DE LA RECHERCHE À L'INDUSTRIE

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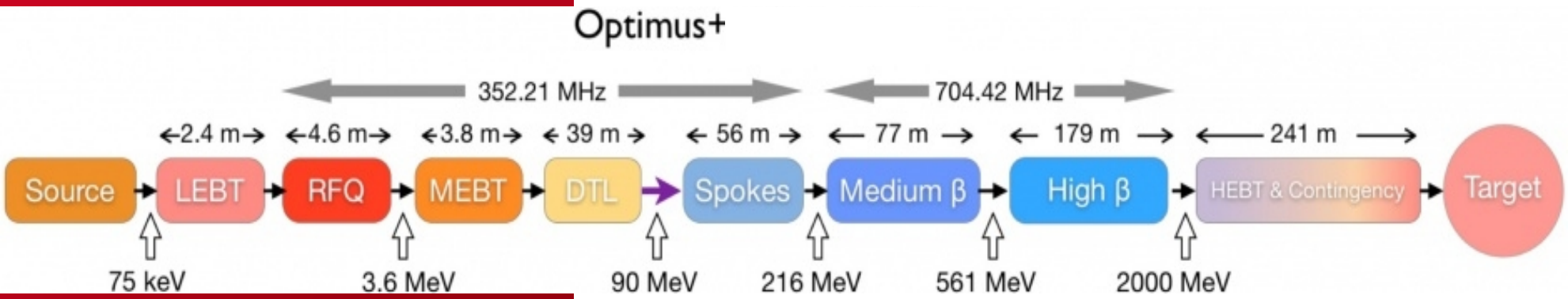
Model of an IPM: investigation on space charge perturbation to the profile measurement



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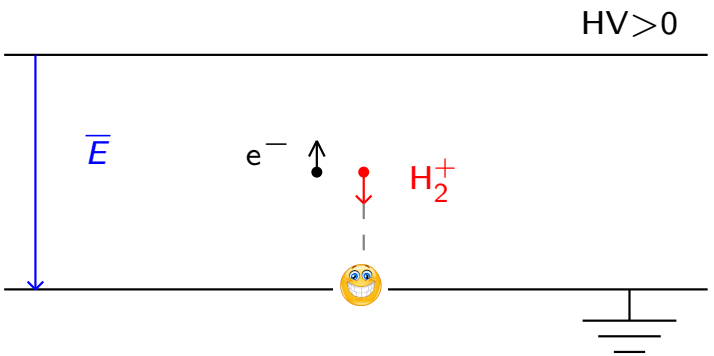
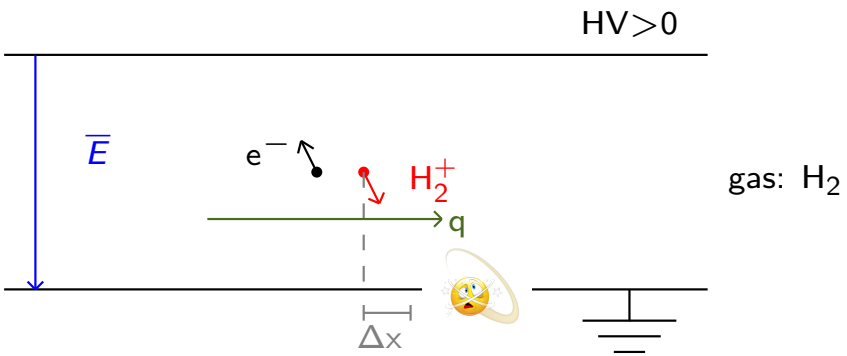
[2] ESS, Lund, Sweden

Space charge effect

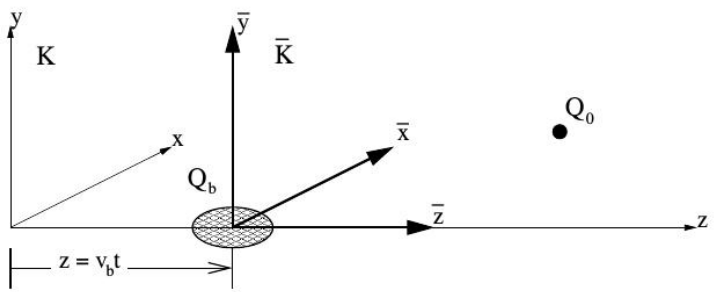
REMINDER:





POSSIBLE CORRECTION METHODS

- Add magnetic field ✗
- High electric field ✓ ✗
- Software correction ✓



SOFTWARE CORRECTION

R. Wanzenberg, Nonlinear Motion of a Point Charge in the 3D Space Charge Field of a Gaussian Bunch.

A Gaussian bunch with total charge $\mathbf{Q}_b$ is moving with the velocity $\mathbf{v}_b$ along the z-axis of the laboratory frame K.
The electric field of the bunch is calculated in the comoving frame and transformed into an electric and magnetic field in the laboratory frame K where the Lorentz-Force on a point charge $\mathbf{Q}_0$ is calculated.

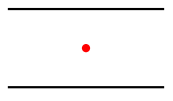
Correction code

CODES:

- MATLAB (**C. Thomas**)
- C++ (translation of the MATLAB code)

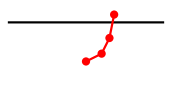
SIMULATION STEPS:

- **a single electron (or ion)** is created in the center of the IPM: x= Gaus(0,σ_x)
  y= Gaus(0,σ_y)
  z = Unif(-2.5 mm, 2.5 mm)



- in a first moment it is assumed that at creation time the electron (or ion) is **at rest**
- a proton bunch of total charge Q = 1.7 e^{-10} C and kinetic energy E_p is considered
- a time step *dt* is chosen by the program
- the displacement $d\overline{x}$ of the electron (or ion) is calculated by solving the motion equation (adaptive Runge Kutta Fehlberg method)

- another time step *dt* is chosen by the program
- the displacement $d\overline{x}$ of the electron (or ion) is calculated by solving the motion equation (adaptive Runge Kutta Fehlberg method)
- time ... displacement ... time ... displacement ...



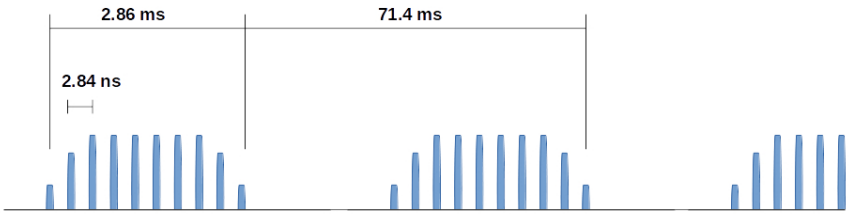
- when the y position of the electron (or ion) y$\geq$ $y_{collection\ plate}$, the simulation stops
- at every *dt* passed, the following variable values were saved: t, x, y, z, v_x, v_y, v_z, a_x, a_y, a_z, fields info (lab and comoving frame)
- t and y are plotted and fitted with a spline to find the time $\mathbf{t}_{stop}$ when the electrode was reached
- t and x are plotted and fitted with a spline. x(t_{stop}) is extracted
- the procedure is iterated N times, to reach a statistical uncertainty of (100 $\frac{\sqrt{N}}{N}$) %

Demo

ESS code parameters

ESS PROTON BEAM PARAMETERS:

- Energy : [90,2000] MeV
- Current peak: 62.5 mA = 0.0625 × 6.242 × 10^{18} p/s
- Pulse length: 2.86 ms
- Pulse frequency: 14 Hz (duty cycle 4%)
- Bunch frequency: 352.21 MHz

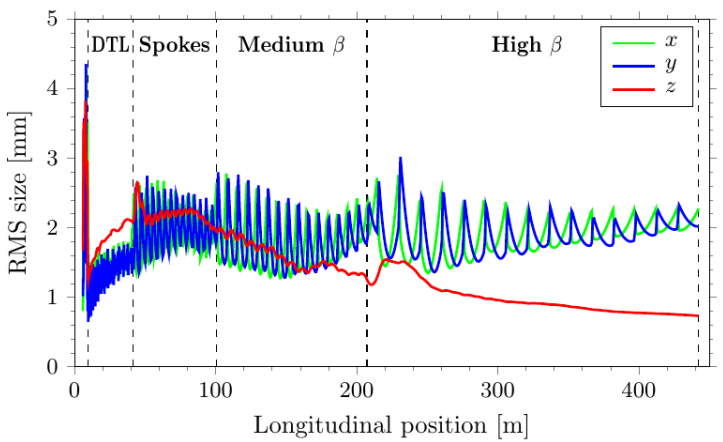


IPM GAS PARAMETERS:

- Composition : H_2 (79%), CO (10%), CO_2 (10%), N_2 (1%) [source: ESS vacuum group]
- Pressure: 10^{-9} mbar

CHOSEN CODE PARAMETERS:

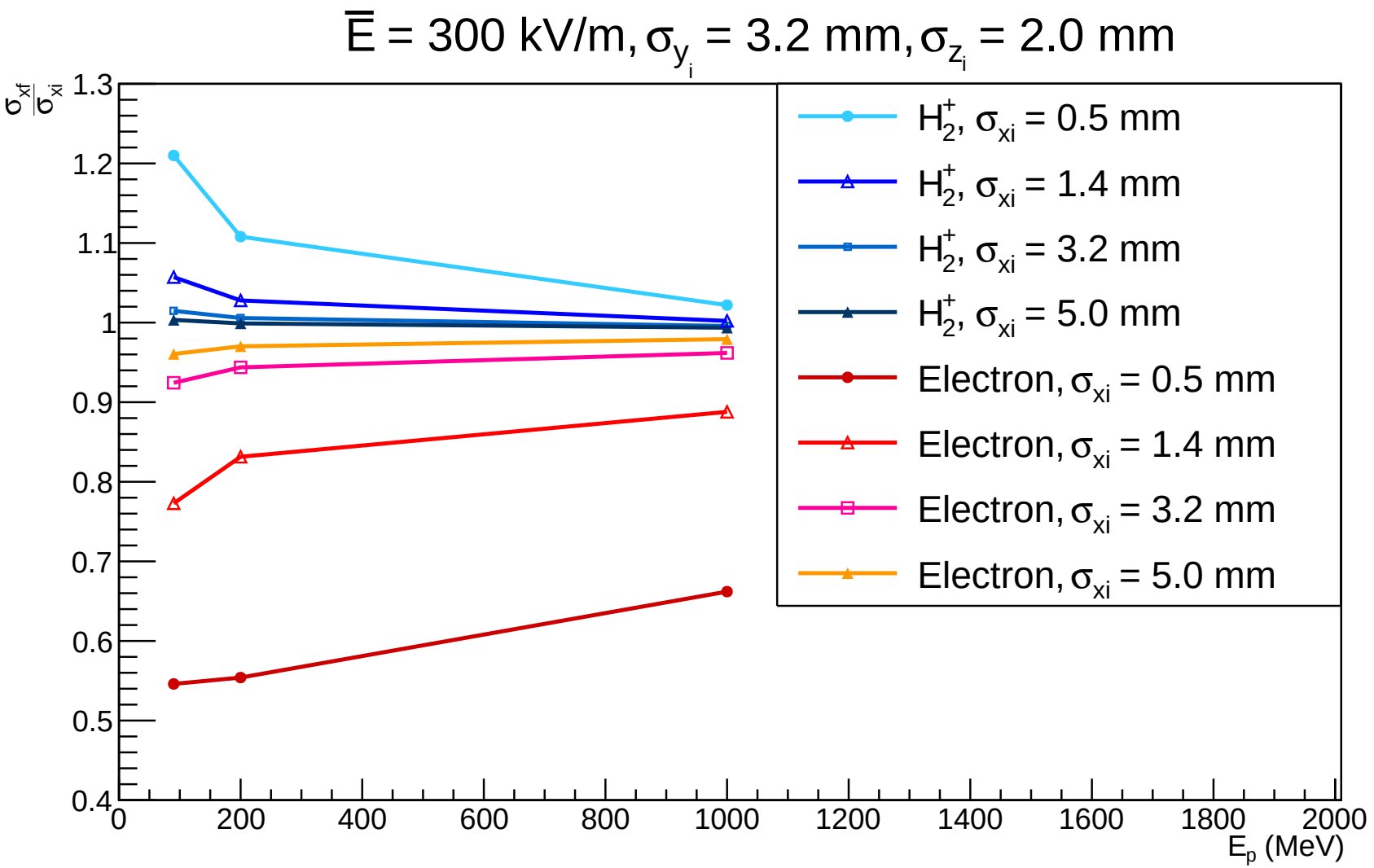
- Proton energies: **90 MeV, 200 MeV, 1 GeV**
- Proton bunch intensity: 62.5 mA/ 352.21 MHz = **1.1 10^{+9} p/bunch**
- σ_x **= 0.5 mm, 1.4 mm, 2.3 mm, 3.2 mm, 4.1 mm, 5 mm, 10 mm**
- σ_y **= 0.5 mm, 1.4 mm, 2.3 mm, 3.2 mm, 4.1 mm, 5 mm, 10 mm**
- σ_z **= 0.75 mm, 2.0 mm, 10 mm**
- Ionization products: **e^-, H_2^+**, N_2^+, CO^+, CO_2^+
- $\overline{E}$: **50 kV/m, 100 kV/m, 200 kV/m, 600 kV/m, 1000 kV/m**



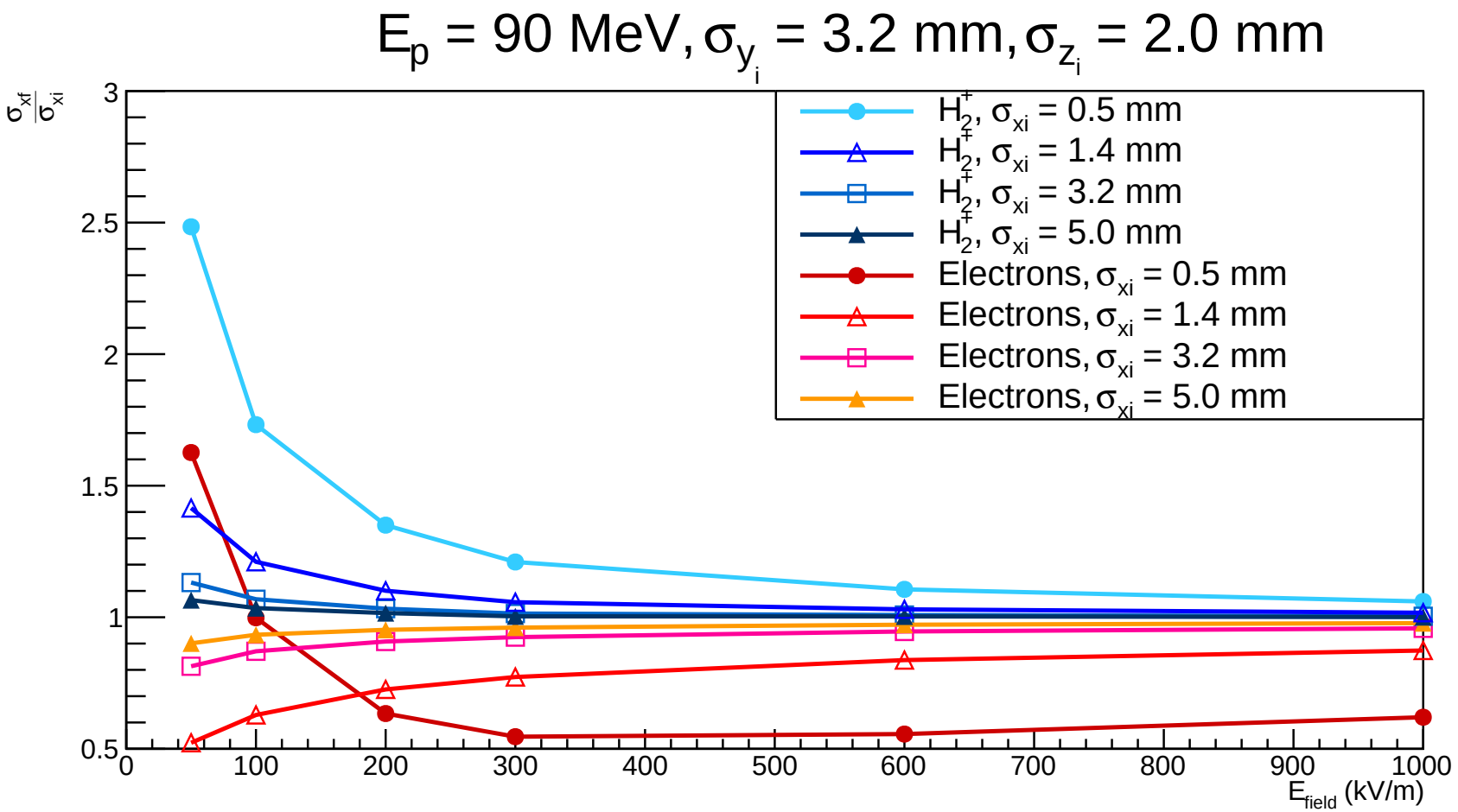
LEVEL 4 REQUIRERMENTS:

- The transvers beam profile shall be measured with a total measurement error in the RMS extension of the beam of less than ± 10%.
- [Space resolution, time tesolution...]

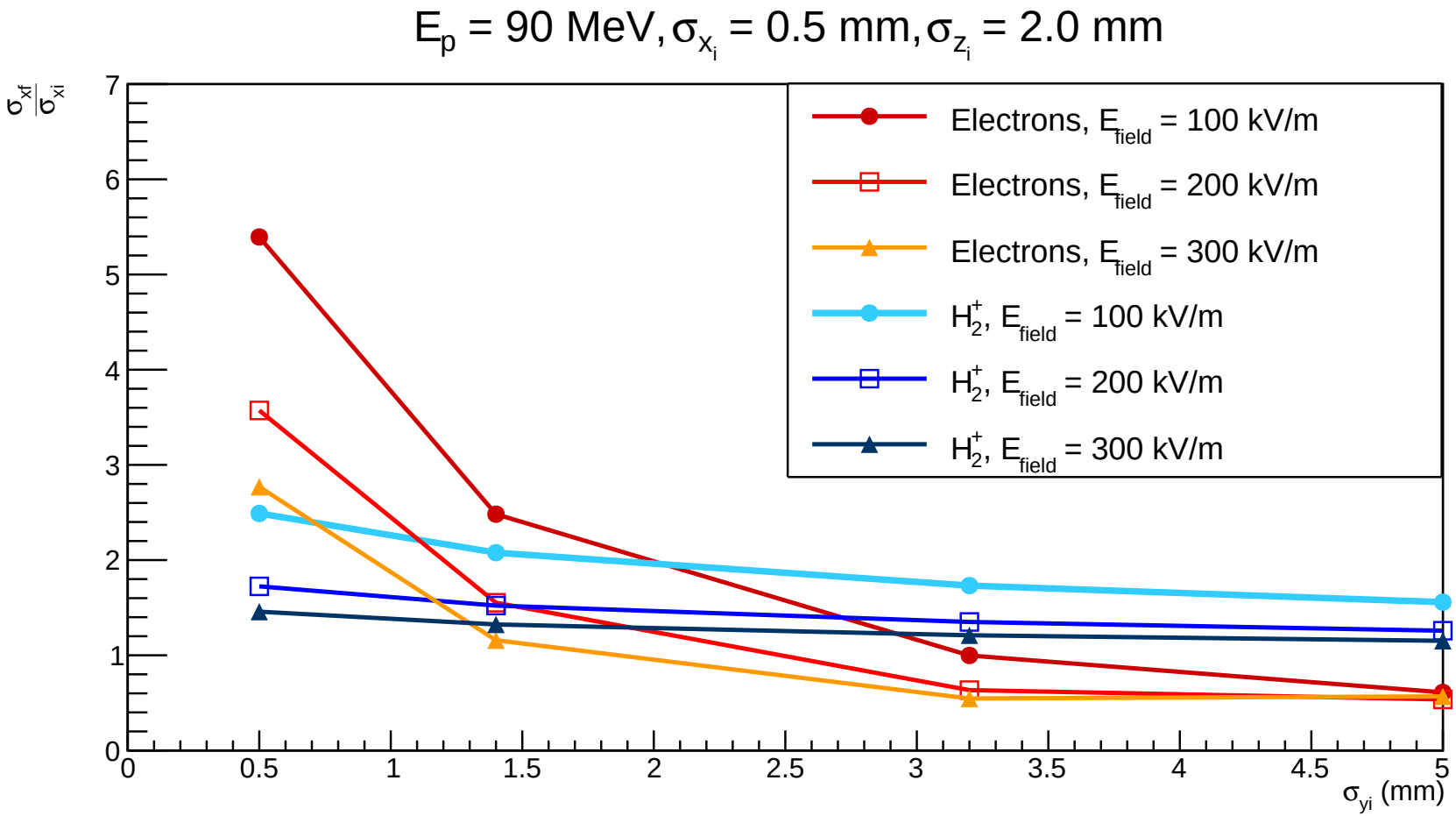
Results: $f(E_p)$


$\bar{E}$ = 300 kV/m, σ_{y_i} = 3.2 mm, σ_{z_i} = 2.0 mm
σ_{xf}/σ_{xi}
1.3
1.2
1.1
1
0.9
0.8
0.7
0.6
0.5
0.4
0
200
400
600
800
1000
1200
1400
1600
1800
2000
E_p (MeV)
H_2^+, σ_{xi} = 0.5 mm
H_2^+, σ_{xi} = 1.4 mm
H_2^+, σ_{xi} = 3.2 mm
H_2^+, σ_{xi} = 5.0 mm
Electron, σ_{xi} = 0.5 mm
Electron, σ_{xi} = 1.4 mm
Electron, σ_{xi} = 3.2 mm
Electron, σ_{xi} = 5.0 mm

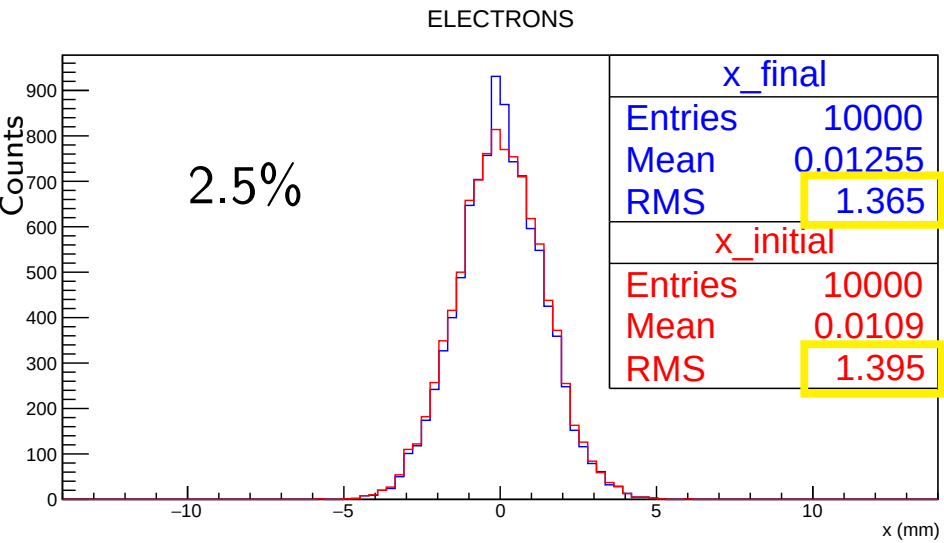
Results: f($\overline{E}$)

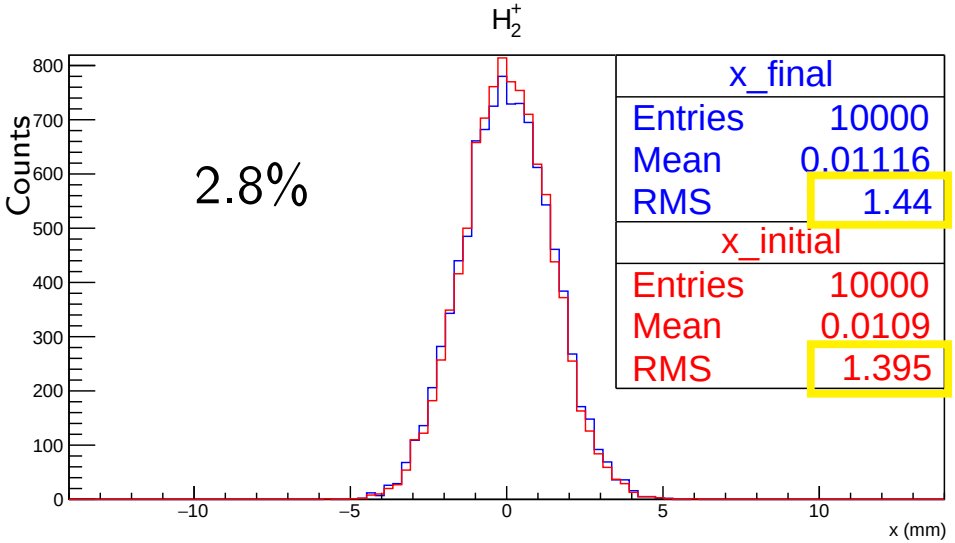


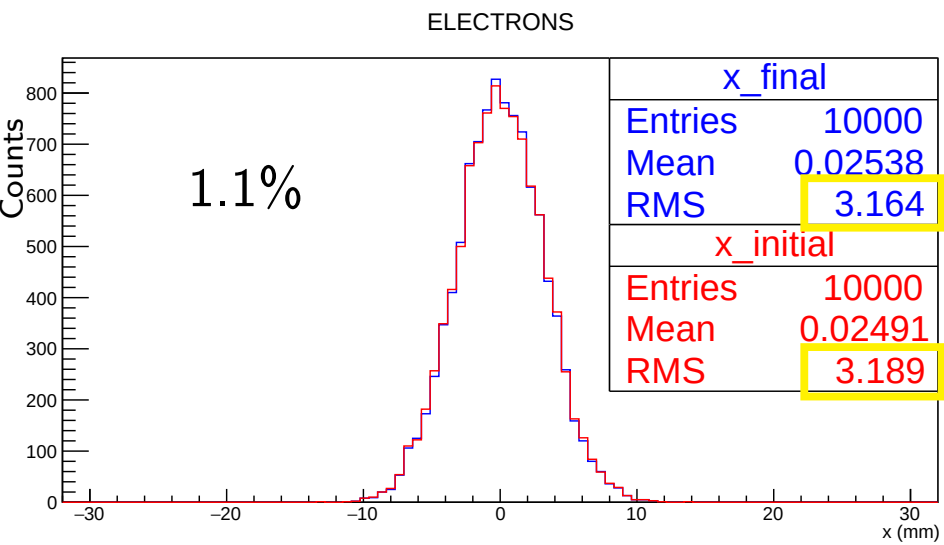
Results: $f(\sigma_{y_i})$

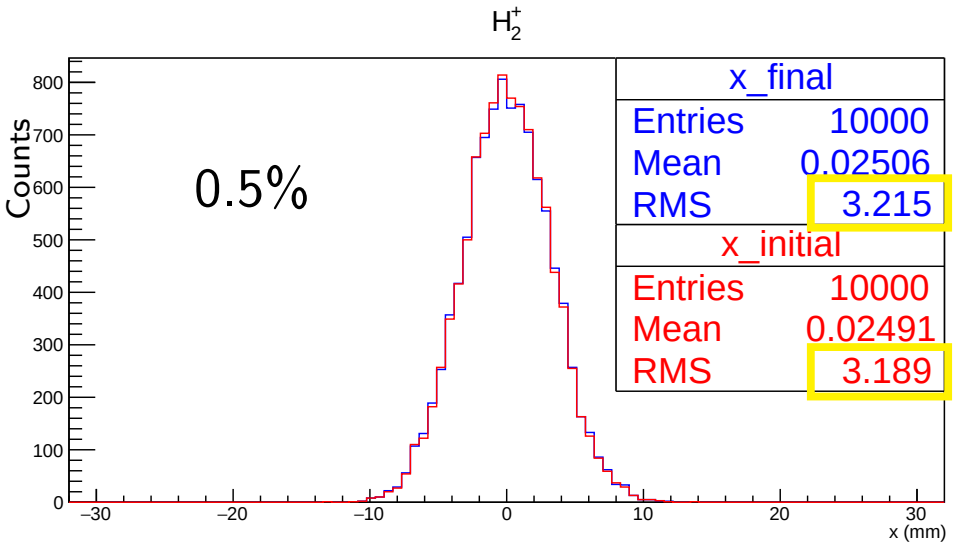


Results: $\sigma_{x_i} = \sigma_{y_i}$ & $\sigma_{z_i} = 2$ mm, $\overline{E} = 300$ kV/m, $E_p = 90$ MeV







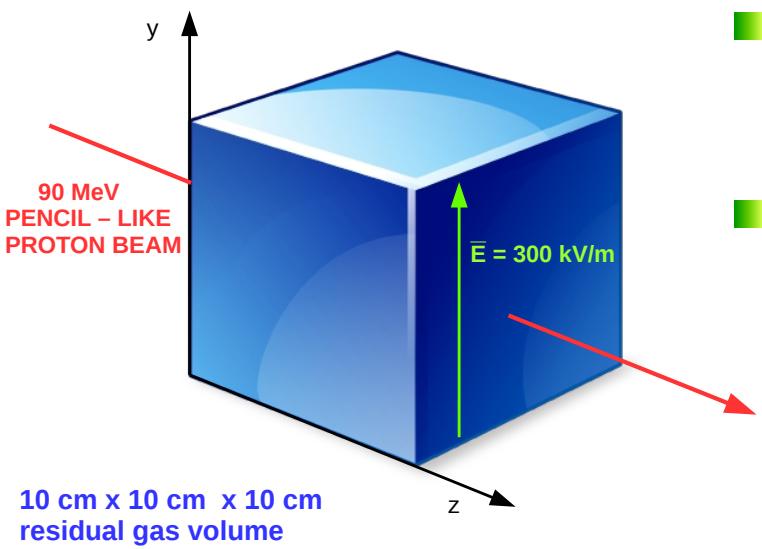


Assumption review: speed

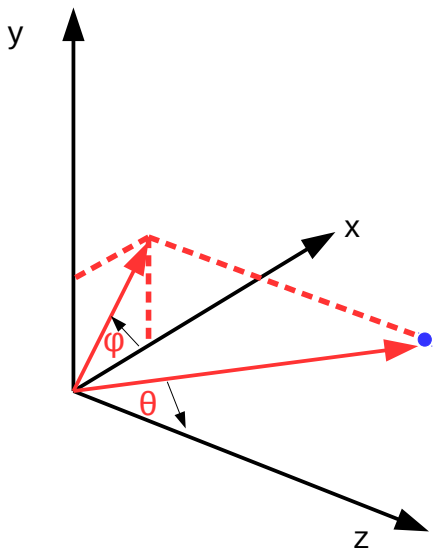
SIMULATION STEPS (Slide 9):

- ...
- in a first moment it is assumed that at creation time the electron (or ion) is **at rest**
- ....

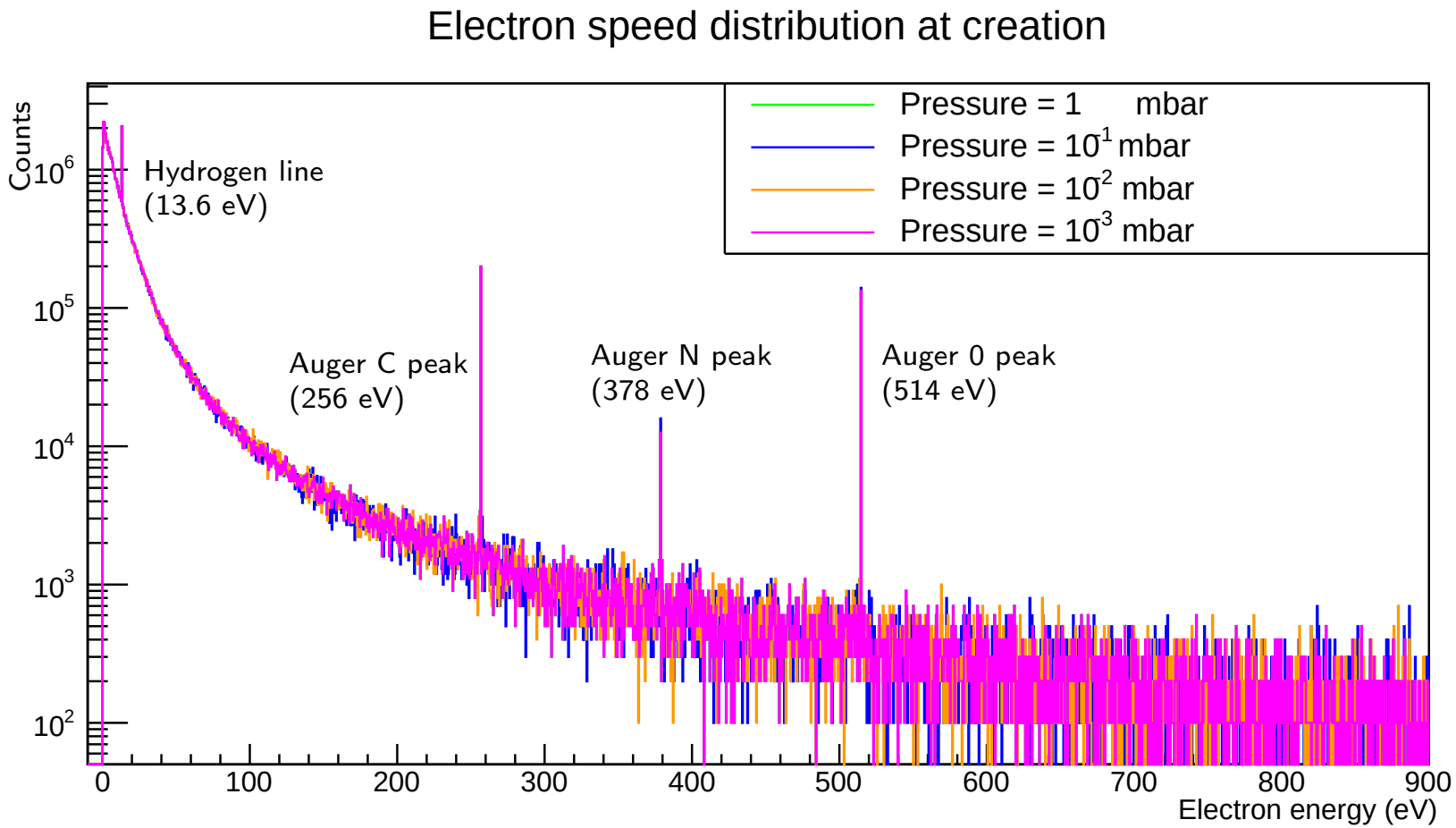
Check assumption validity with Garfield++ (toolkit for simulations of particle detectors with gas and semi-conductors as sensitive medium)



- Different gas densities tested to gain time & statistics
- As for primaries, only electron info can be retrieved



Assumption review: speed



Assumption review: simulations

✓ GARFIELD++ provides different momenta distribution of the primary electrons for different incident proton beam energies and electric fields ($\mathbf{v}_e$, θ_e, ϕ_e).

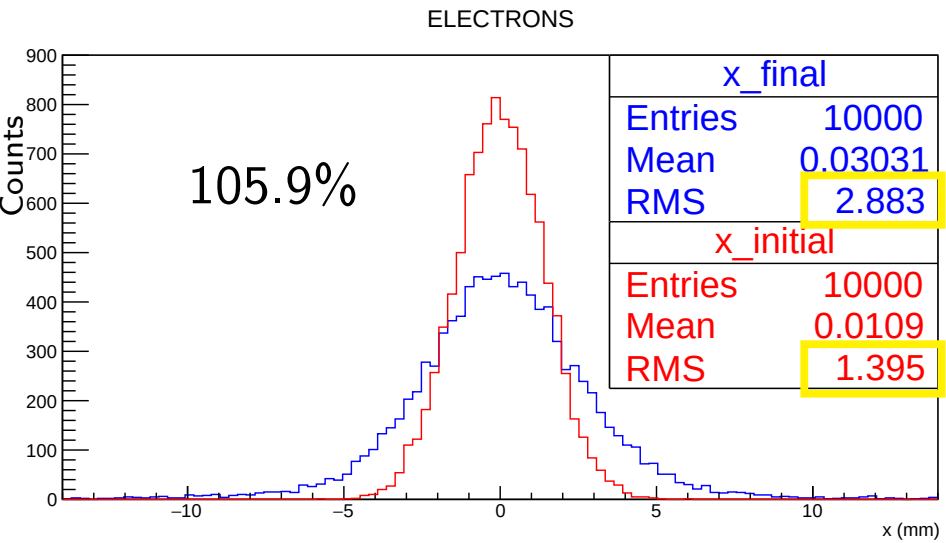
ELECTRONS:

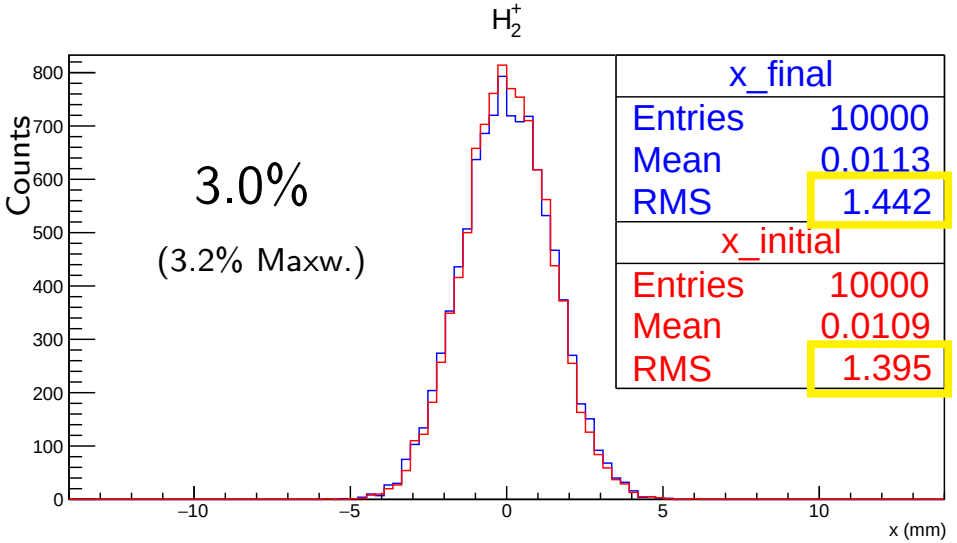
- $E_p = 90$ MeV
- $\overline{E} = 300$ kV/m
- $x_{i_{el}} = f(\sigma_{x_{i_{el}}})$, $y_{i_{el}} = f(\sigma_{y_{i_{el}}})$
- $z_{i_{el}}$ uniformly $\in$ [-5 cm, 5 cm]
- $\sigma_{x_{i_{el}}} = \sigma_{y_{i_{el}}} =$ 0.5 mm, 1.4 mm, 3.2 mm, 4.1 mm, 5.0 mm, 10.0 mm
- $\sigma_{z_{i_{el}}} = 0.75$ mm, 2.0 mm, 10.0 mm
- $\mathbf{v}_{i_{el}}$ from GARFIELD++
- (θ, ϕ) from GARFIELD++

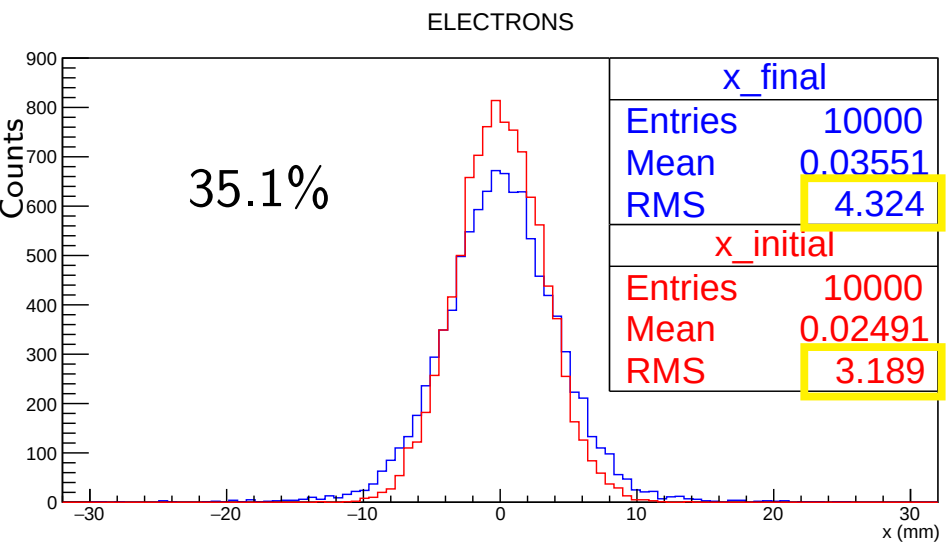
IONIZED MOLECULES:

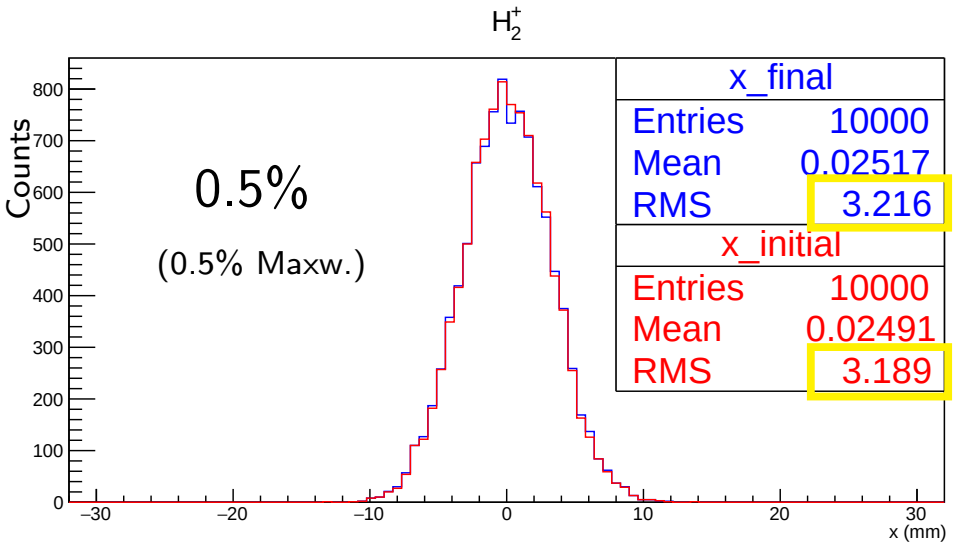
- $E_p = 90$ MeV
- $\overline{E} = 300$ kV/m
- $x_{i_{ion}} = f(\sigma_{x_{i_{ion}}})$, $y_{i_{ion}} = f(\sigma_{y_{i_{ion}}})$
- $z_{i_{ion}}$ uniformly $\in$ [-5 cm, 5 cm]
- $\sigma_{x_{i_{ion}}} = \sigma_{y_{i_{ion}}} =$ 0.5 mm, 1.4 mm, 3.2 mm, 4.1 mm, 5.0 mm, 10.0 mm
- $\sigma_{z_{i_{ion}}} = 0.75$ mm, 2.0 mm, 10.0 mm
- $\mathbf{v}_{i_{ion}}$ assuming
  a) $\mathbf{v}_{i_{electron}} \cdot m_{electron} = \mathbf{v}_{i_{ion}} \cdot m_{ion}$
  b)Maxwellian energy distribution
- (θ, ϕ) from GARFIELD++

Results: $\sigma_{x_i} = \sigma_{y_i}$ & $\sigma_{z_i} = 2$ mm, $\overline{E} = 300$ kV/m, $E_p = 90$ MeV









Conclusions (FILTER 10% L4 constraint)

The results from the IPM simulation code with the above initial conditions show:

- the space charge effect is lower for higher proton energies
- the space charge effect is higher for lower beam sizes (smaller than nominal conditions)
- ionized molecules are less affected by space charge effects than electrons
- the initial momentum with which particles are created can be neglected for ionized molecules, but not for electrons
- if electrons are detected and the beam sizes are $\sigma_{x_i} = \sigma_{x_i} = 3.2$ mm and $\sigma_{z_i} = 2.0$ mm an error of about 35% is obtained (requirements not met)
- if electrons are detected and the beam size is smaller than 2 mm, the error on the beam width is higher than 35% (requirements not met)
- if ionized molecules are detected, in nominal conditions, not more than 4% error on the beam width is obtained
- as for ionized molecules here above H_2^+ was meant. If the totality of the ionized molecules is considered with the appropriate weight, the previously given error improve by few %.

BACKUP SLIDES

Results: heavier ion comparison

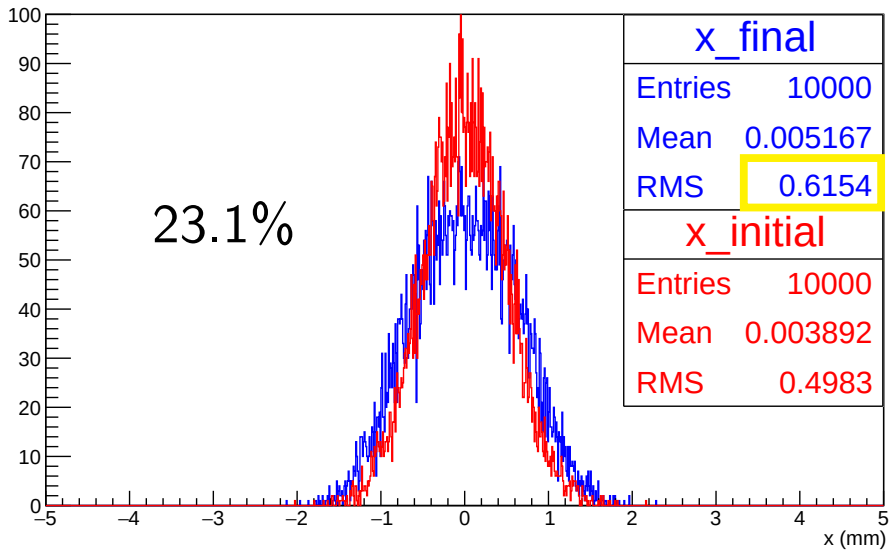
- Initial conditions:

$$\overline{E} = 600 \text{ kV/m}$$
$$E_p = 90 \text{ MeV}$$
$$\sigma_{x_i} = \sigma_{y_i} = 0.5 \text{ mm}$$
$$\sigma_{z_i} = 0.75 \text{ mm}$$

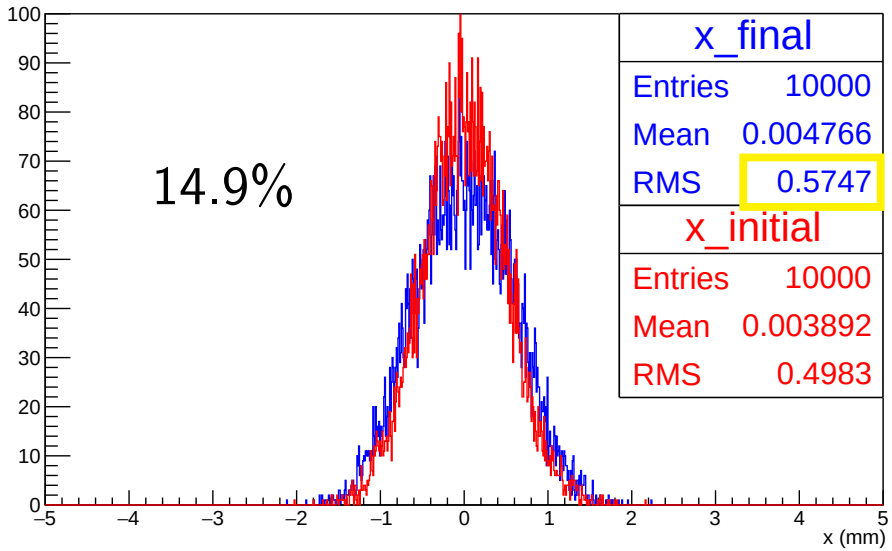
- Remarks:

$$m_{N_2} \approx m_{CO}$$
heavier particle = smaller Δx

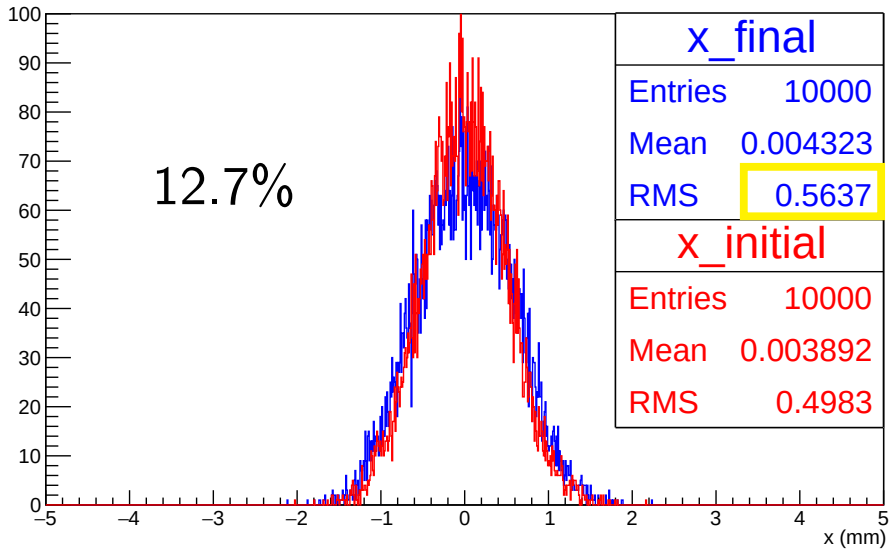
H_2^+



CO^+

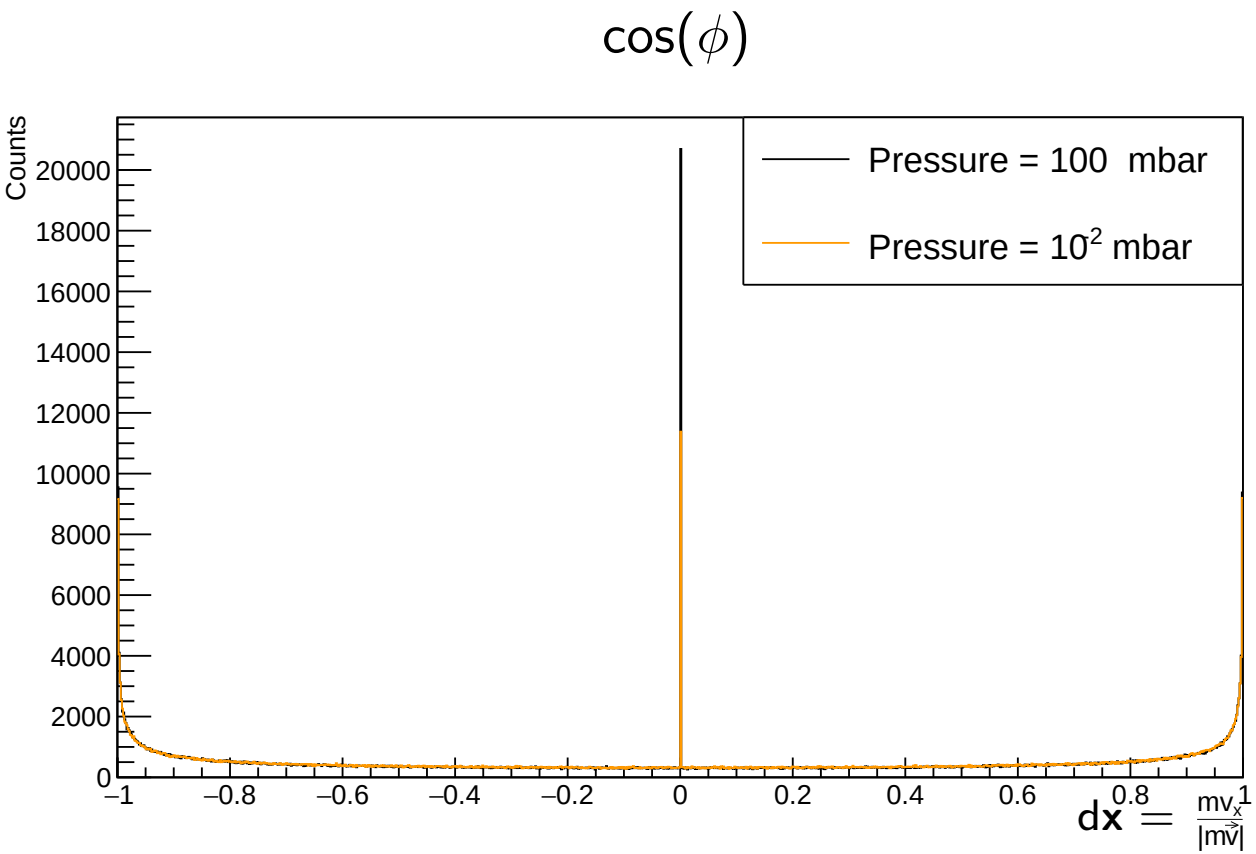


CO_2^+

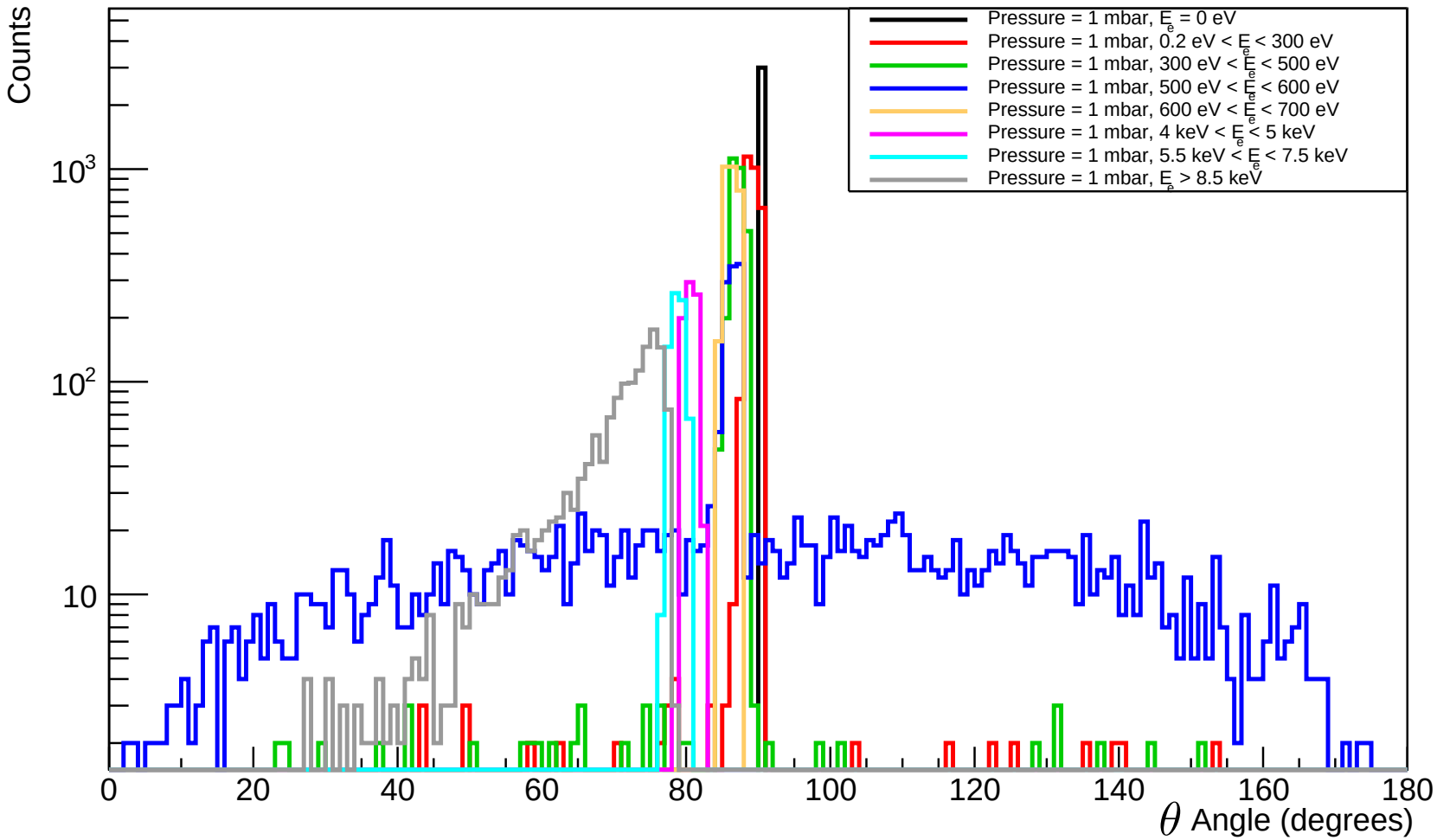


Assumption review: angular distribution

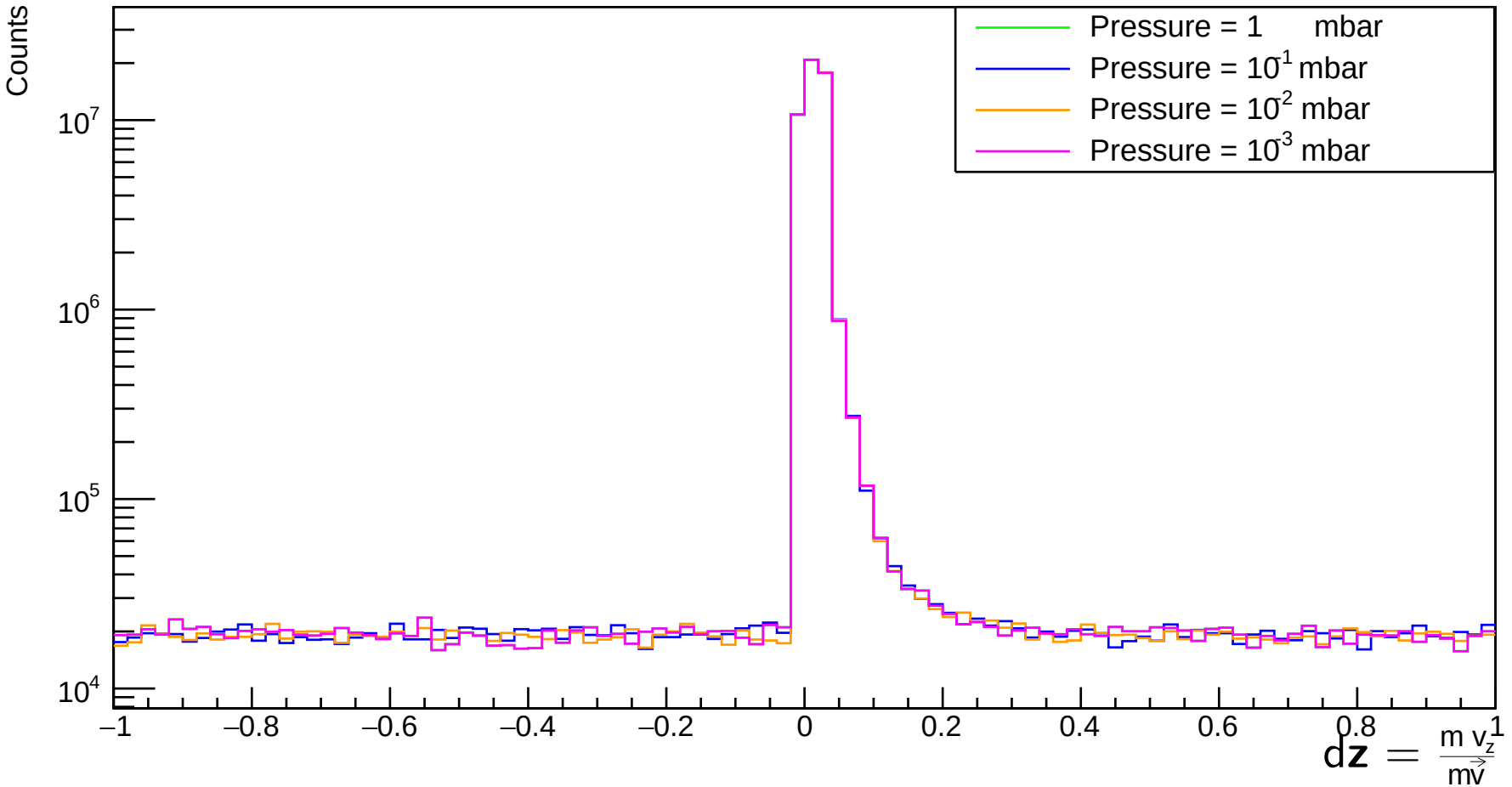
- In GARFIELD++ the ϕ (azimuthal) angle is uniformly sampled in [0,2π) $\Rightarrow$ same distribution for cos(ϕ) & sin(ϕ).
- At higher gas pressures more electrons are emitted with lower speed



Assumption review: angular distribution



Assumption review: angular distribution



Assumption review: simulations