q^2
 β : dimensionless ΔE

$$\beta = \frac{E_f - E}{kT} = -\frac{\hbar\omega}{kT}$$

$$\begin{aligned} \alpha &= \frac{\hbar^2}{2m_n kT} q^2 \\ &= \frac{E + E_f - 2\mu\sqrt{EE_f}}{kT} \quad \mu = \cos\theta_{\text{scat}} \\ &= \frac{2E}{kT} + \beta - 2\mu\sqrt{\frac{E}{kT} \left(\frac{E}{kT} + \beta\right)} \end{aligned}$$

Scattering lengths taken outside definition of S:

$$\frac{d^2\sigma}{dE_f d\Omega} = \sqrt{\frac{E_f}{E}} \frac{\sigma_b}{4\pi} \frac{S(\alpha, \beta)}{k_b T}$$

Total cross section, with explicit kinematic limits:

$$\sigma(E) = \frac{\sigma_b kT}{4E} \int_{-E/kT}^{\infty} \int_{\alpha_-(E, \beta)}^{\alpha_+(E, \beta)} S(\alpha, \beta) d\alpha d\beta$$

constant affects $\sigma(E)$,
but not (α, β)-sampling

neutron lose all its energy

$\mu = -1$, complete backwards scattering

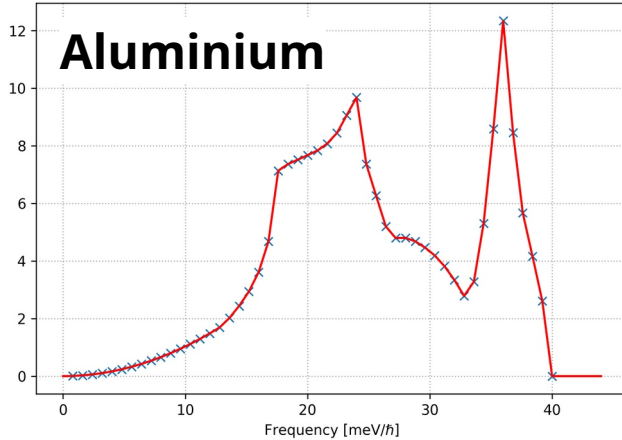
$\mu = +1$, complete forward scattering

$$\alpha_{\pm}(E, \beta) = \frac{2E}{kT} + \beta \pm 2\sqrt{\frac{E}{kT} \left(\frac{E}{kT} + \beta\right)}$$

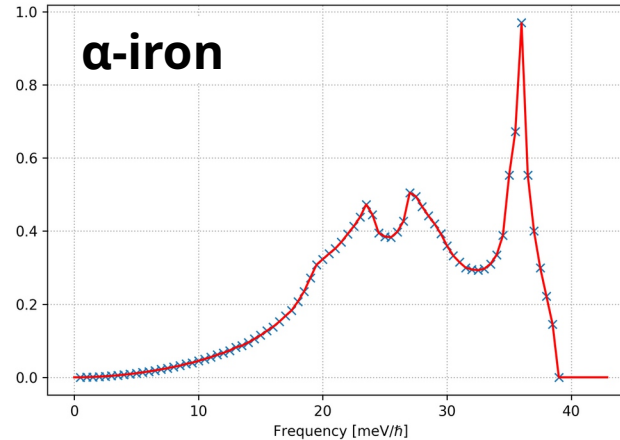
kinematically accessible region is a parabola in the (α, β)-plane

Solids: Scattering kernels are connected to phonon frequency spectrums (aka Vibrational Density Of States, VDOS)

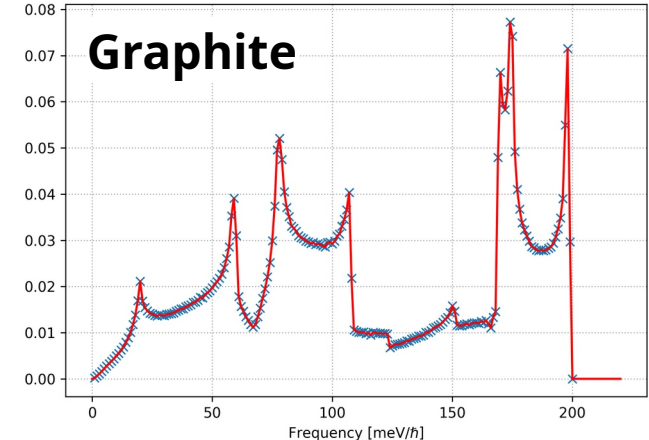
Al: VDOS



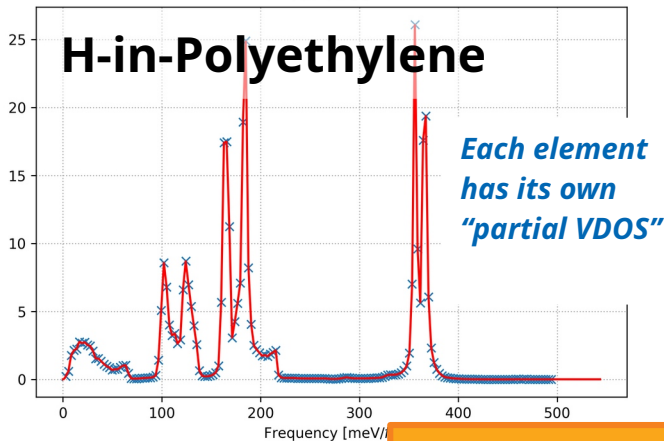
Fe: VDOS



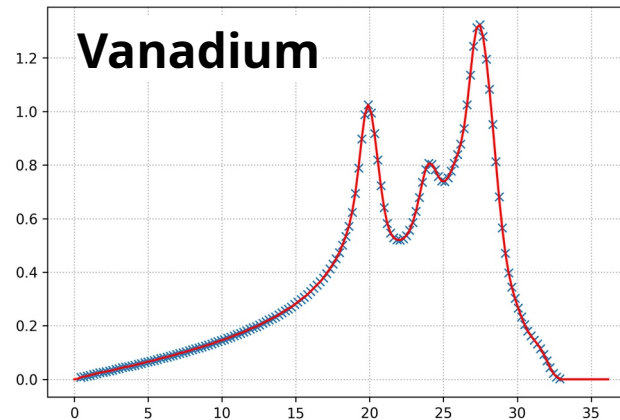
PG: VDOS



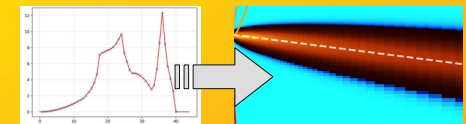
PE: VDOS



V: VDOS



NCrystal can expand VDOS to scattering kernels on-the-fly in O(100ms).



**Captures material structure info relevant for *inelastic* neutron scatterings (isotropic materials, incoherent approximation)
+ gives displacements (Debye-Waller factors) needed for *elastic* scatterings.**

Phonon spectrum (VDOS) sources

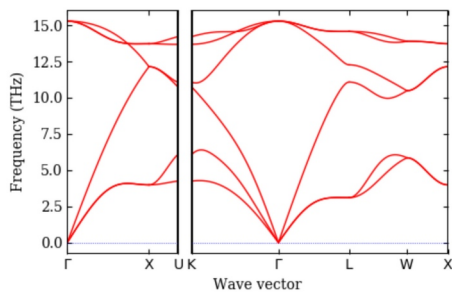
VDOS is not specific to neutrons!

→ Many resources exists

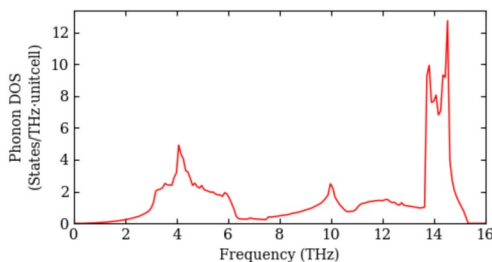
Materials id 149 / Si / Fd-3m (227)

- Date page updated: 2018-4-17
- Space group type: Fd-3m (227) / F 4d 2 3 -1d
- Number of formula units (Z): 8
- Phonon raw data: [mp-149-20180417.tar.gz](#)
- Link to Materials Project: <https://www.materialsproject.org/materials/mp-149/>

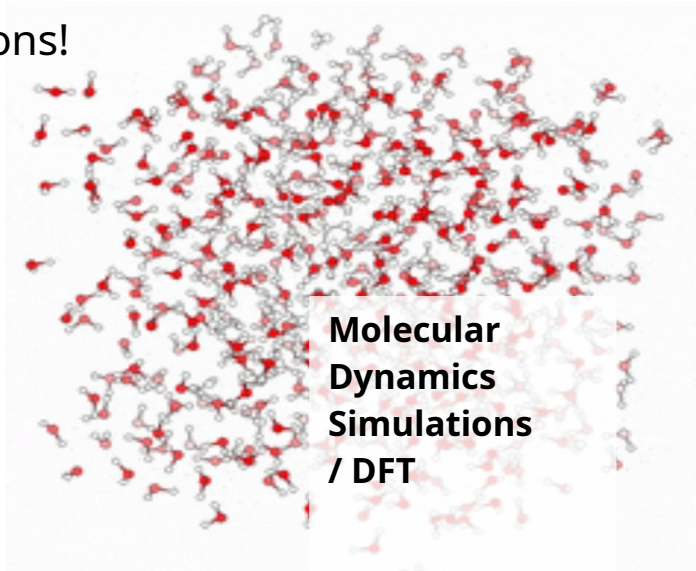
Phonon band structure



Phonon DOS



<http://phonondb.mtl.kyoto-u.ac.jp/>



**Molecular
Dynamics
Simulations
/ DFT**

Daive Campi's lectures at the 2023 HighNESS school contains more information:
<https://indico.ess.eu/event/3096/>



VDOS can also be measured experimentally...

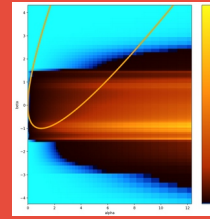
... or dug out from old research papers!

Or a combination, potentially using other SW (QuantumEspresso / VASP / phononpy / Oclimax / ...)

Many VDOS curves need a bit of processing and cleanup to be used.

This can be done in Python using the PhononDOSAnalyser class provided with NCrystal.

NCrystal has unique features for *using* scattering kernels

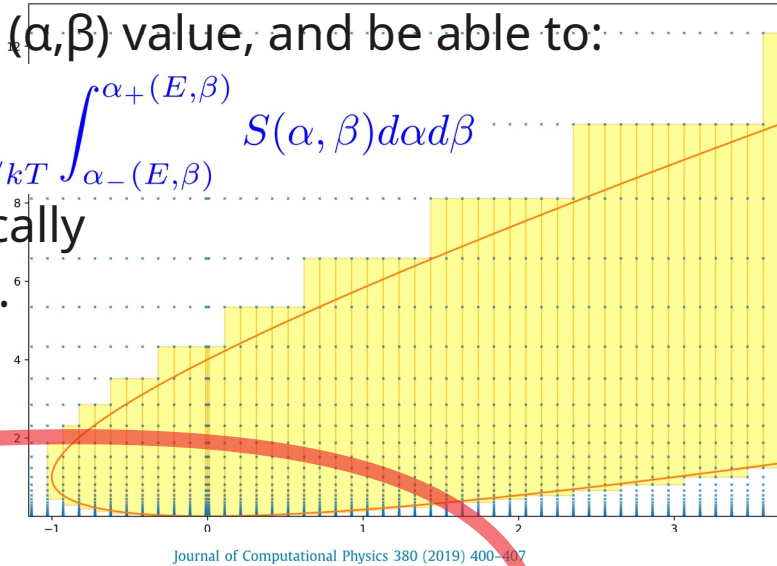


- Given $S(\alpha, \beta)$ values on a grid (α_i, β_i) and a neutron with energy, E , we must define suitable interpolation scheme to provide $S(\alpha, \beta)$ for any (α, β) value, and be able to:

1) Estimate scattering cross section:
$$\sigma(E) = \frac{\sigma_b kT}{4E} \int_{-E/kT}^{\infty} \int_{\alpha_-(E, \beta)}^{\alpha_+(E, \beta)} S(\alpha, \beta) d\alpha d\beta$$

2) Sample (α, β) values randomly within the kinematically accessible region, with density proportional to $S(\alpha, \beta)$.

- This must be done accurately and with reasonable computing resources! **Tricky part is sampling.**
- NCrystal has novel method for accurate+fast sampling, without ACE-like discretisation, with attention to near-endpoint sampling (crucial for ultra-cold neutron moderator studies).
- We have ideas to further improve this** (make it faster, remove remaining artifacts).



Contents lists available at [ScienceDirect](https://www.sciencedirect.com)
Journal of Computational Physics
www.elsevier.com/locate/jcp

Rejection-based sampling of inelastic neutron scattering

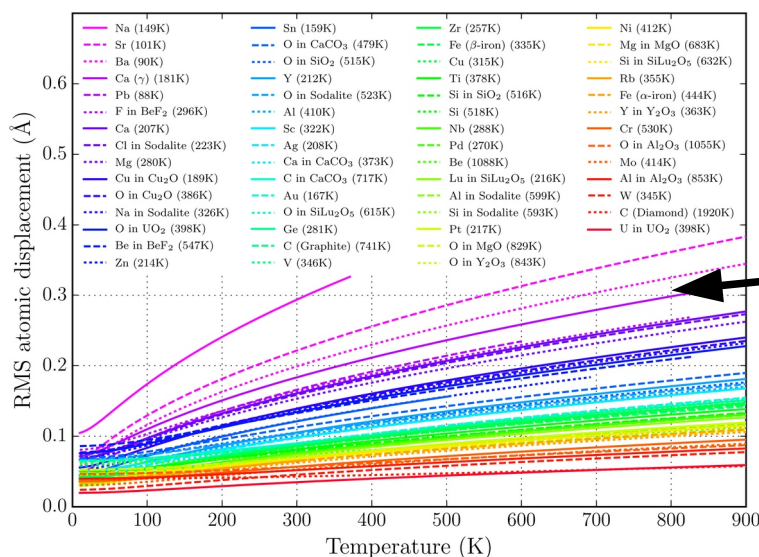
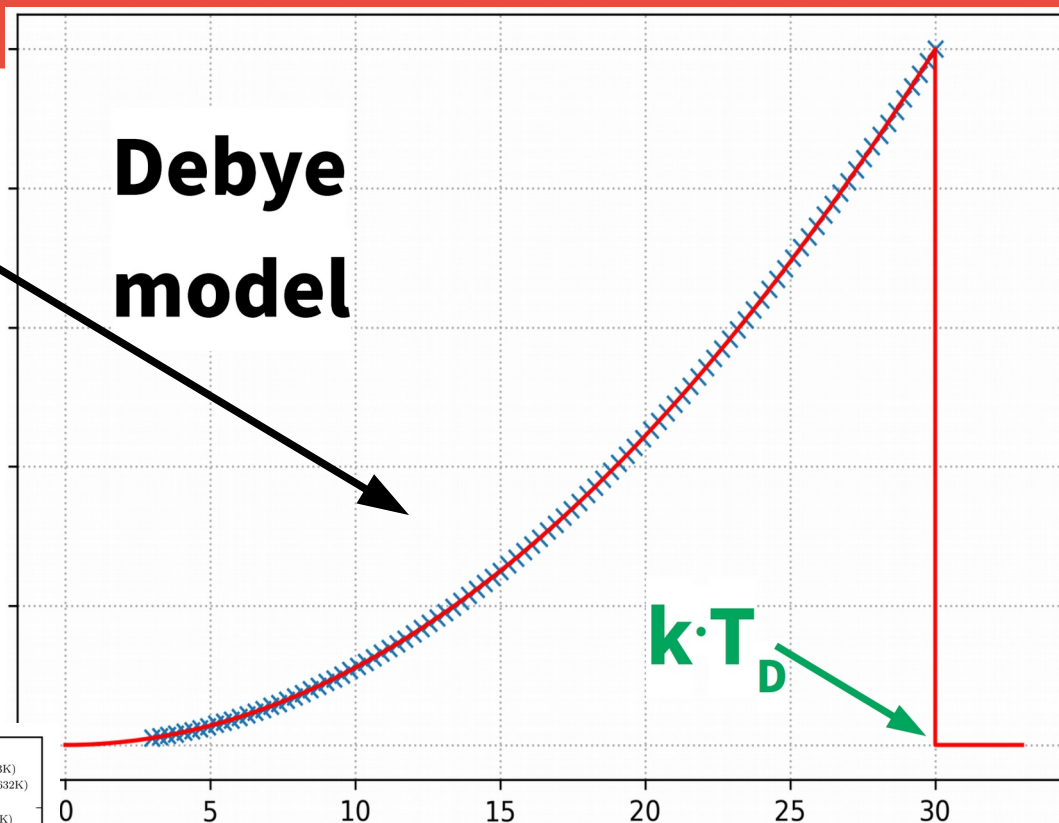
X.-X. Cai^{a,b,*}, T. Kittelmann^b, E. Klinkby^{a,b}, J.I. Márquez Damián^c

^a Technical University of Denmark, Denmark
^b European Spallation Source ERIC, Sweden
^c Nuclear Data Group, Neutron Physics Department, Centro Atómico Bariloche, CNEA, Argentina

How we handle materials with no phonon DOS specified?

Idealised DOS (Debye Model) is constructed and fed into same infrastructure as any other DOS.

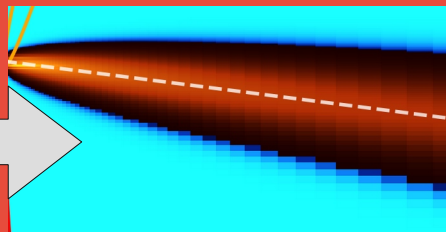
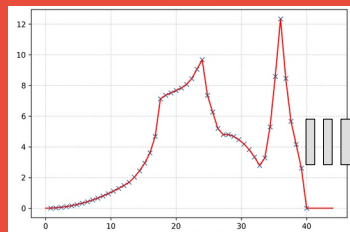
Lacks details of course, but gives consistent kinematics and handles multi-phonon physics ~OK.



T-dependent atomic displacements (δ), from Debye temperature (T_D)

Of course, a real DOS gives more realistic δ .

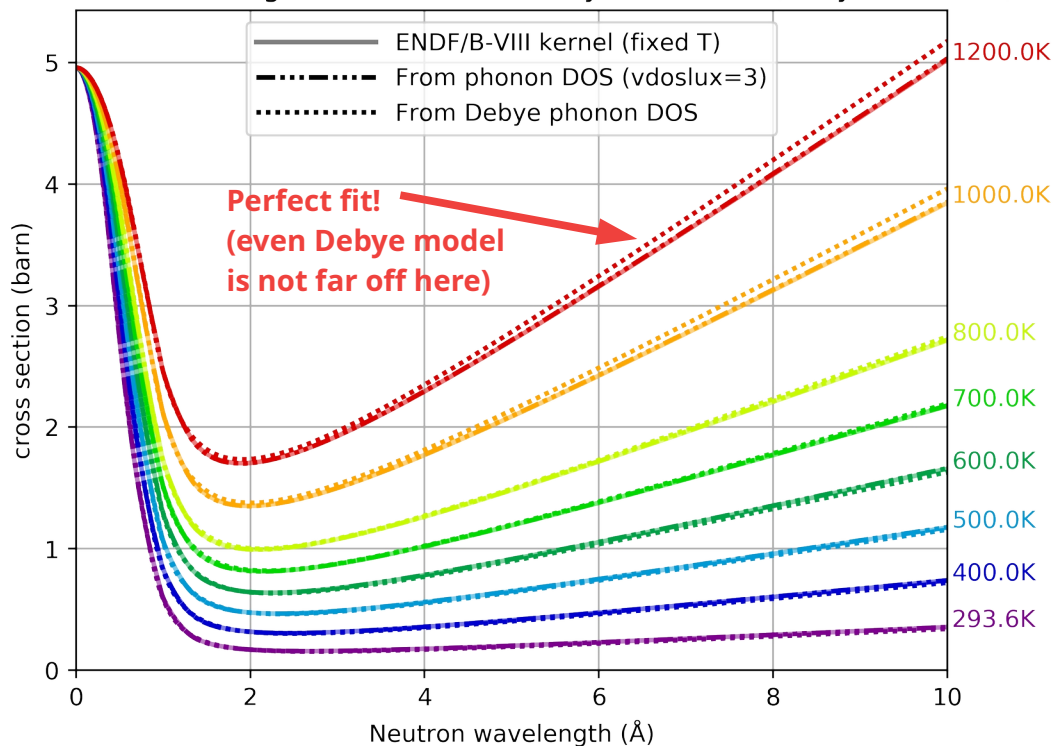
VDOS \rightarrow $S(\alpha, \beta)$ [solids]



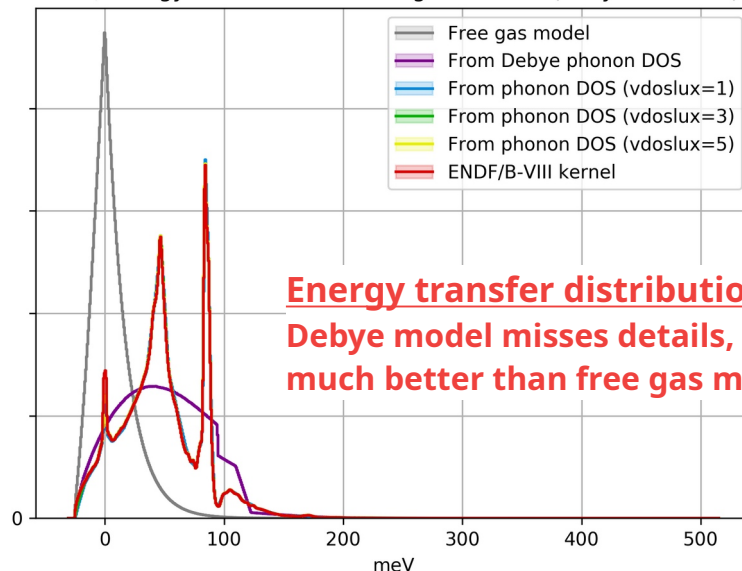
Identical results as when using LEAPR/ENDF kernels:

- Comparing at fixed temperature values from ENDF/B-VIII, using the same VDOS curve.
- NCrystal "luxury" level (cfg param "vdoslux", default value 3) mostly affects scattering kernel grid size+granularity.

Inelastic scattering cross section for Beryllium Oxide (NCrystal v2.0.0)

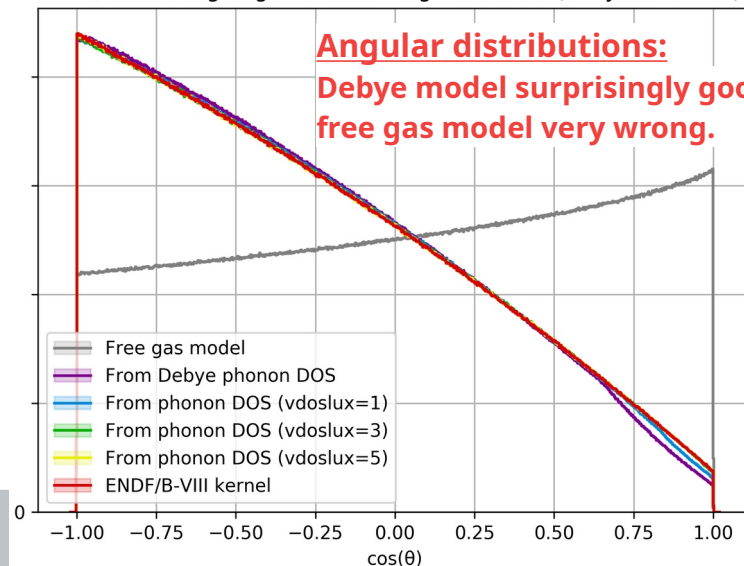


BeO, Energy transfer in scatterings at 1.8 Å (NCrystal v2.0.0)



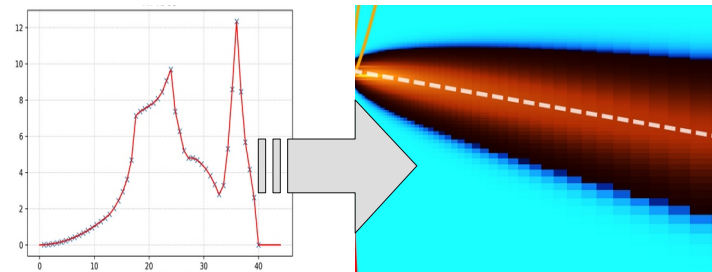
Energy transfer distributions:
Debye model misses details, but much better than free gas model.

BeO, Scattering angle in scatterings at 1.8 Å (NCrystal v2.0.0)

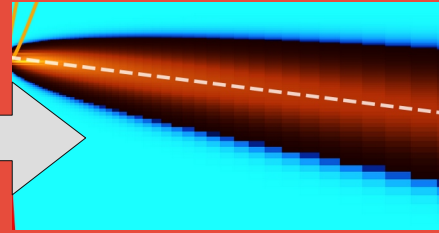
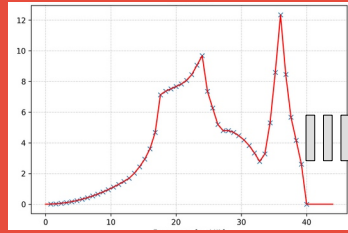


Angular distributions:
Debye model surprisingly good, free gas model very wrong.

VDOS \rightarrow Scattering kernel (the Sjölander method)



VDOS $\rightarrow S(\alpha, \beta)$



NCrystal
Thermal Neutron Transport

ARKIV FÖR FYSIK Band 14 nr 21

Communicated 14 May 1958 by IVAR WALLER and ERIK RUDBERG

Multi-phonon processes in slow neutron scattering by crystals

By ALF SJÖLANDER

With 12 figures in the text

ABSTRACT

The multi-phonon processes in incoherent scattering of slow neutrons by crystals are discussed, assuming the harmonic approximation for the crystal vibrations. The differential scattering cross section is expanded in the Hermite orthogonal functions and approximate expressions for the cross section are derived. Extensive numerical calculations have been carried out to illustrate the accuracy of the approximations made. An approximation for the total cross section (the mass-ratio expansion) suggested by Placzek is discussed and in some respects generalized. The approximations for the differential cross section mentioned above are also used to derive approximate formulae for the total cross section valid for cold neutrons but arbitrary temperatures and mass ratios.

Introduction

The basic ideas of the theory of slow neutron scattering by crystals were developed by Wick [1], Pomeranchuk [2], Seeger and Teller [3] and Akhiezer and Pomeranchuk [4]. A quantitative account was given by Weinstock [5], who discussed the temperature dependence of the total scattering. Afterwards the formal treatment was completed especially by Fröman [6]. He separated the scattering into phonon processes and consistently used the analogies with X-ray diffraction. An alternative method, very convenient for calculating the total scattering cross section, was later suggested by Placzek [7]. Recently the theory was reformulated by Glauber [8] and Van Hove [9] making it more surveyable. They derived closed expressions for the differential scattering cross section, which seem to be a convenient starting point for quantitative discussions. Van Hove also generalized the theory to general systems of nuclei, as for instance liquids and magnetic materials. A large number of experiments have been performed and these mainly confirm the basis of the theoretical treatment [10, 11].

Well-established method!

Used in NJOY/LEAPR. Most ENDF $S(\alpha, \beta)$ kernels were created this way.

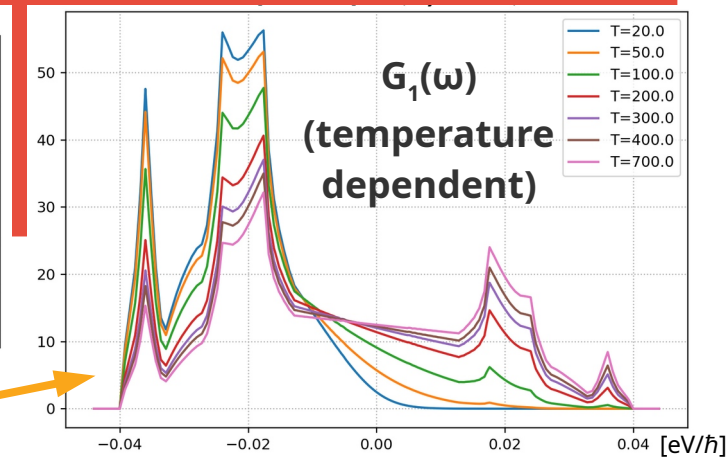
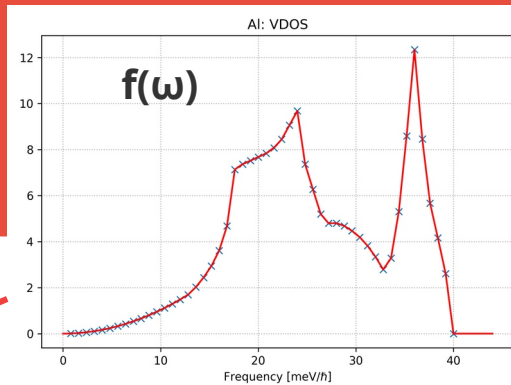
Key feature: Capability is built into NCrystal
And so fast (<0.1s) it can be invoked on-the-fly.

Gives us:

- **Flexibility.** Work directly from VDOS input, avoid usage of non-trivial third-party SW.
- **More materials.** VDOS are much more easily obtained than full kernels.
- **Small data files!**
Can easily include everywhere.
- **Temperature dependency built in:**
Unlike static $S(\alpha, \beta)$ which is only valid for a specific temperature.



VDOS \rightarrow $S(\alpha, \beta)$ Sjölander's recipe

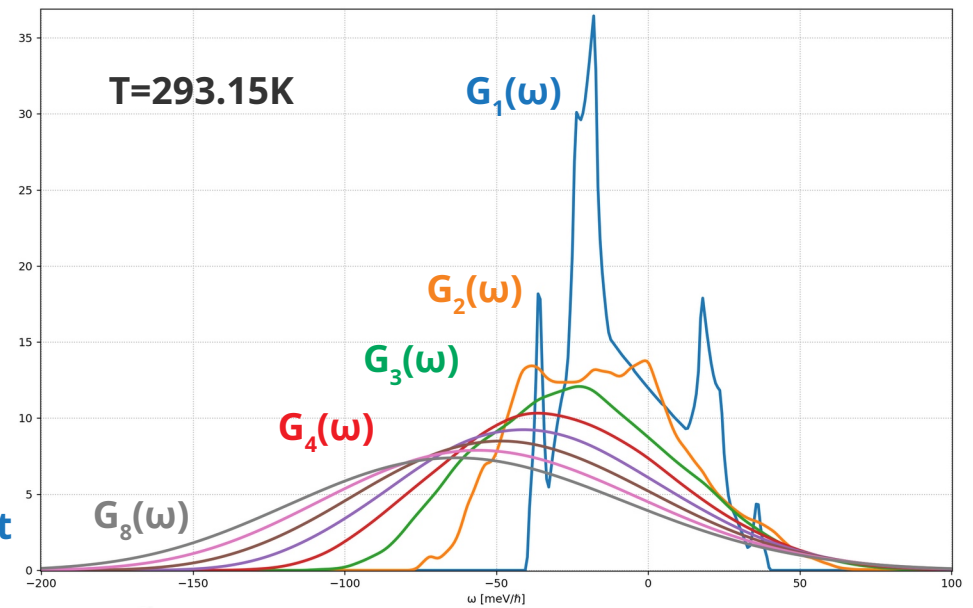


$$G_1(\omega) = g(\omega) = \frac{f(\omega)}{\omega \gamma(0)} \frac{\coth\left(\frac{\hbar\omega}{2kT}\right) - 1}{2},$$

$$G_2(\omega) = \int_{-\infty}^{\infty} g(\omega - \omega') G_1(\omega') d\omega',$$

.....

$$G_{n+1}(\omega) = \int_{-\infty}^{\infty} g(\omega - \omega') G_n(\omega') d\omega'.$$



$2W = \delta^2 q^2$, $\delta = \text{atomic displacement}$

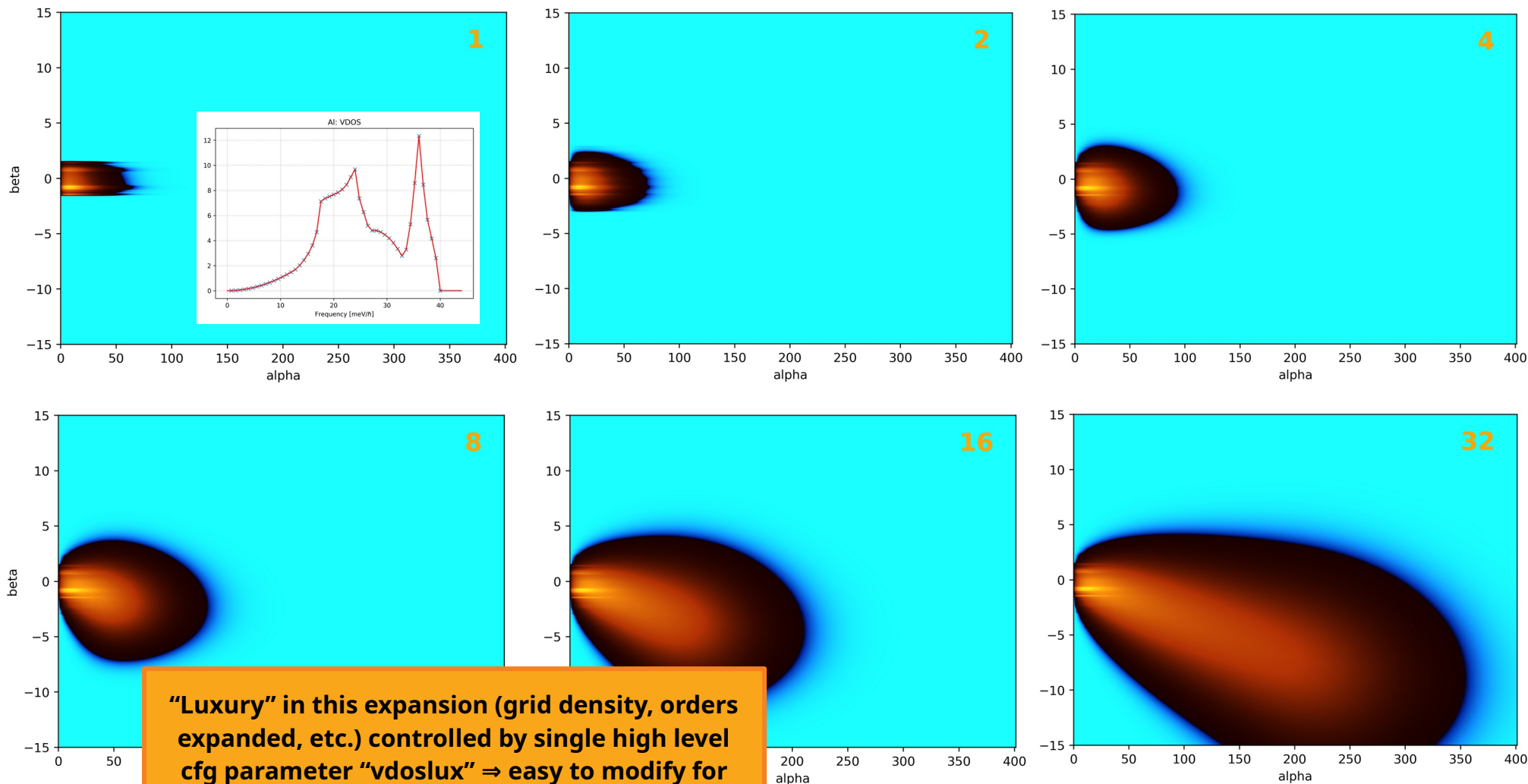
σ_b

$$\frac{d^2 \sigma_{\text{incoh}}}{d\Omega d\omega} = A \frac{k}{k_0} e^{-2W} \sum_{n=1}^{\infty} \frac{(2W)^n}{n!} G_n(\omega - \omega_0) \equiv \sqrt{\frac{E_f}{E} \frac{\sigma_b}{4\pi} \frac{S(\alpha, \beta)}{k_b T}}$$

$-\hbar(\omega - \omega_0)/kT = \Delta E/kT = \beta$

VDOS \rightarrow $S(\alpha, \beta)$: Aluminium

<https://github.com/mctools/ncrystal/wiki/VDOSAnimations>

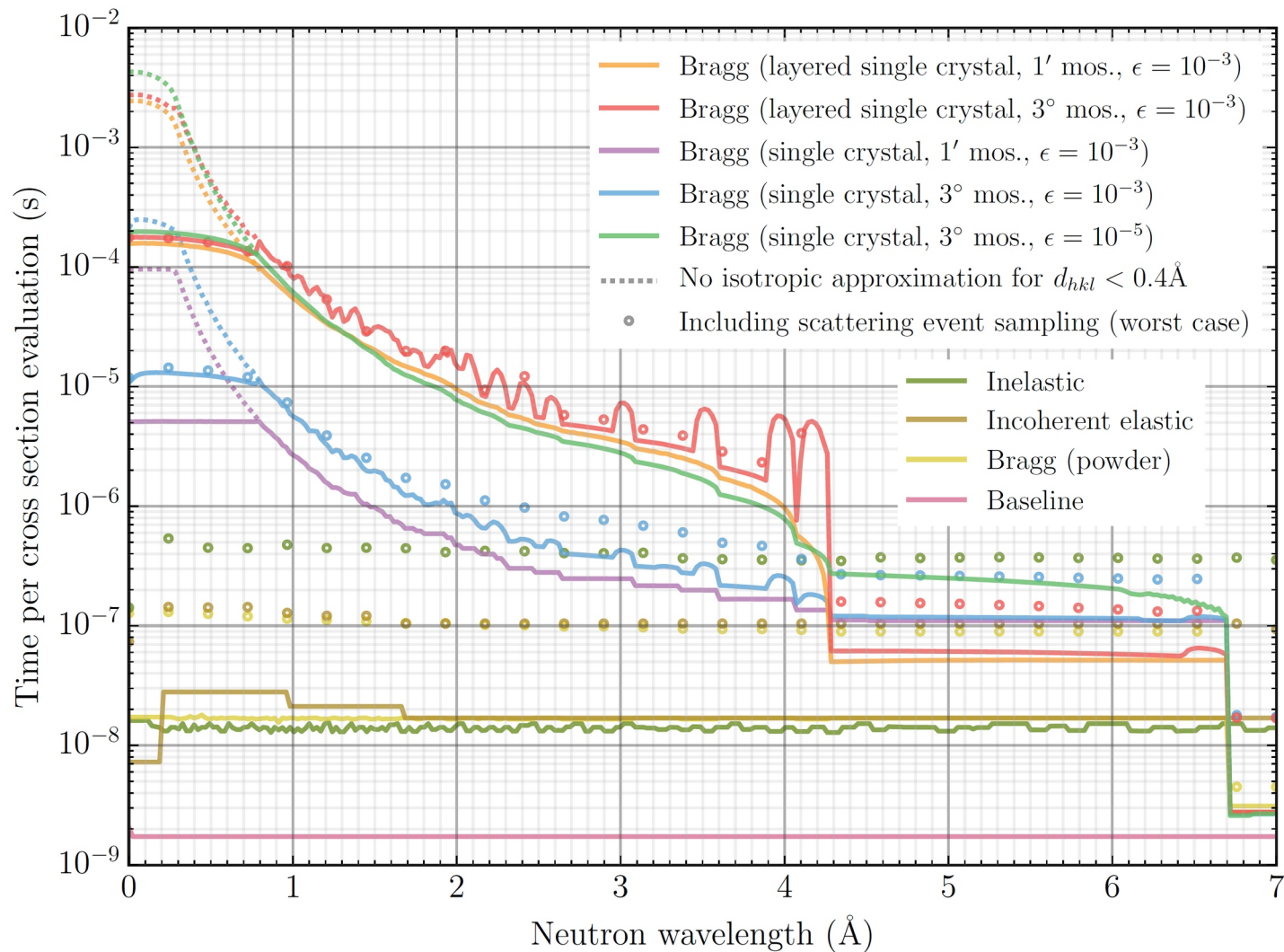


“Luxury” in this expansion (grid density, orders expanded, etc.) controlled by single high level cfg parameter “vdoslux” \Rightarrow easy to modify for any user (see backup slide for details). Default value is of course sensible.

Miscellaneous subjects:

- Computational speed
- Amorphous solids
- Flexible atomic definitions
- Multiphase materials + SANS
- Coherent elastic phonons
- Support for developed plugins

Strong focus on computational speed



Rough conclusions for MC simulations with thin samples:

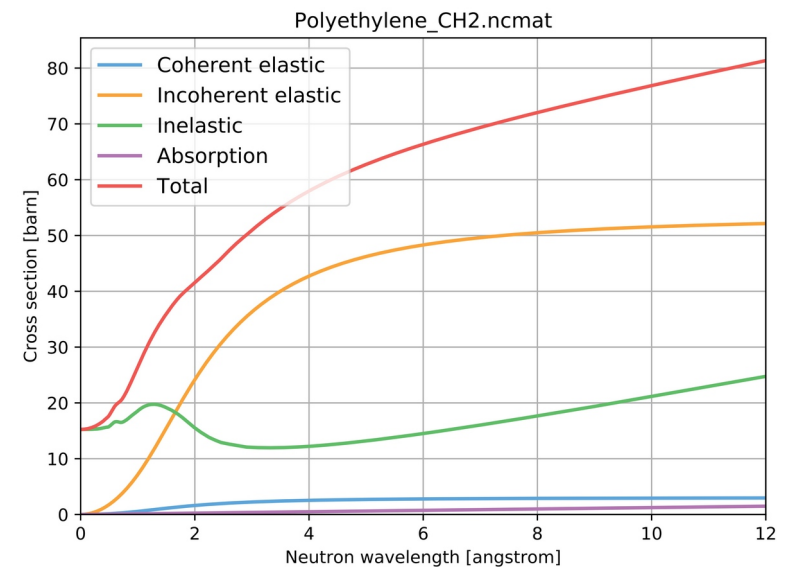
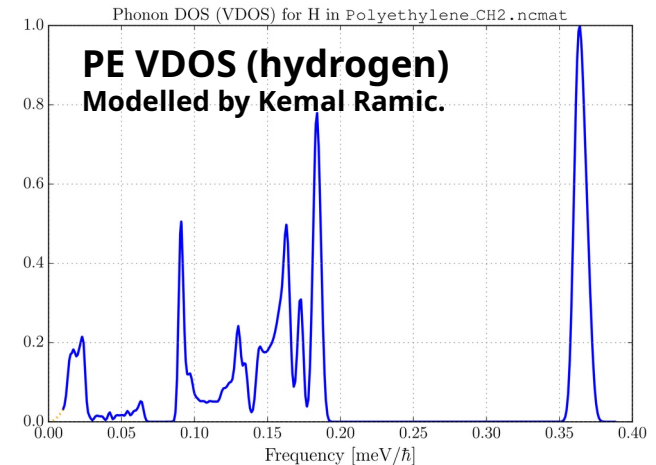
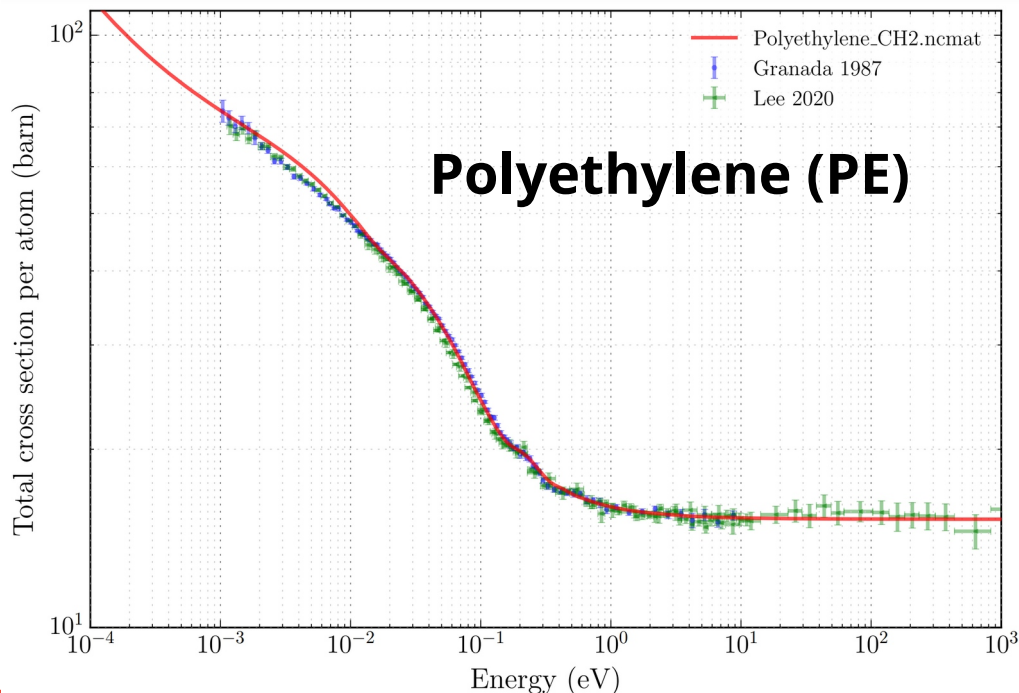
- O(1-100MHz) neutrons *per thread* in powder
- O(0.1-10MHz) neutrons *per thread* in single crystal (depends on λ)

Material *initialisation* time also very strong focus.

- V3.9.0 introduced several speedups and the option for multithreaded initialisation.
- Most materials initialise in <200ms (many <10ms)

Amorphous solids

- Uses same inelastic and incoherent-elastic approach as for crystalline solids.
- Coherent-elastic scattering via incoherent approximation for now, best for materials with lots of incoherent scattering like H-rich materials (but see next slide).






Easily model any hydrogen-rich amorphous solids (CLI tool)

- DFT/MD modelling of amorphous materials can be difficult and time consuming.
- Recent paper (Romanelli et. al., 2021) provides trustworthy and cheap alternative for hydrogen-rich materials.
- Relies on universality of hydrogen vibrations in different materials: Overall hydrogen VDOS can be composed from list of hydrogen bindings.
- We provide script for setting up NCMAT files with this.

Journal of Physics: Condensed Matter

PAPER

Thermal neutron cross sections of amino acids from average contributions of functional groups

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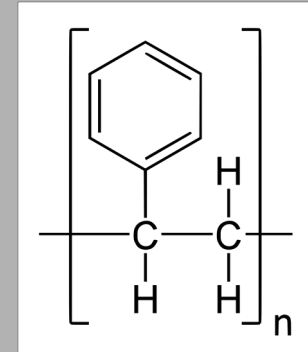
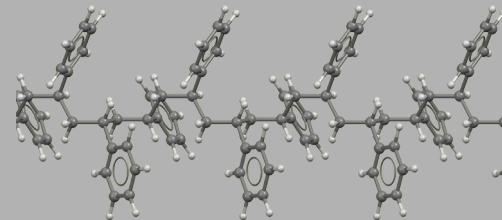
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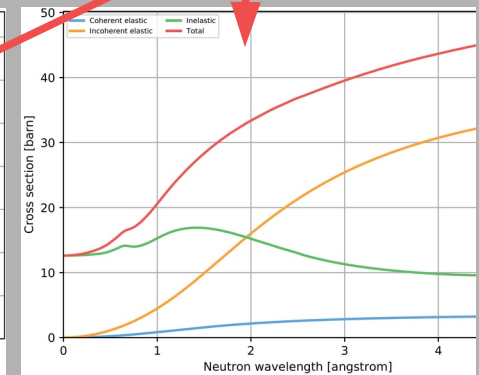
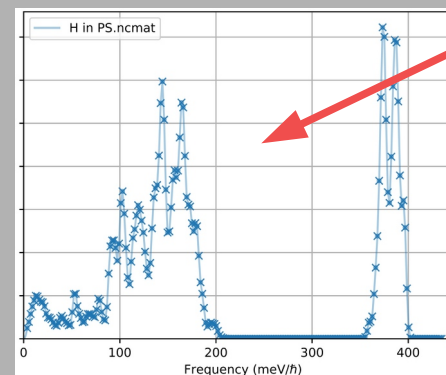
[References](#) ▾

Example (polystyrene):

- 1 aromatic ring with 5 H
- 1 CH₂ group
- 1 aliphatic CH binding

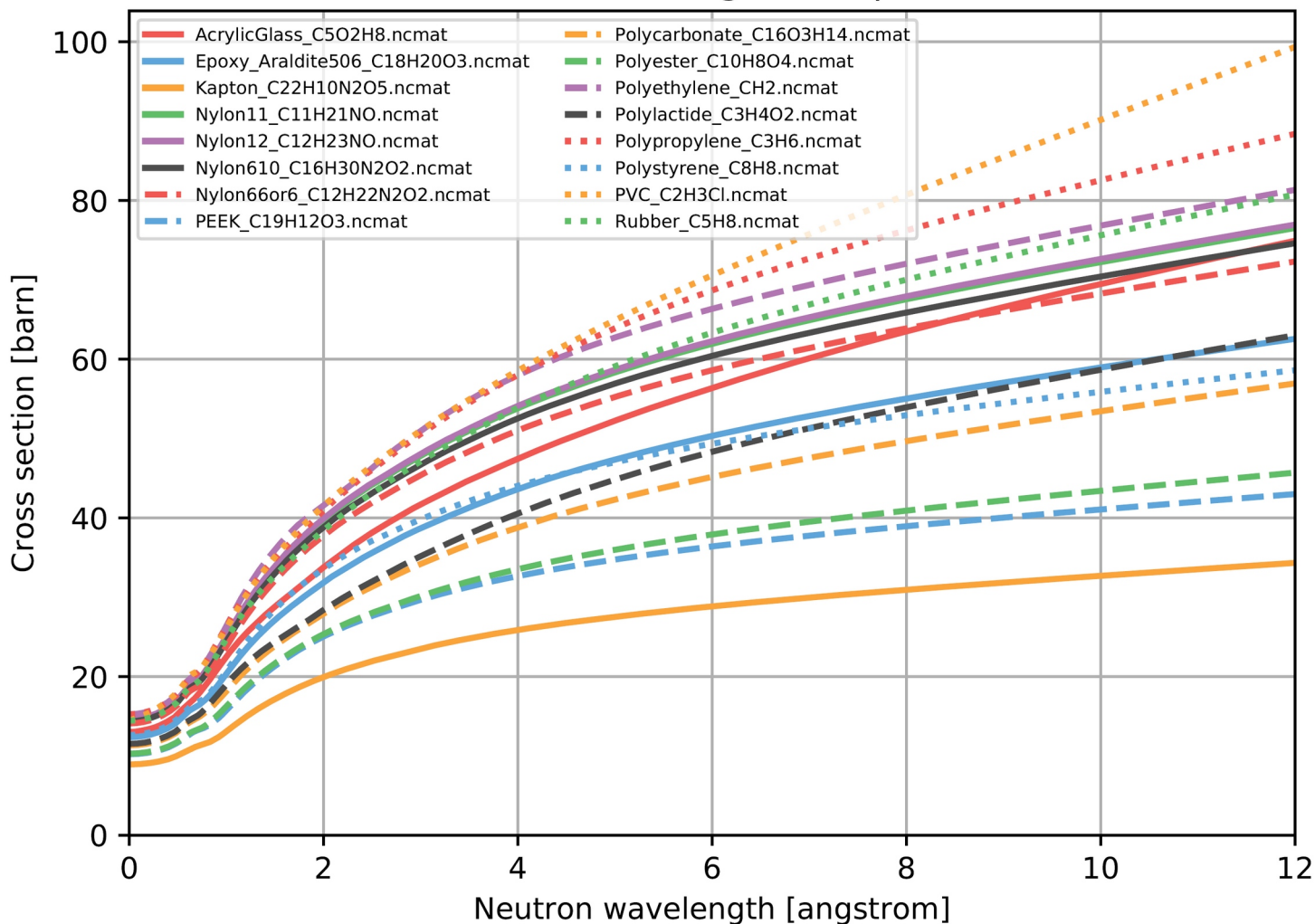


```
$> ncrystal_hfg2ncmat --formula C8H8 \  
--spec 5xCharo+1xCHali+1xCH2 \  
--density 0.99 -o PS.ncmat
```



Amorphous materials in data library

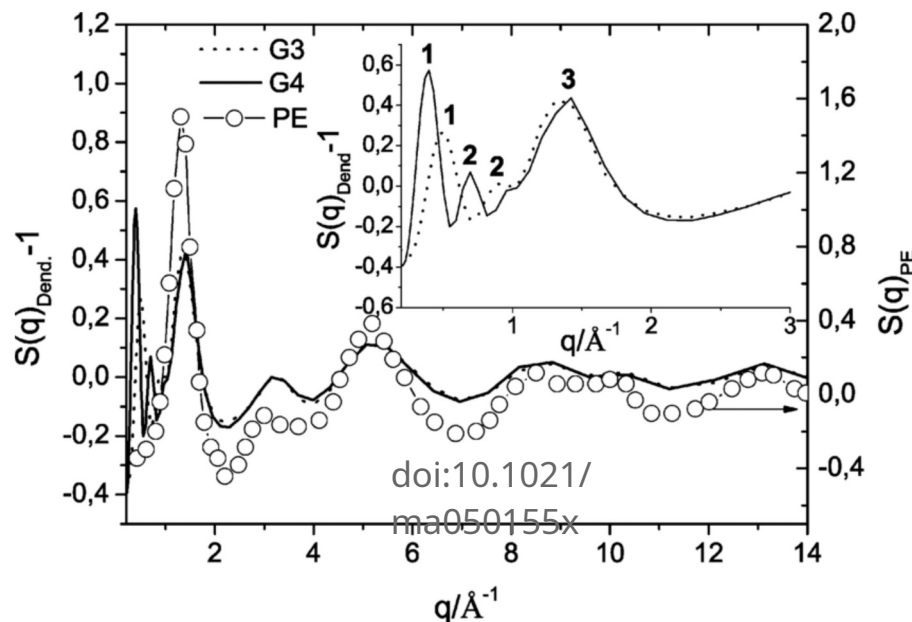
Total scattering+Absorption



- **Polyethylene and AcrylicGlass (a.k.a. Plexiglass/Lucite) based on VDOS from other sources.**
- **14 others based on ncrystal_hfg2ncmat script (AFGA).**
- **Let us know if we are missing something useful!**

Coherent effects in amorphous materials: static structure factors

- We plan to eventually also optionally include static structure factors $S(q)$ in our treatment of amorphous solids, but for now they are modelled under the *incoherent approximation*.
- The *incoherent approximation* is very good for esp. hydrogen-rich materials, but amorphous materials without strong incoherent cross sections might suffer in realism currently.



NCrystal development at ESS was recently chosen to be supported by the APRENDE EURATOM grant. This will hopefully allow us to include these effects for increased realism.

The tricky part is to include them along with the current inelastic kernel, without ending up with double-counting (likely we will use Sköld's method).

Flexible atomic (re)definitions

NCrystal supports atoms which are not just natural elements!

- Ships with database of 80+ natural elements and 261+ isotopes.
- Possibility to customise:
 - In NCMAT data
 - In cfg-string parameter
 - With the NCMATComposer

NCMAT v3
@ATOMDB

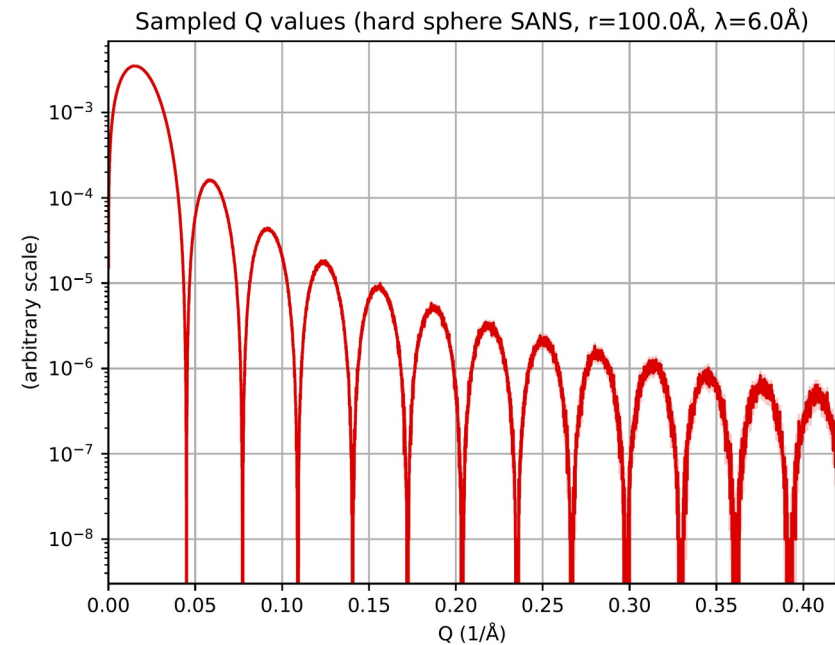
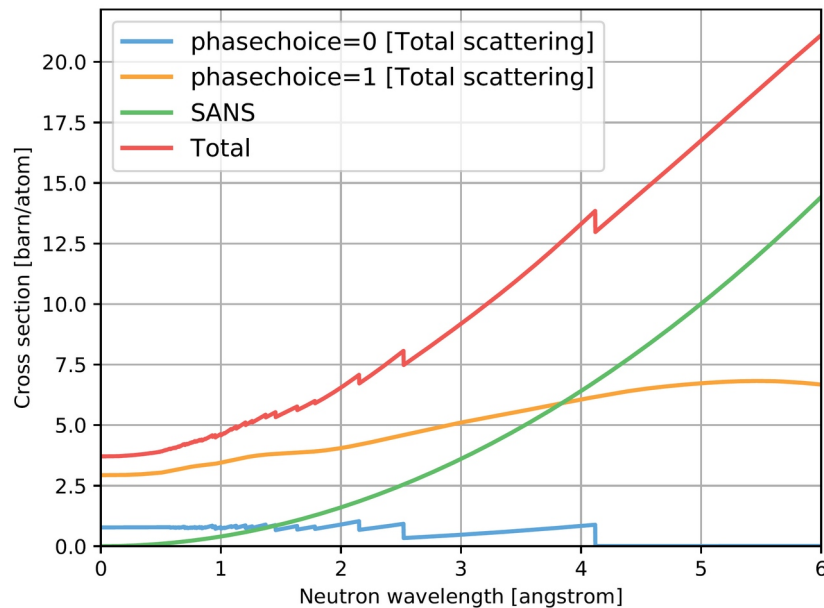
```
#Override data for whatever reason:
H 1.008u -3.7fm 80.3b 0.3b
#Provide absent data:
Rn222 222.017u 123fm 0.456b 789b
#Enrich Boron:
B mix 0.95 B10 0.05 B11
#Add dopants on Al positions:
Al mix 0.99 Al 0.01 Cr
#Alternatively use "variable names"
#(for usage elsewhere in the file):
X mix 0.2 Al 0.4 Cr 0.4 Th
#Or simply assign:
B is B10
```

```
auto sc = NCrystal::createScatter("Al203_sg167_Corundum.ncmat;atomdb=Al:mix:0.99:Al:0.01:Cr");
```

Multiphase materials

- Multiphase materials can be defined inside NCMAT data (i.e. with the NCMATComposer), or in a cfg-string:
 - `“phases<FRAC1*CFGSTR1&...&FRACN*CFGSTRN>;COMMONCFG”`
- Example (enriched B4C pellets in epoxy):
 - `“phases<0.01*solid::B4C/2.52gcm3/B_is_0.95_B10_0.05_B11
&0.99*Epoxy_Araldite506_C18H2003.ncmat>;temp=250K”`
- NB: Using volume fractions, not mass fractions (for now).
- NB: Syntax designed so you can always append e.g. `“;temp=250K”` to a cfg-string, and have it work.

- Closely connected to multiphase support, NCrystal contains a framework for SANS physics (= phase interference).
- For now, only a basic hard-sphere SANS model can be enabled, as proof of concept. Planning to at least add this and general $I(Q)$ support properly to the NCMAT format



Extend NCrystal with 3rd-party plugins

NCrystal includes a plugin mechanism, making it possible add custom physics models

- This can help people with their specific simulation use-case, and (in an ideal world) high quality models can eventually be adopted into the main NCrystal code.
- Extending NCrystal will naturally require C++ knowledge.
- Such plugins can be developed in separate github repos, with standard mechanism for how to include them in a given NCrystal setup.
- More details on: <https://github.com/mctools/ncrystal/wiki/Plugins>

Nanodiamond plugin:

Rizzi, N., et al. (2023).

Benchmarking of the NCrystal SANS Plugin for Nanodiamonds.

Nuclear Science and Engineering, 198(1), 92-100.

<https://doi.org/10.1080/00295639.2023.2196926>

<https://indico.ess.eu/event/3096/contributions/17717/> (slides)

Magnetic scattering plugin:

Xu, S., et al. (2024).

Physical model of neutron scattering by clathrate hydrate and C60 hosting paramagnetic oxygen molecules.

Journal of Physics: Condensed Matter, Volume 36, Number 38.

<https://doi.org/10.1088/1361-648X/ad5947>

<https://indico.ess.eu/event/3096/contributions/17717/> (slides)

Other plugins in development:

- March-Dollase Texture plugin by S. Xu et al.
- Coherent phonon plugin by X. X. Cai et al.

WIP: Coherent inelastic effects

- CSNS group (Xiao Xiao Cai, et al.) working on tools for providing high quality coherent-inelastic kernels for NCrystal.
- A proof-of-concept plugin for NCrystal for using those already exists.
- Such files would be temperature-specific and much larger, but for many use-cases this would be very interesting.
- Group also looking at extending this to non-isotropic materials (single crystals).

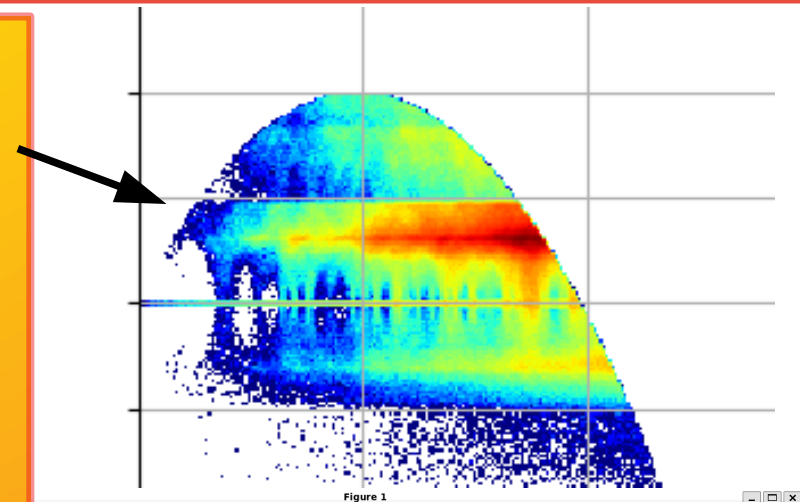
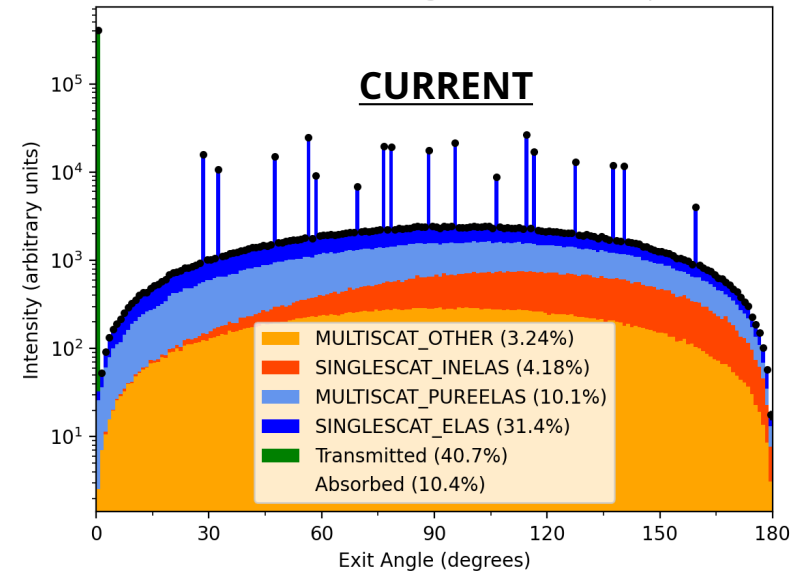
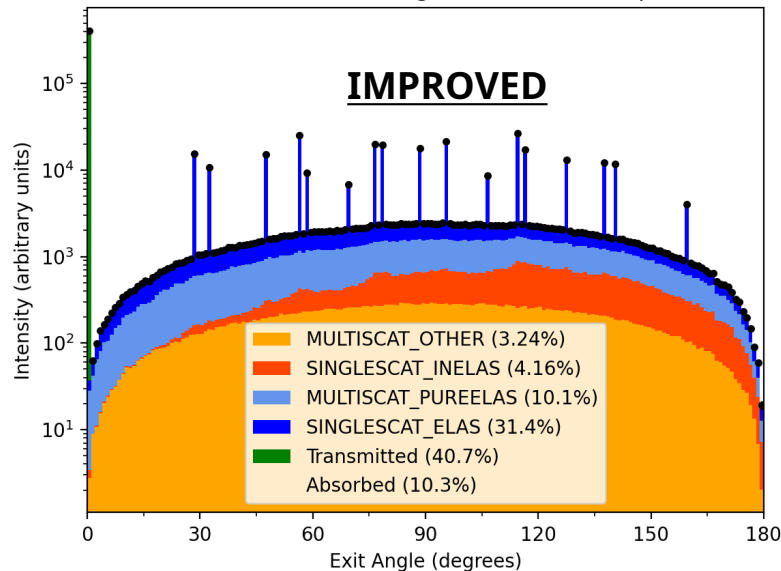
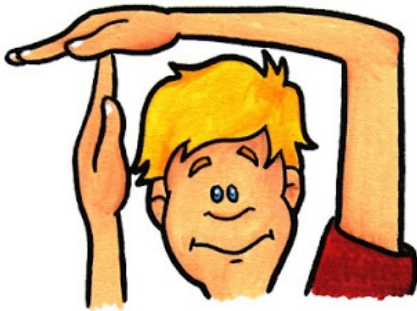


Figure 1

skeleton_c1_vol_77K.ncmat
10⁶ 1Aa neutrons through 5mm diameter sphere





Second half of the notebook: "Creating materials and the NCMATComposer"

 **Jupyter tutorials at:**
<https://github.com/mctools/ncrystal-notebooks/>





(of these slides)

Backup slides

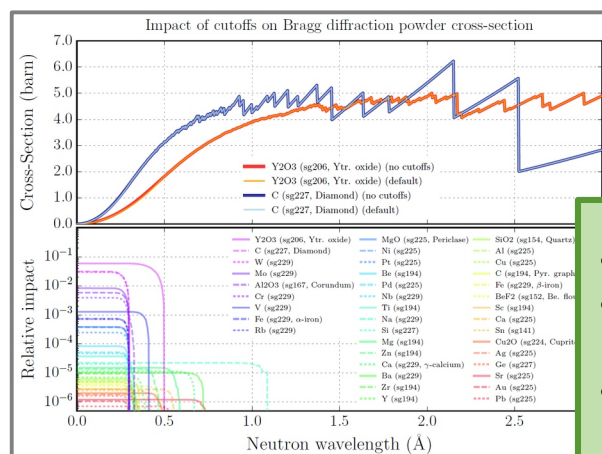
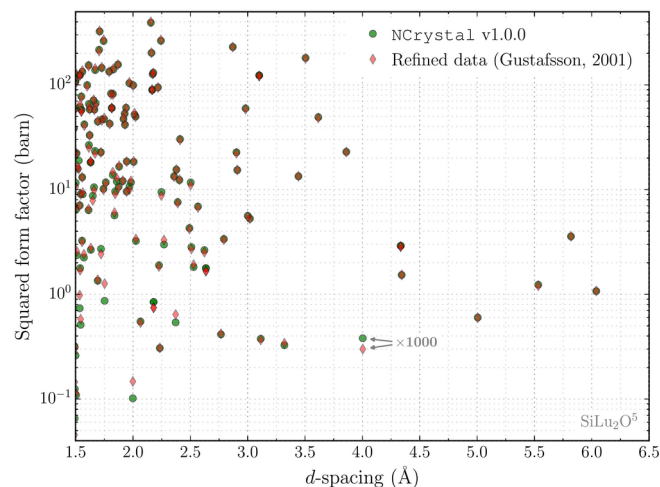
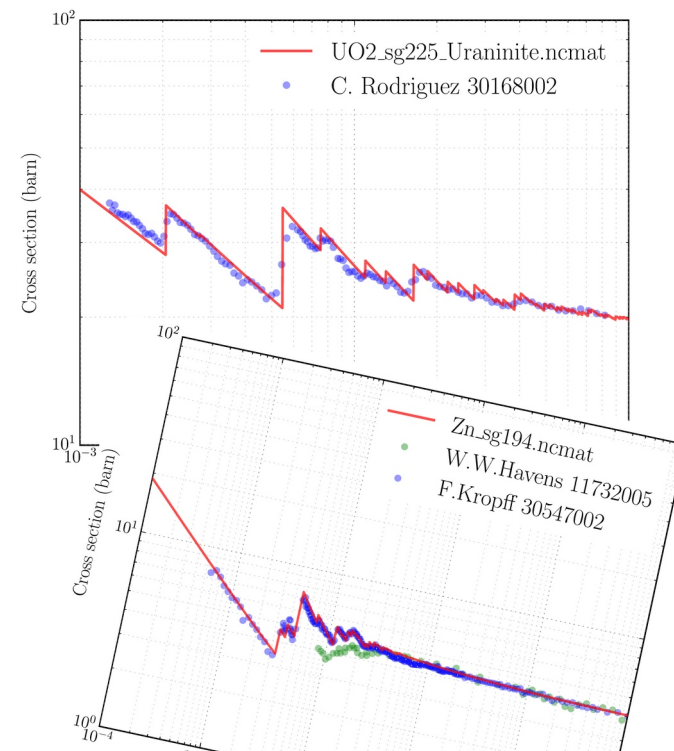
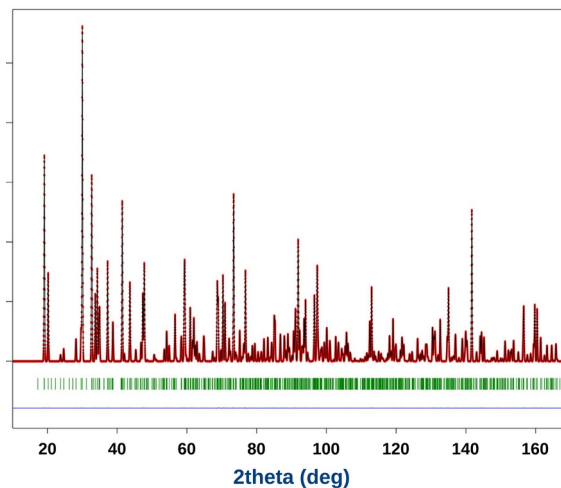
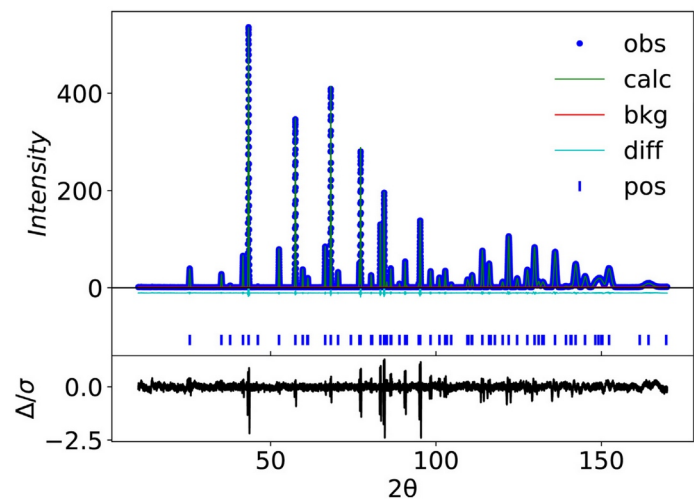


Control DOS→scat. kernel expansion through cfg parameter “vdoslux”

- Controls all aspects of DOS→kernel expansion with only one high level user-accessible parameter.
- Exposing the underlying multitude of parameters to end-users would do no good in practice since no-one would understand how to change them in a self-consistent way.
- **vdoslux=0**: Extremely crude, 100x50 grid, Emax=0.5eV (costs 0.1MB mem, 0.02s init time) ← **The default if using Debye model instead of actual input data (vdoslux gets reduced by 3 for these mats.)**
- **vdoslux=1**: Crude, 200x100 grid, Emax=1eV (costs 0.5MB mem, 0.04s init time)
- **vdoslux=2**: Decent, 400x200 grid, Emax=3eV (costs 2MB mem, 0.08s init time) ← **Typical level in ENDF kernels**
- **vdoslux=3** : Good, 800x400 grid, Emax=5eV (costs 8MB mem, 0.2s init time) ← **The default!**
- **vdoslux=4**: Very good, 1600x800 grid, Emax=8eV (costs 30MB mem, 0.8s init time)
- **vdoslux=5**: Extremely good, 3200x1600 grid, Emax=12eV (costs 125MB mem, 5s init time) ← **Overkill, exists for validation purpose**

Users adviced to leave at default (3), or change with ±1 to 2 or 4.

HKL structure factors initialised on-the-fly (validated thoroughly)

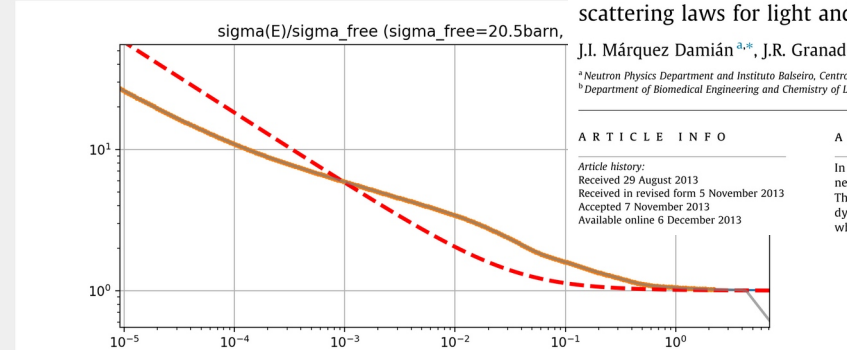
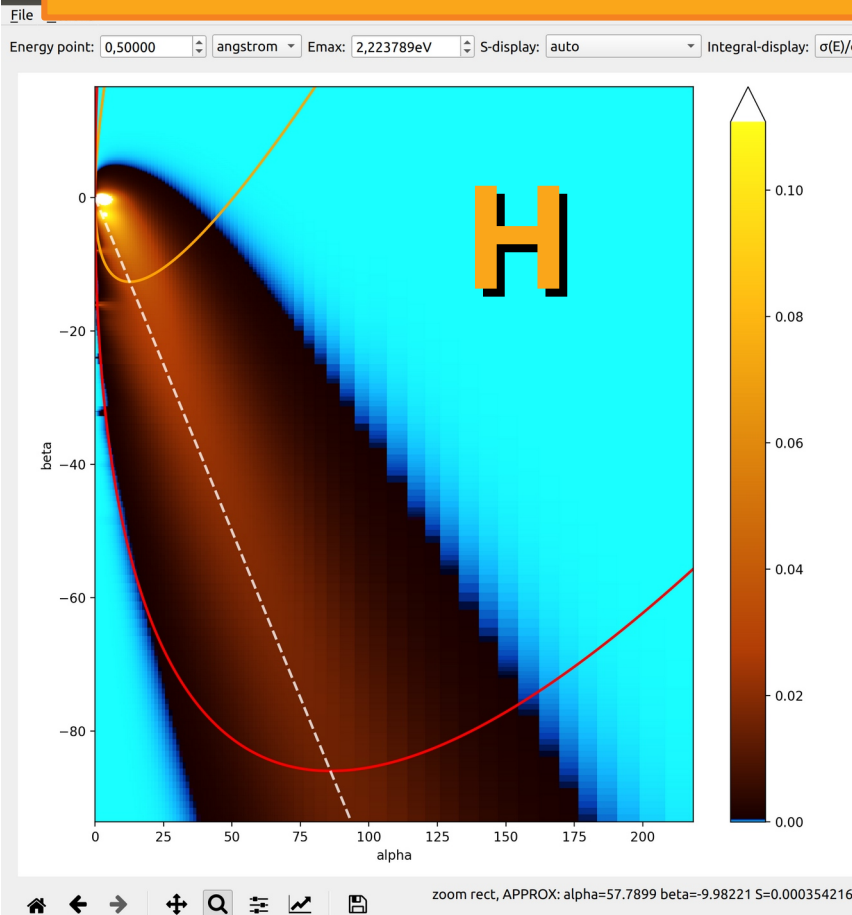


- Fast (few ms) init. of **all** relevant planes.
- Comparisons to measured structure factors and total cross sections.
- NCrystal+McStas simulated scattering patterns analysed with GSAS-II/Fullprof (recovering input crystal parameters).
- Comparison with NXS library predictions.

Support for liquids rely on externally provided kernels, here water (converted from ENDF8)



**VDOS→S(α,β) does not work directly for liquids!
NCrystal for now relies on kernel converted from e.g. ENDF**



CAB models for water: A new evaluation of the thermal neutron scattering laws for light and heavy water in ENDF-6 format

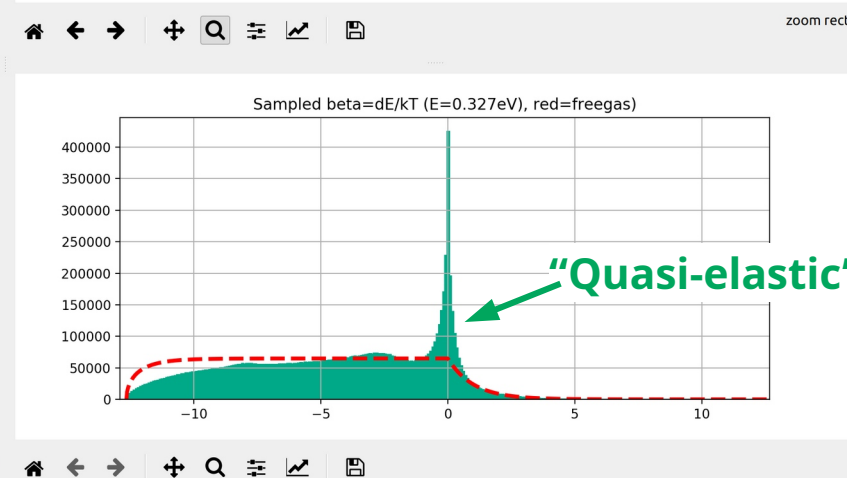
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ABSTRACT

In this work we present the CAB models for water: a set of new models for neutron scattering laws for light and heavy water in ENDF-6 format, using dynamics simulations. The calculations show a significant improvement when compared with measurements of differential and integral scattering



Oxygen is modelled as free gas

Showing tsl-HinH2O_300.0K.ncmat [H, A=1.00794, fraction=66.67%, T=300K, kT=0.02585eV, 1.1MB]



Single crystal with Gaussian mosaicity uses cheap pre-check to speed up

```
double NC::GaussMos::calcCrossSections( InteractionPars& ip,
                                       const NC::Vector& indir,
                                       const std::vector<NC::Vector>& deminormals,
                                       std::vector<NC::GaussMos::ScatCache>& cache,
                                       VectD& xs_commul ) const
{
    nc_assert(ip.isValid()&&ip.m_wl>0);
    nc_assert(indir.isUnitVector());
    std::vector<Vector>::const_iterator it(deminormals.begin()), itE(deminormals.end());
    double xsoffset = xs_commul.empty() ? 0.0 : xs_commul.back();
    double xssum(0.0);
    const double cptsq = ip.m_cos_perfect_theta_sq;
    const double cta = m_gos.getCosTruncangle();
    for(;it!=itE;++it) {
        const Vector& normal = *it;
        const double dot = normal.dot(indir);
        double sdotcptsq = (1.0 - dot * dot)*cptsq;
        double ds = dot * ip.m_sin_perfect_theta;

        //First a combined check, which usually allows us to skip both normal and
        //anti-normal:
        double A0 = ncmax( 0.0, cta - ncabs(ds) );
        if ( sdotcptsq <= A0*A0 )
            continue;

        //At least one of the two normals should contribute, so deal with them:
        double Am = ncmax( 0.0, cta - ds );
        if ( sdotcptsq > Am*Am ) {
            //anti-normal is within truncated Gauss
            double xs = calcRawCrossSectionValue(ip, dot );
            if (xs) {
                xs_commul.push_back(xsoffset + (xssum += xs));
                cache.emplace_back(-normal, ip.m_inv2dsp);
            }
        }
        double Ap = ncmax( 0.0, cta + ds );
        if ( sdotcptsq > Ap*Ap ) {
            //normal is within truncated Gauss
            double xs = calcRawCrossSectionValue(ip, -dot );
            if (xs) {
                xs_commul.push_back(xsoffset + (xssum += xs));
                cache.emplace_back(normal, ip.m_inv2dsp);
            }
        }
    }
    return xssum;
}
```

This function gives xsect for all planes with a given d-spacing (only called if d-spacing < $\lambda/2$)

Must check all normals in group.

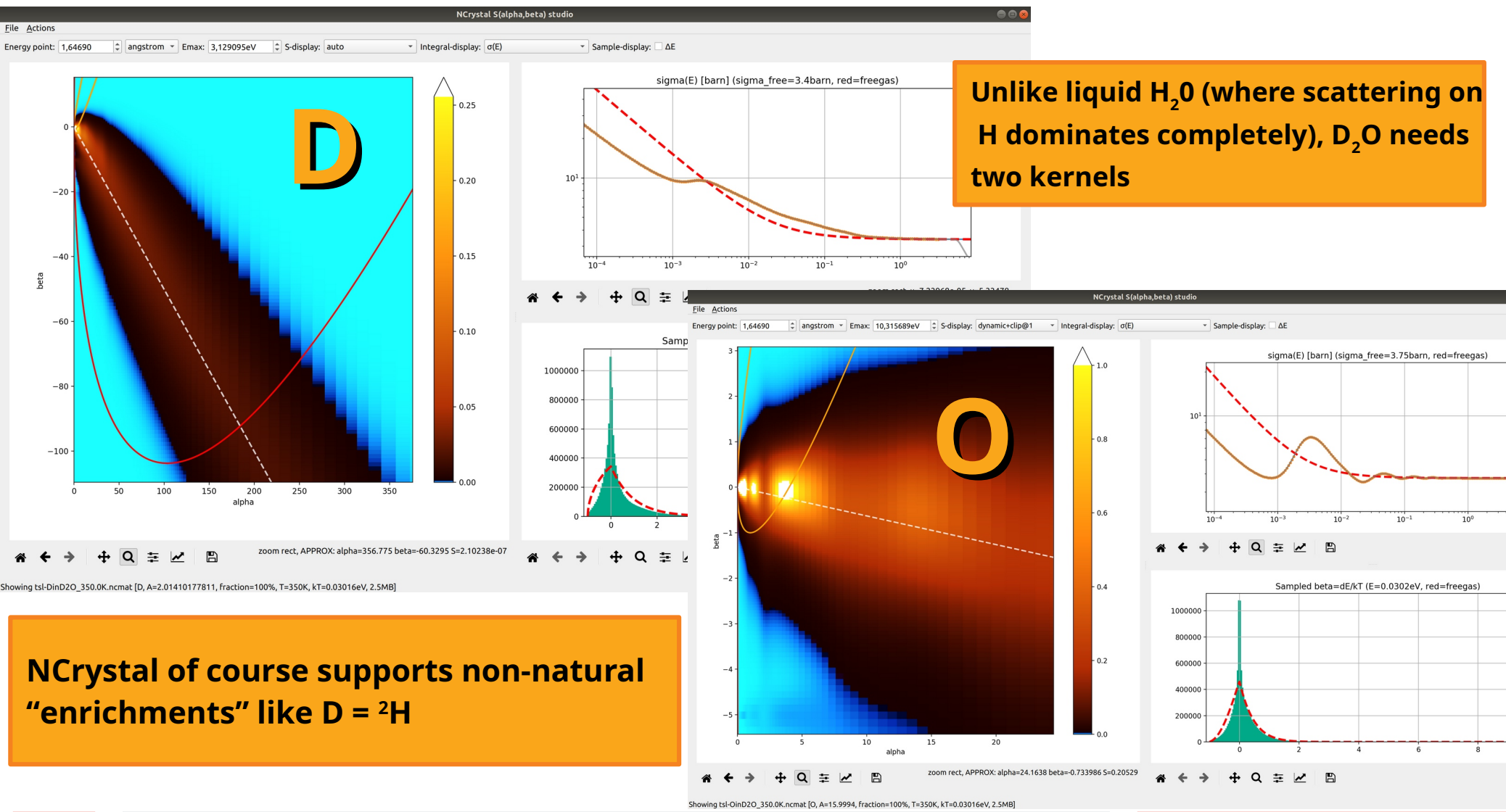
Precheck allows most planes to be skipped since they do not contribute.

Precise evaluation of the non-zero contribution is still where most time is spent, even when only very few planes survives the cheap pre-check!

Time to sample interactions is much less crucial, since it mostly deals with only a single plane.

... and heavy water (also converted from ENDF8)

Unlike liquid H₂O (where scattering on H dominates completely), D₂O needs two kernels



NCrystal of course supports non-natural "enrichments" like D = ²H