

Measurement and evaluation of the neutron scattering cross section for moderator materials in accelerator-based neutron sources

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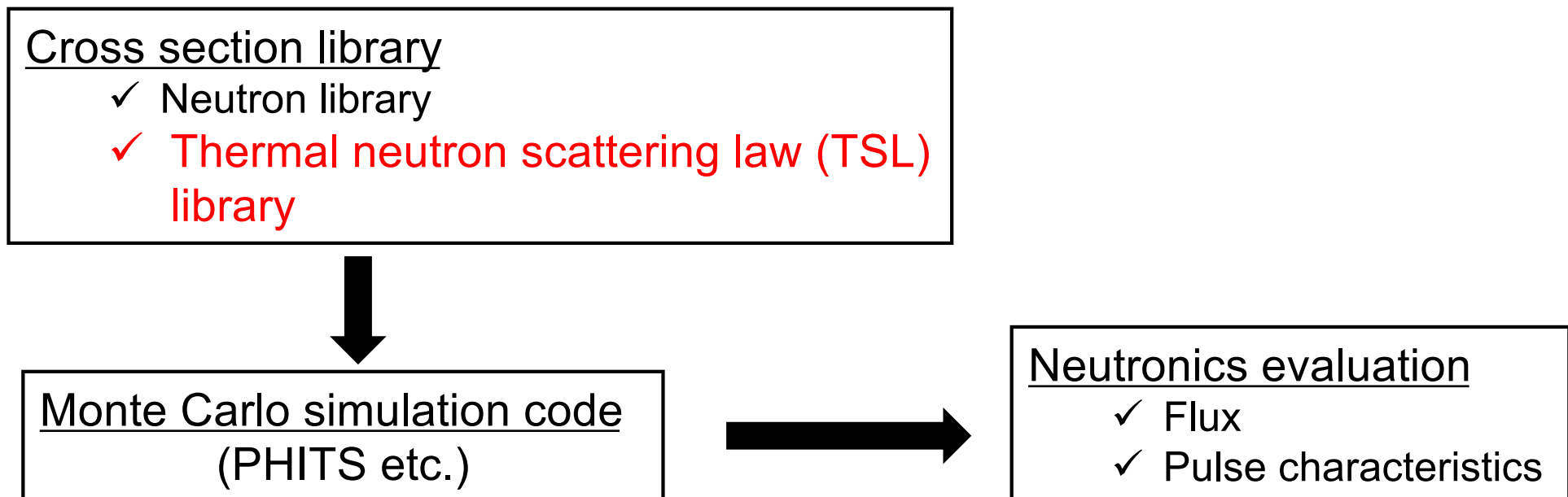
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Introduction

In the development of moderators at neutron sources, the estimation of performance by neutronics calculations using Monte Carlo simulations is important.

Low energy neutron transport calculation



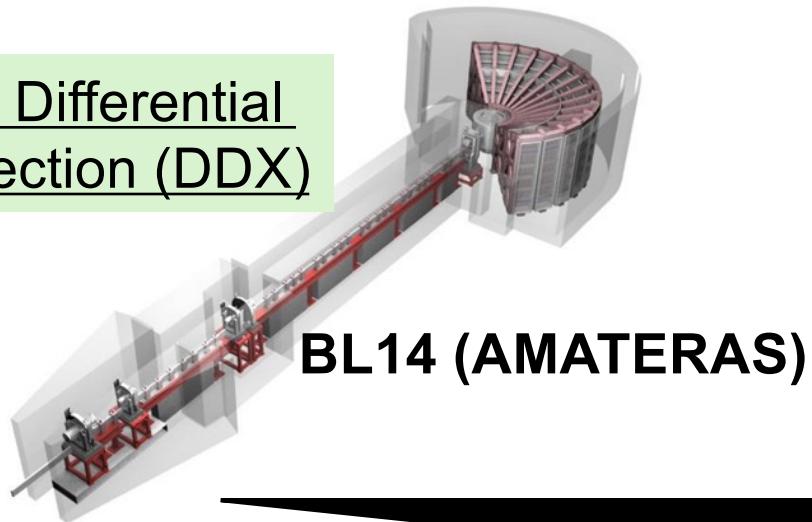
To accurately estimate neutronics of low energy neutrons, TSL data for moderator and reflector materials are important.

Introduction

Experiment at MLF J-PARC

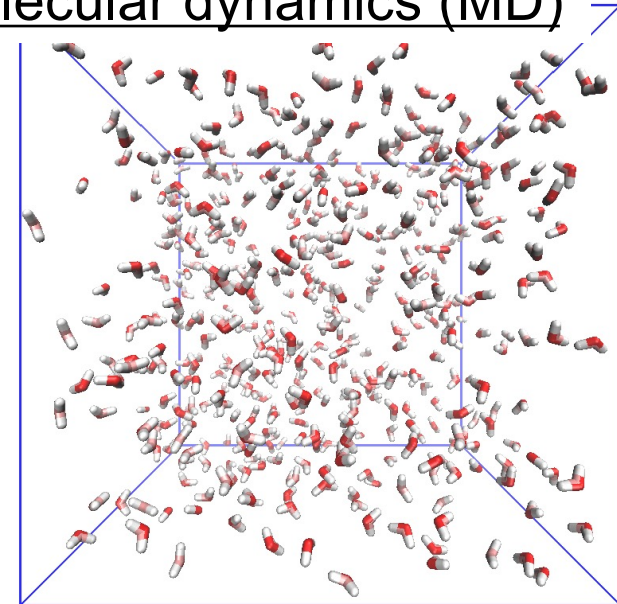


Double Differential cross section (DDX)



Evaluation

Molecular dynamics (MD)



KUNSCA

Kyoto University Neutron Scattering
Cross-section Analyzer ^[1]

Highly accurate TSL data for moderator materials

[1]Y. Abe, *et al.*, *Annals of Nuclear Energy*, vol 194, 110101, 2023.

Outline

- Improvement of scattering cross section for H₂O
 - Measurement of DDX
 - Comparison with calculation values

- Calculation of scattering cross section for liquid-H₂, -D₂, -HD
 - Addition of a new feature in KUNSCA

Outline

■ Improvement of scattering cross section for H₂O

- Measurement of DDX
- Comparison with calculation values

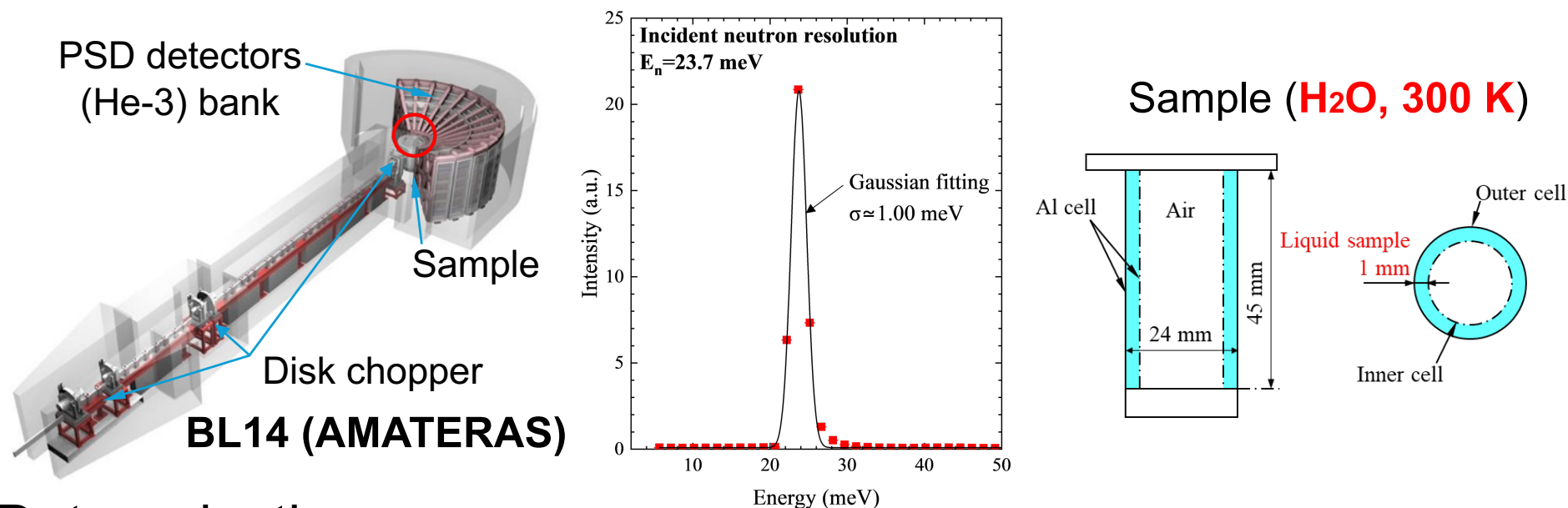
■ Calculation of scattering cross section for liquid-H₂, -D₂, -HD

- Addition of a new feature in KUNSCA

Measurement of DDX

■ Experimental setup

- Incident neutron energy : 10.5 meV, **23.7 meV**
- Scattering angle : 30 ~ 110-deg (10-deg interval)



■ Data reduction

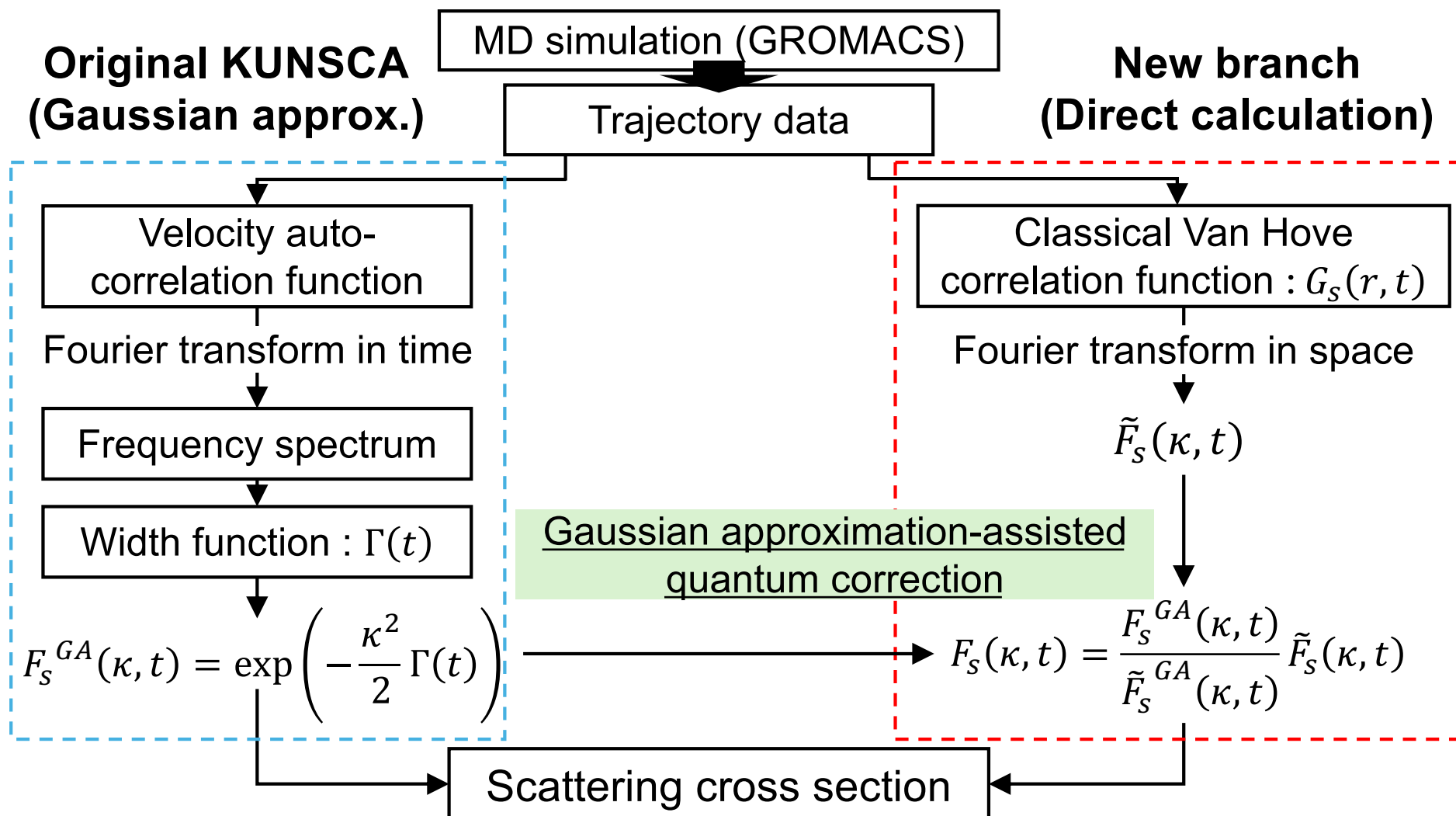
- The absolute DDX was deduced relative to the incoherent scattering cross section of vanadium.
- Correction factors for multiple scattering and neutron attenuation were calculated by Monte Carlo simulation.

Calculation methodology

$$\kappa = |\vec{k}_0 - \vec{k}|$$

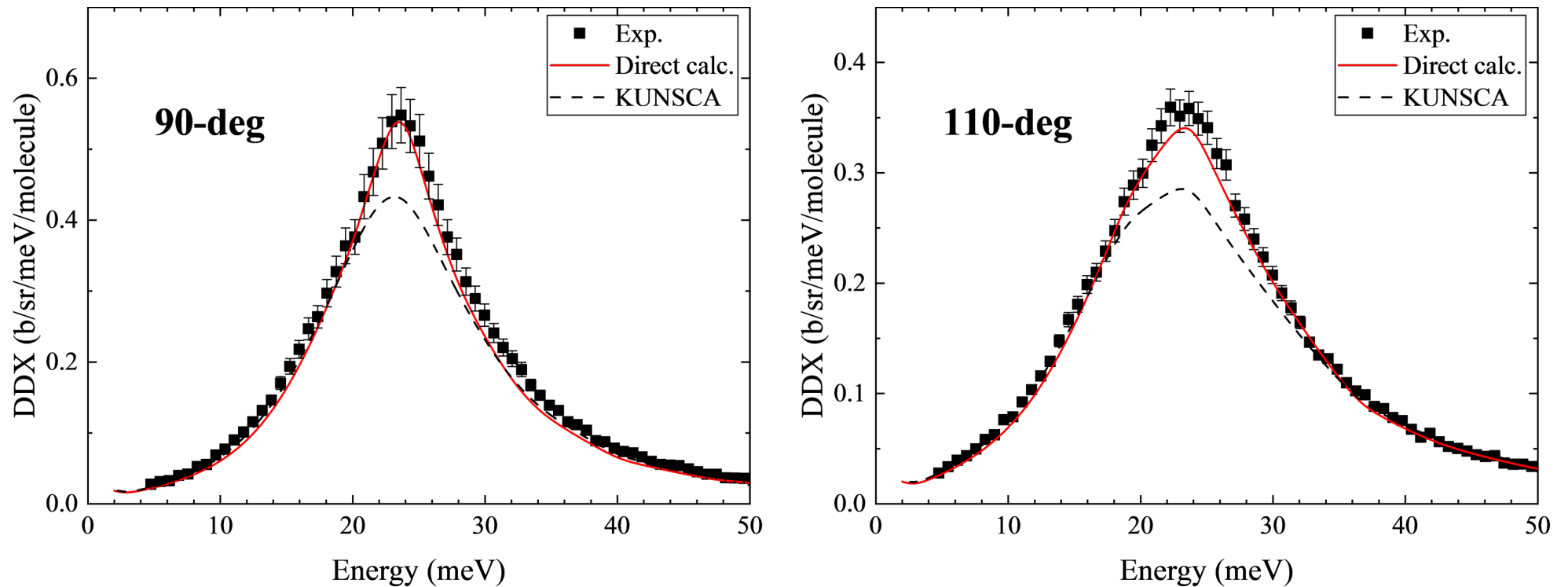
$$\varepsilon = \hbar\omega = E_0 - E$$

$$\frac{d^2\sigma}{d\Omega d\varepsilon} = \frac{k'}{k} \sum_{x=1}^N \frac{\sigma_b^x}{4\pi\hbar} S_S^x(\kappa, \omega) \quad S_S^x(\kappa, \omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} F_S(\kappa, t) \exp(-i\omega t) dt$$



Results

Comparison with calculation values



Good agreement with direct calculation results

It is considered that the under estimation of the KUNSCA results from the Gaussian approximation.

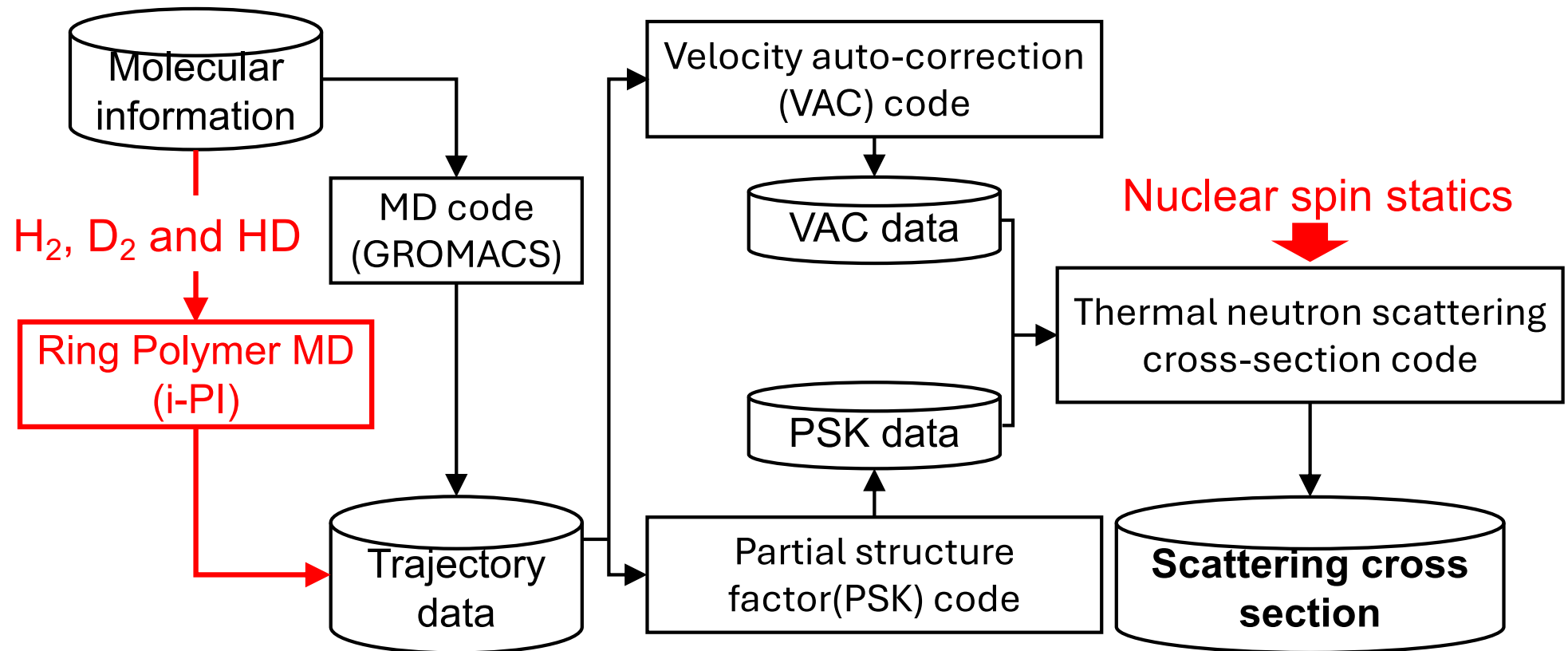
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Calculation for cryogenic moderators

■ New feature in KUNSCA

- Scattering cross section for **Liquid-H₂, -D₂ and -HD**
- **KUNSCA couldn't calculate scattering cross section for them.**



Nuclear quantum effect

Calculation methodology

$$\frac{d^2 \sigma}{d\Omega d\varepsilon} = \frac{k'}{k} \left[u(k) S_d(\kappa, \omega) + \sum_{J_0 J_1 \nu_1} F(\kappa, J_0, J_1, \nu_1) S_s(\kappa, \omega - \omega_{J_0 J_1} - \omega_{\nu_0 \nu_1}) \right]$$

- u, F {
- Nuclear spin statics
 - Spin correlation (ortho/para-H₂, -D₂)
 - $\sigma_{b,coherent/incoherent}$
- J : Rotational quantum number
 ν : Vibrational quantum number
 $\nu_1 = \nu_0$ (Ground state)

Dynamic structure factor

- Self part : $S_s(\kappa, \omega)$
Gaussian approximation
- Distinct part : $S_d(\kappa, \omega)$
Sköld approximation
 $S_d(\kappa, \omega)$
 $= S(\kappa) S_s \left(\frac{\kappa}{\sqrt{S(\kappa)}}, \omega \right) - S_s(\kappa, \omega)$

RPMD simulation condition

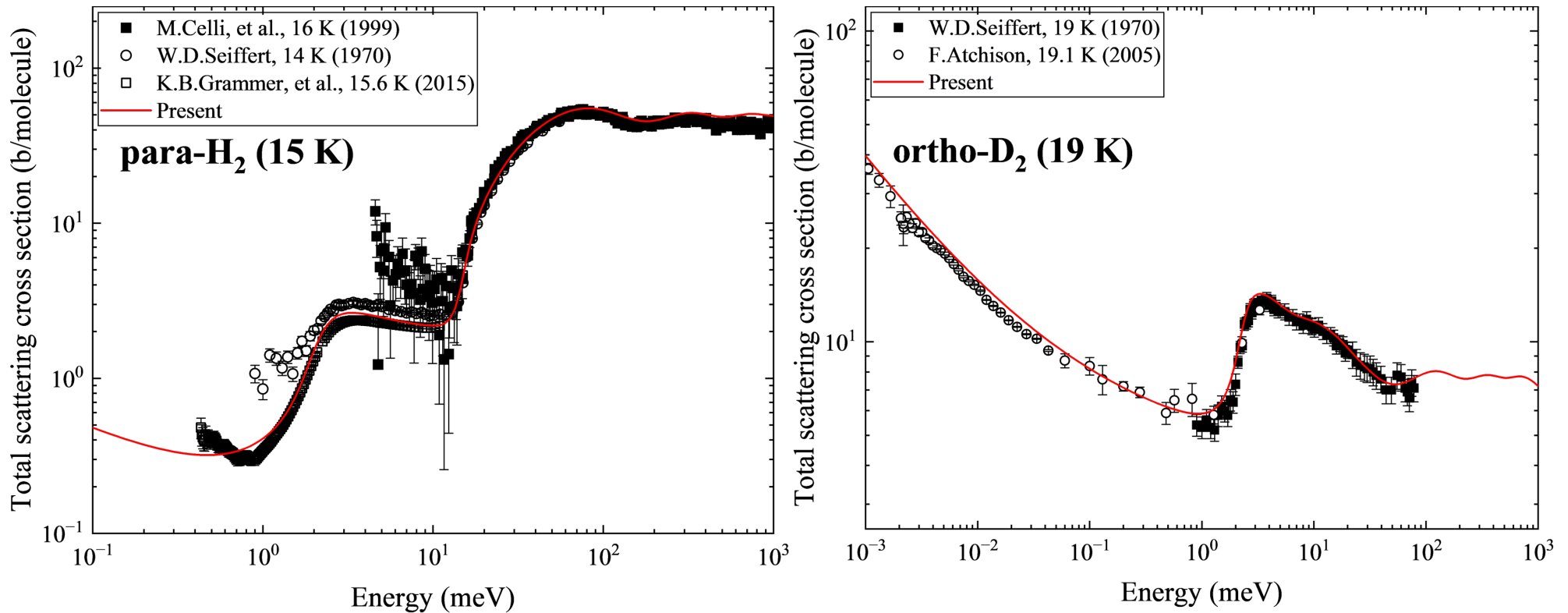
| | |
|---------------------|---|
| Potential | Silvera-Goldman (SG) |
| Number of molecules | 512 |
| Ensemble | (NVT → NPT →) NVT |
| Number of beads | 62 |
| Boundary condition | Periodic boundary |
| Temperature (K) | 15 (H ₂), 19 (D ₂), 17 (HD) |
| Time step (fs) | 0.1 |
| Number of steps | 10 ⁵ |

Equilibrium runs

Results

■ Liquid-H₂ and -D₂

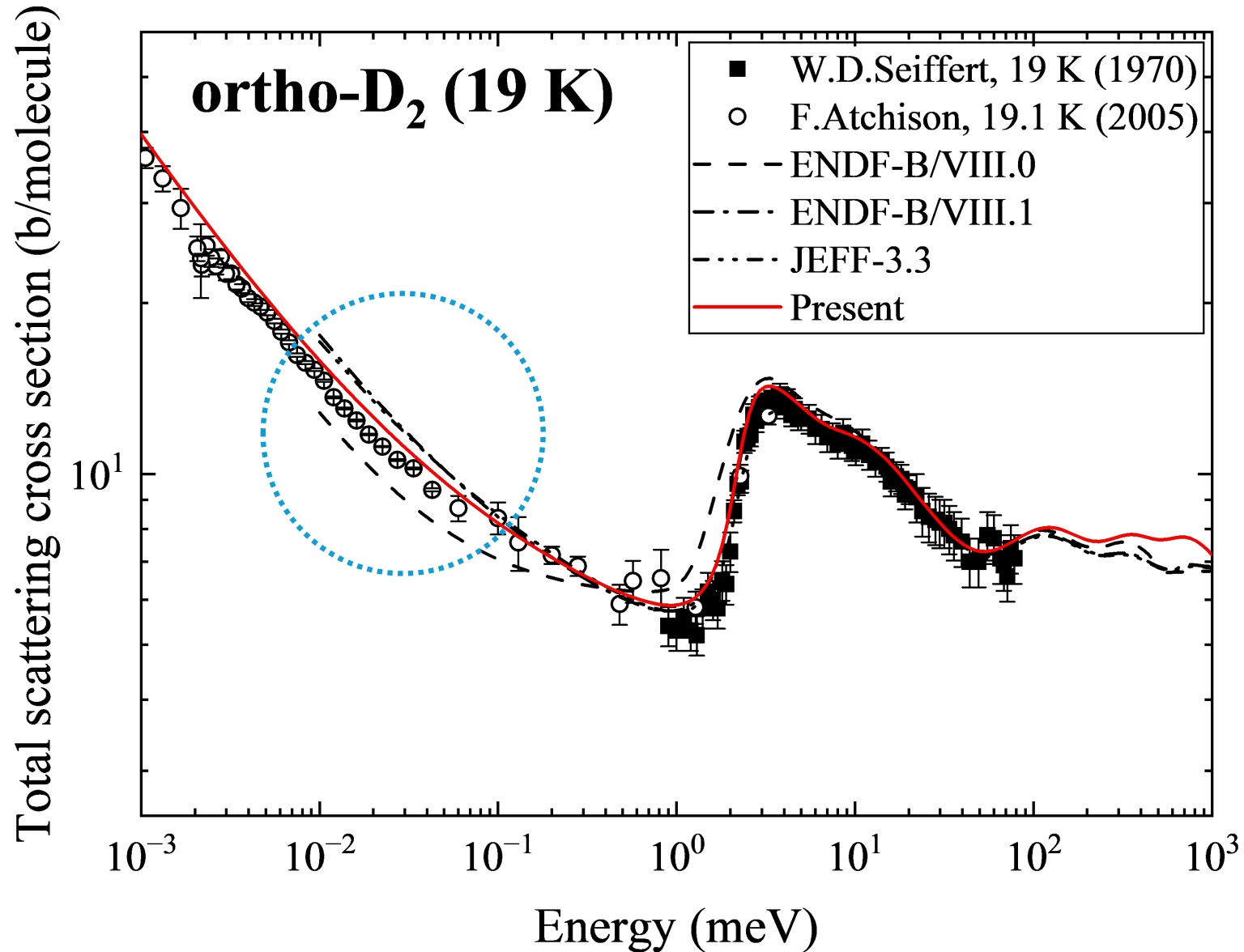
Comparison with experimental data obtained from EXFOR



Good agreement with experimental data

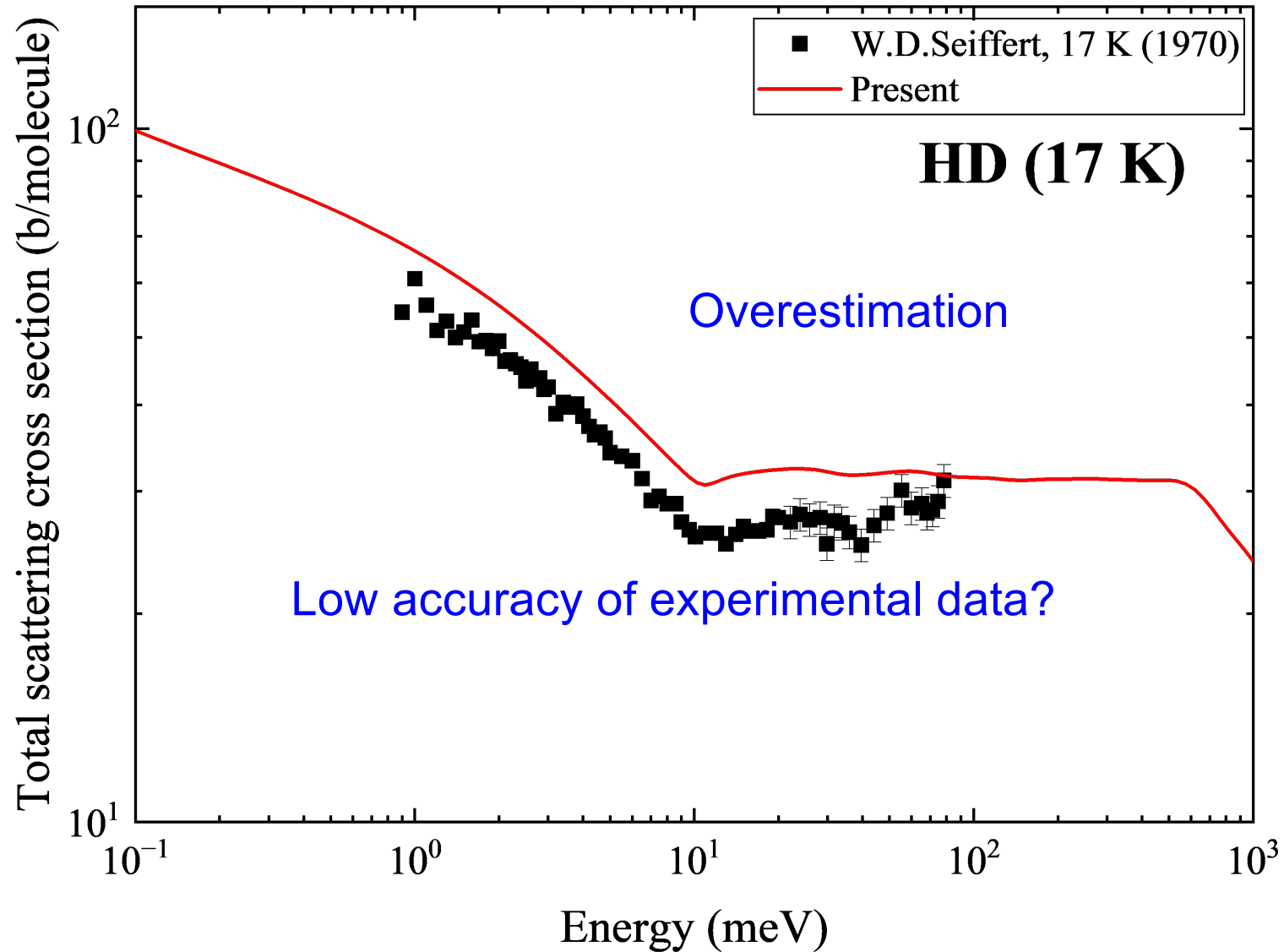
Results

Comparison with nuclear data libraries



Results

■ Liquid-HD



Summary

■ Improvement of scattering cross section for H₂O

The direct calculation results agreed better with experimental DDX values obtained at MLF J-PARC than the KUNSCA results .

■ Calculation of scattering cross section for liquid-H₂, -D₂ and -HD

New feature in KUNSCA

- H₂ and D₂: Good agreement with experimental data
- HD : Overestimation

Future perspective

Measurement of total cross section and DDX for liquid-H₂, -D₂ and -HD at MLF, J-PARC