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Rotational and magnetic contributions to the thermal neutron cross section of air

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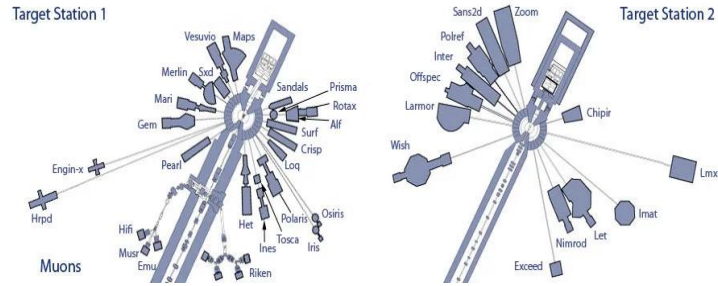
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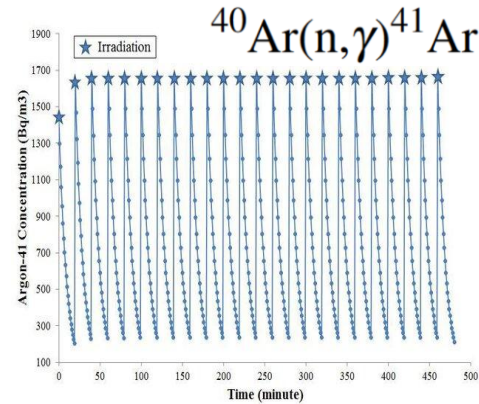
Motivation

Thermal neutron cross sections are essential for **Monte Carlo** transport simulations used to guide device design and operation. Air presence is often approximated in the design of:

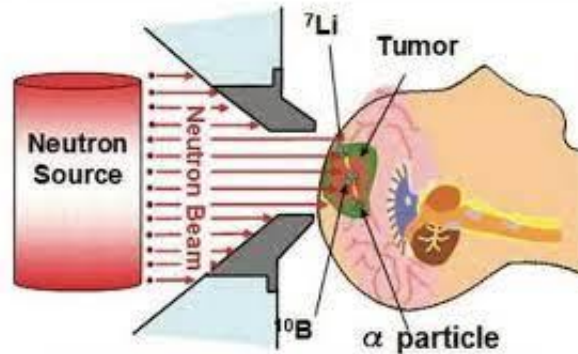


Design and operation of neutron facilities

LINAC for radiotherapy



Boron neutron capture therapy



When operating a LINAC for radiotherapy, **ventilation systems** are used to dilute and remove activated air

Latifah, R & Bunawas, & Noor, Johan. (2018). Journal of Physics: Conference Series

Discrepancies with experimental results are often attributed to uncertainties of **air humidity**, however, **molecular motion is not considered!**

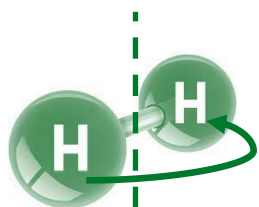


e.g.: *J Appl Crystallogr.* 2015 Jun 27;48(Pt 4):1055-1071.

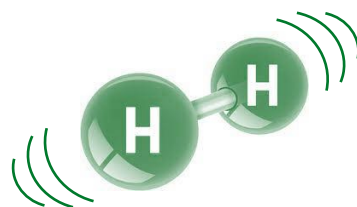
Young and Koppel model

The cross section of diatomic molecules such as N_2 and O_2 depends on multiple degrees of freedom and is not well approximated by a free gas model. Diatomic molecules can:

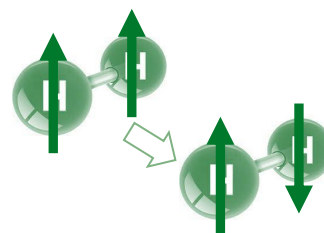
rotate about their centre of mass



vibrate along their axis



flip their spin

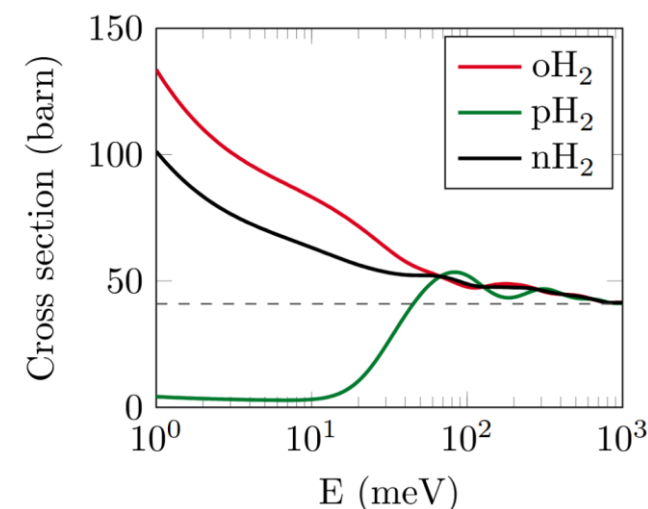
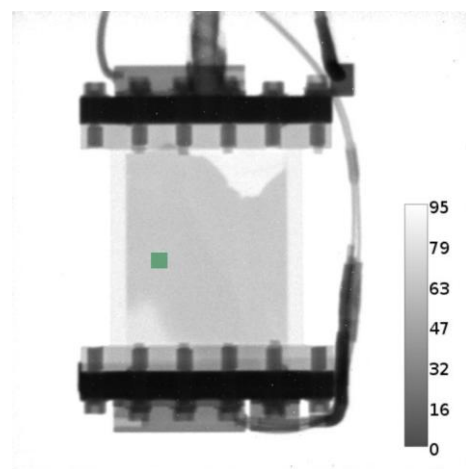


and move in space



The cross section of diatomic molecules can be calculated using the **Young and Koppel model**

J. A. Young and J. U. Koppel. Slow neutron scattering by molecular hydrogen and deuterium. *Phys. Rev.*, 135:A603–A611, Aug 1964.



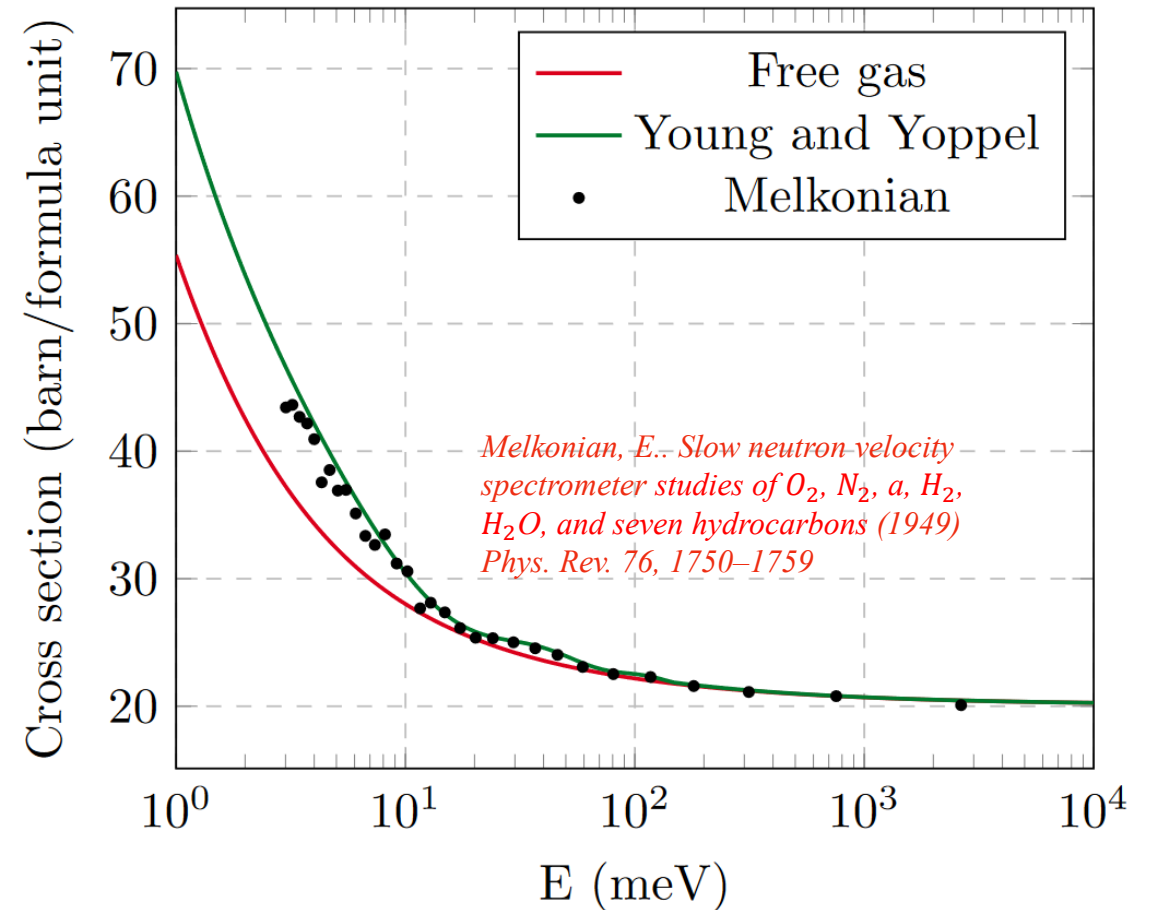
-Simoni, M., Minniti, T., Senesi, R., & Romanelli, G. (2023). Molecular specificity in neutron imaging: the case of hydrogen adsorption in metal organic frameworks. *Phys. Chem. Chem. Phys.* 25, 30821–30831.

Thermal neutron cross section of N_2

We performed the calculation of thermal neutron cross section of diatomic molecules that are abundant in air

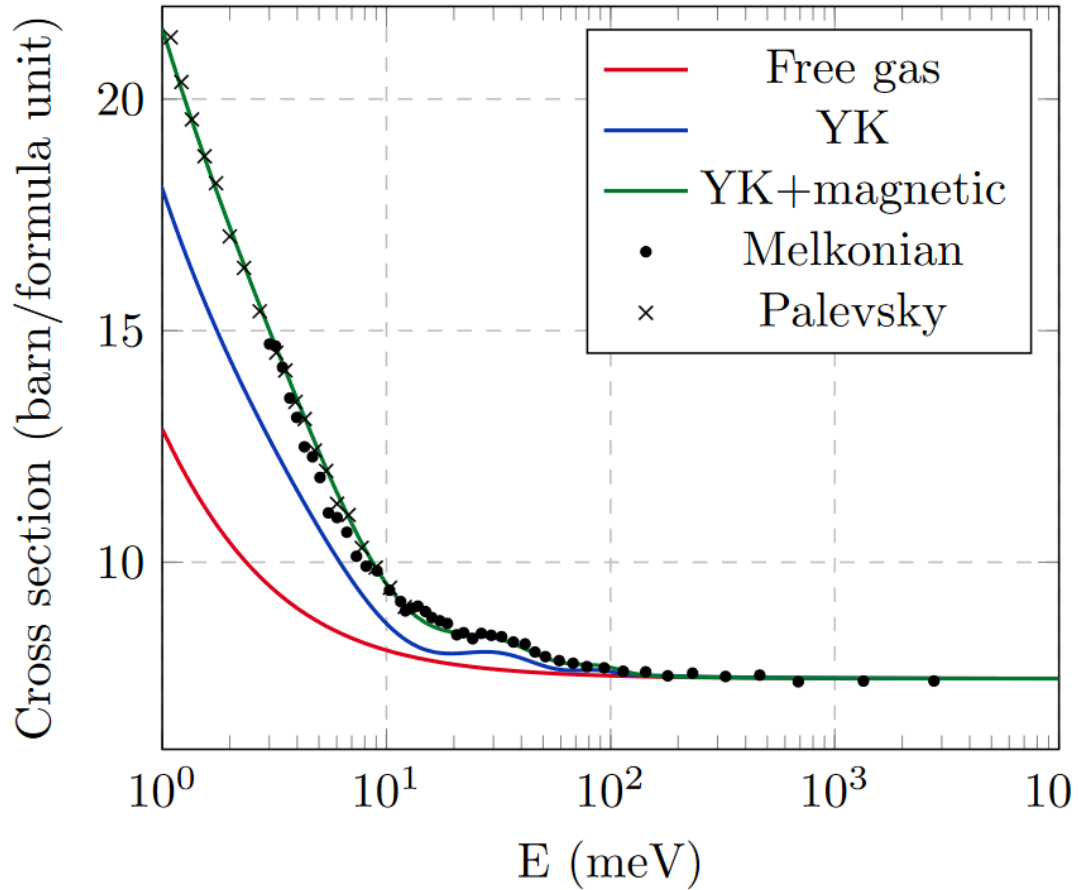
Molecule	Total Sym.	I	J	Electronic ground state
N_2	$S = S \times S \times S$	2 (ortho)	0,2,...	$^1\Sigma_g^+$
	$S = A \times A \times S$	1 (para)	1,3,...	
	$S = S \times S \times S$	0 (ortho)	0,2,...	
O_2	$S = S \times A \times A$	0 (ortho)	1,3,...	$^3\Sigma_g^-$

Neutron scattering cross section was estimated using **Young and Koppel model**, and compared to the free gas model and to experimental data from 1955.

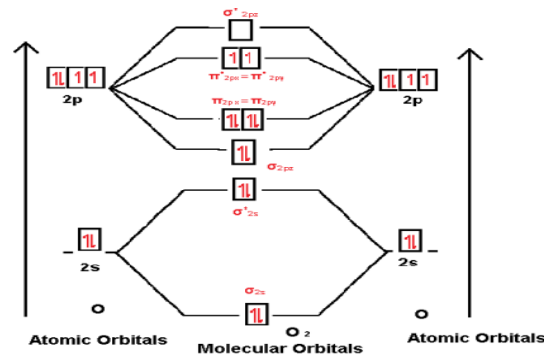


Thermal neutron cross section of O_2

Molecular Oxygen



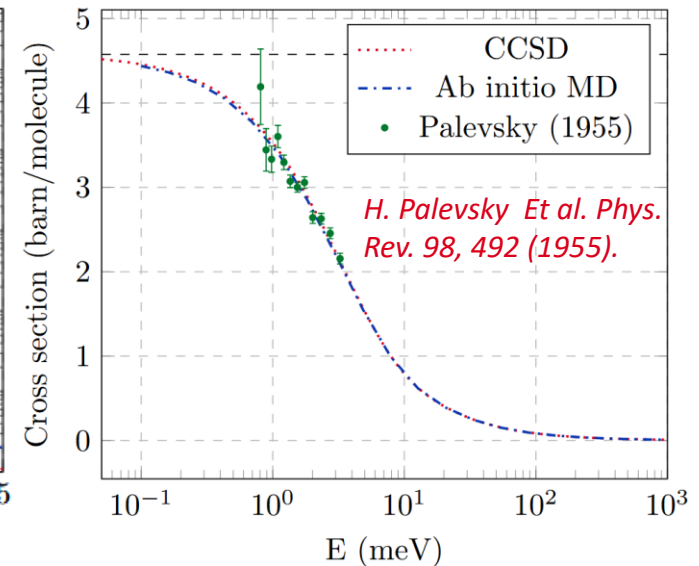
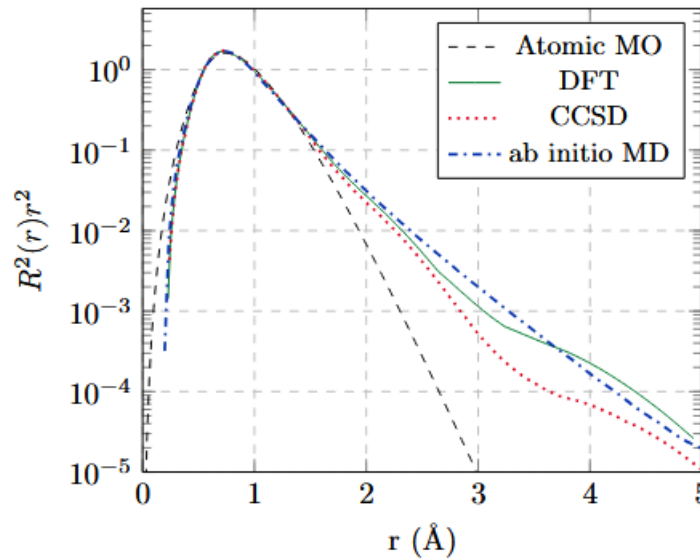
Young and Koppel model was not enough to reproduce O_2 cross section: Its paramagnetic behaviour need to be considered.



$$\frac{d\sigma_s}{d\Omega} = \frac{2}{3} \left(\frac{\mu}{m_n} \right)^2 \gamma^2 r_0^2 S(S+1) e^{-2W(Q)} f^2(Q)$$

$$f(Q) = \int_0^\infty j_0(Qr) r^2 R^2(r) dr$$

W. H. Kleiner, "Magnetic scattering of slow neutrons from o_2 gas," *Phys. Rev.* 97, 411–418 (1955).



H. Palevsky Et al. *Phys. Rev.* 98, 492 (1955).

Thermal neutron cross section of air

Air composition was approximated as:

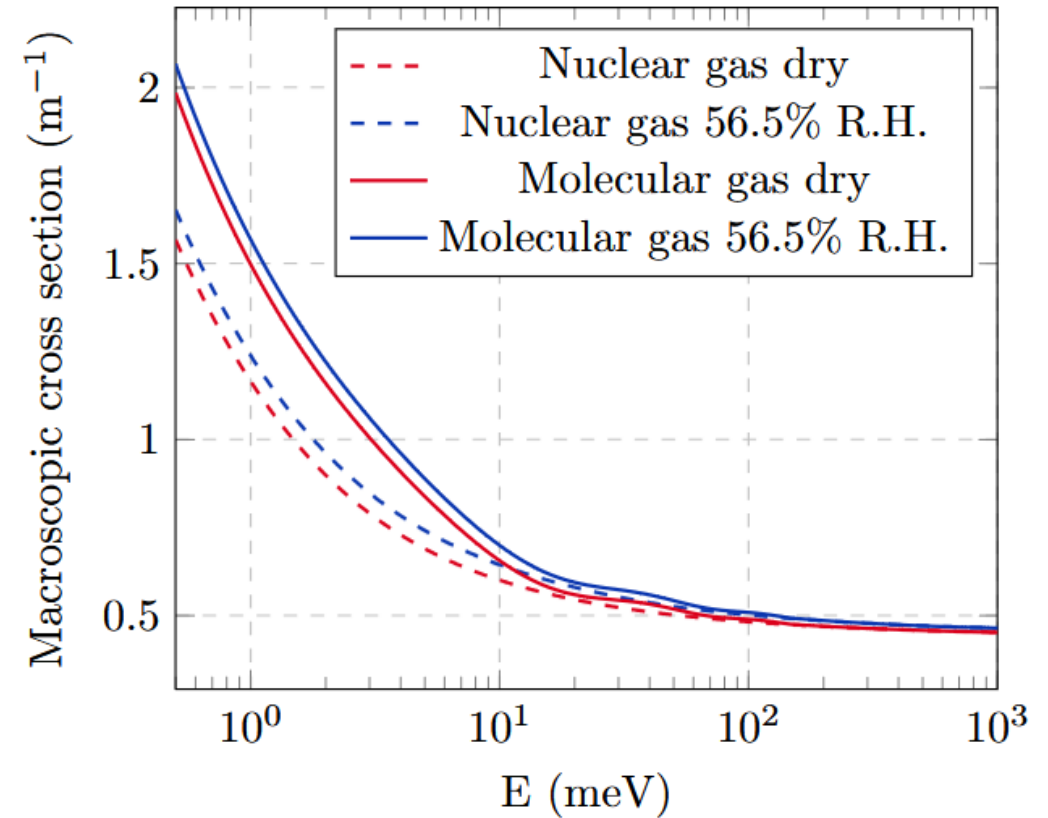
Isotope	mol% in dry air	mol% in hydrated air	Reaction	Absorption XS (barn)
^{14}N	0.7848	0.7696	$^{14}\text{N}(n,\gamma)^{15}\text{N}$	0.075
			$^{14}\text{N}(n,p)^{14}\text{C}$	1.84
^{16}O	0.2105	0.2064 in O_2	$^{16}\text{O}(n,\gamma)^{17}\text{O}$	0.0001
		0.0065 in H_2O		
^{40}Ar	0.0047	0.0046	$^{40}\text{Ar}(n,\gamma)^{41}\text{Ar}$	0.66
^1H	0	0.0129	$^1\text{H}(n,\gamma)^2\text{H}$	0.3326

Water was approximated as liquid, with the use of the CAB model:

J. Màrquez-Damià, J. Granada, D. Malaspina, CAB models for water: A new evaluation of the thermal neutron scattering laws for light and heavy water in ENDF-6 format. *Ann. Nucl. Energy* 65, 280–289 (2014)

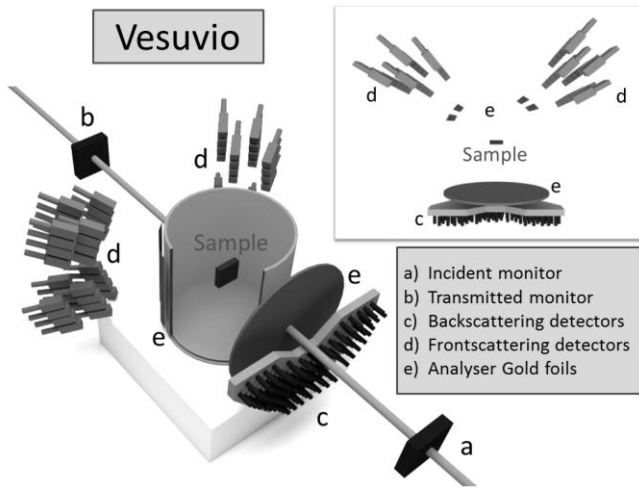
- Mole fraction of water vapour was calculated according to appendix A.1 of <https://www.nist.gov/system/files/documents/calibrations/CI-PM-2007.pdf>

Parameter	Value
Air Density	0.001225 g/cm ³
Humidity	56.5 %
Pressure	1.013 × 10 ⁵ Pa
Temperature	293.6 K



We found that air cross section is strongly affected by molecular rotations!

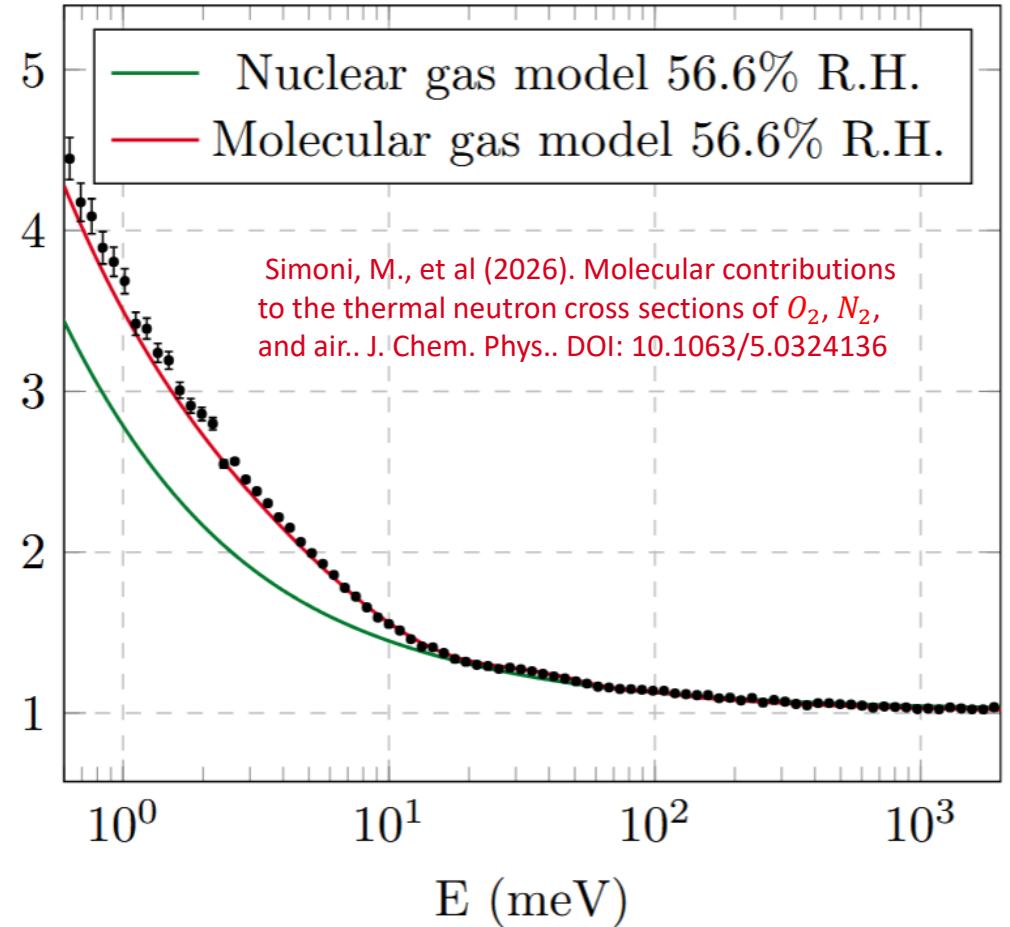
Measuring neutron cross section of air



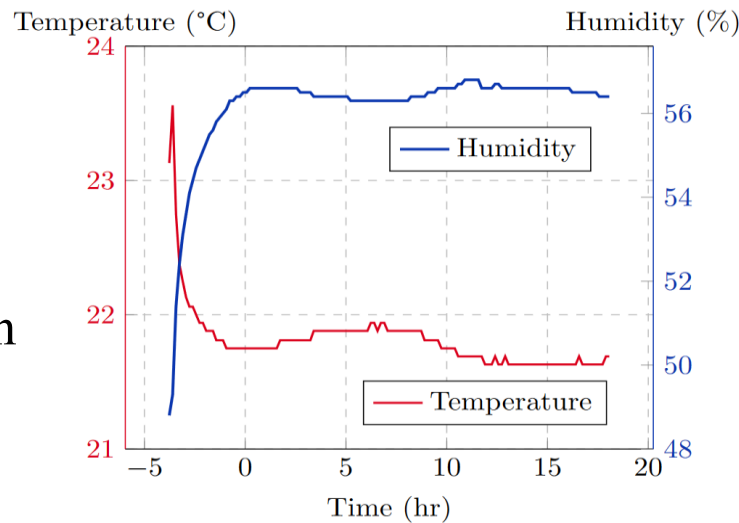
VESUVIO
spectrometer was employed to perform **transmission measurements**

UKRI Science and Technology Facilities Council
ISIS Neutron and Muon Source

Free gas and molecular gas models are compared to experimental data:



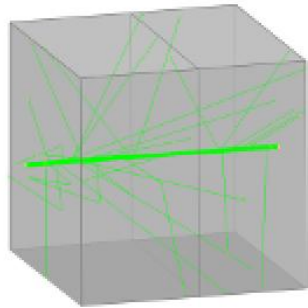
- Good geometry was checked through Monte Carlo simulation



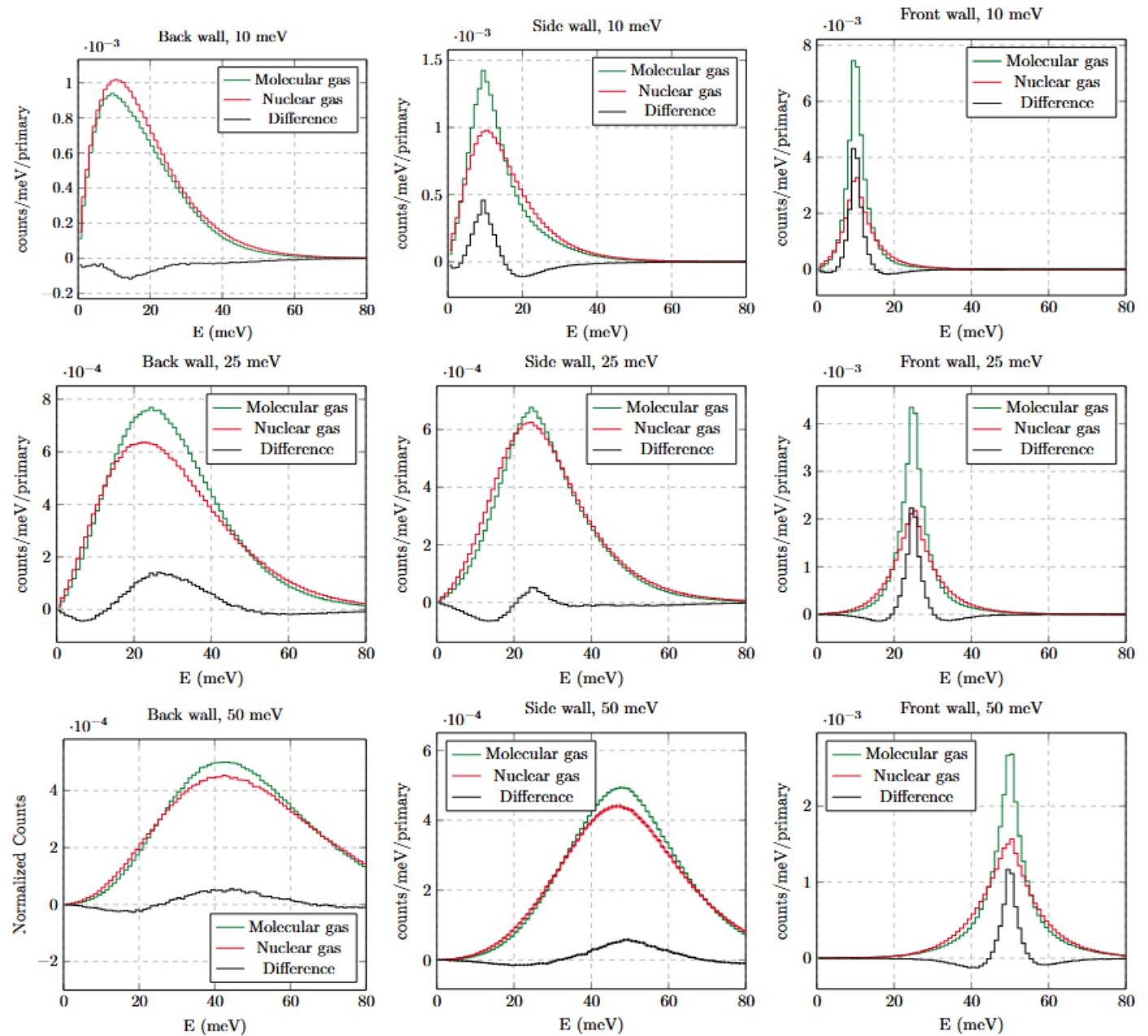
Monte Carlo transport simulations

Geant 4 transport simulations with the
use of the Ncrystal toolkit


X. Cai, T. Kittelmann, **Ncrystal**: A library for thermal
neutron transport. *Comput. Phys. Commun.* 246,
106851 (2020)



The room is of $3 \times 3 \times 3$ m³. The incident
neutron beam (thick green line) is oriented
along the z axis.



Conclusions and outlook

- The Young and Koppel model, together with the paramagnetic model, proved to better estimate the total cross section of air at a given humidity percentage.
- We plan to improve the model by including gaseous water, instead of liquid.
- We plan to make the model easily accessible, together with the models for homonuclear diatomic molecules
- The model was recently published in  [Simoni, M., et al \(2026\). Molecular contributions to the thermal neutron cross sections of O2, N2, and air. J. Chem. Phys.. DOI: 10.1063/5.0324136](https://doi.org/10.1063/5.0324136)

Thank you for your time!